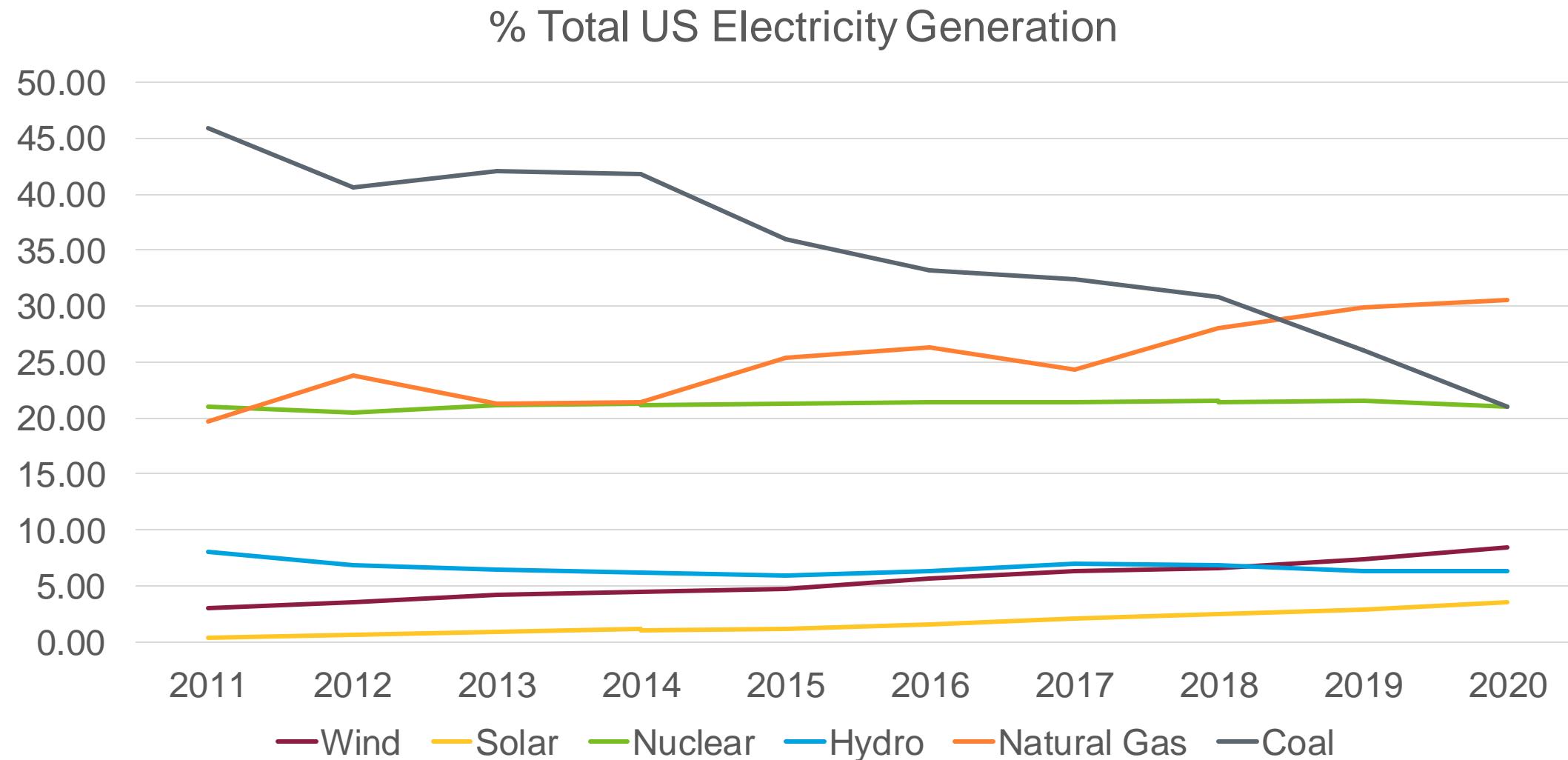


Module 2

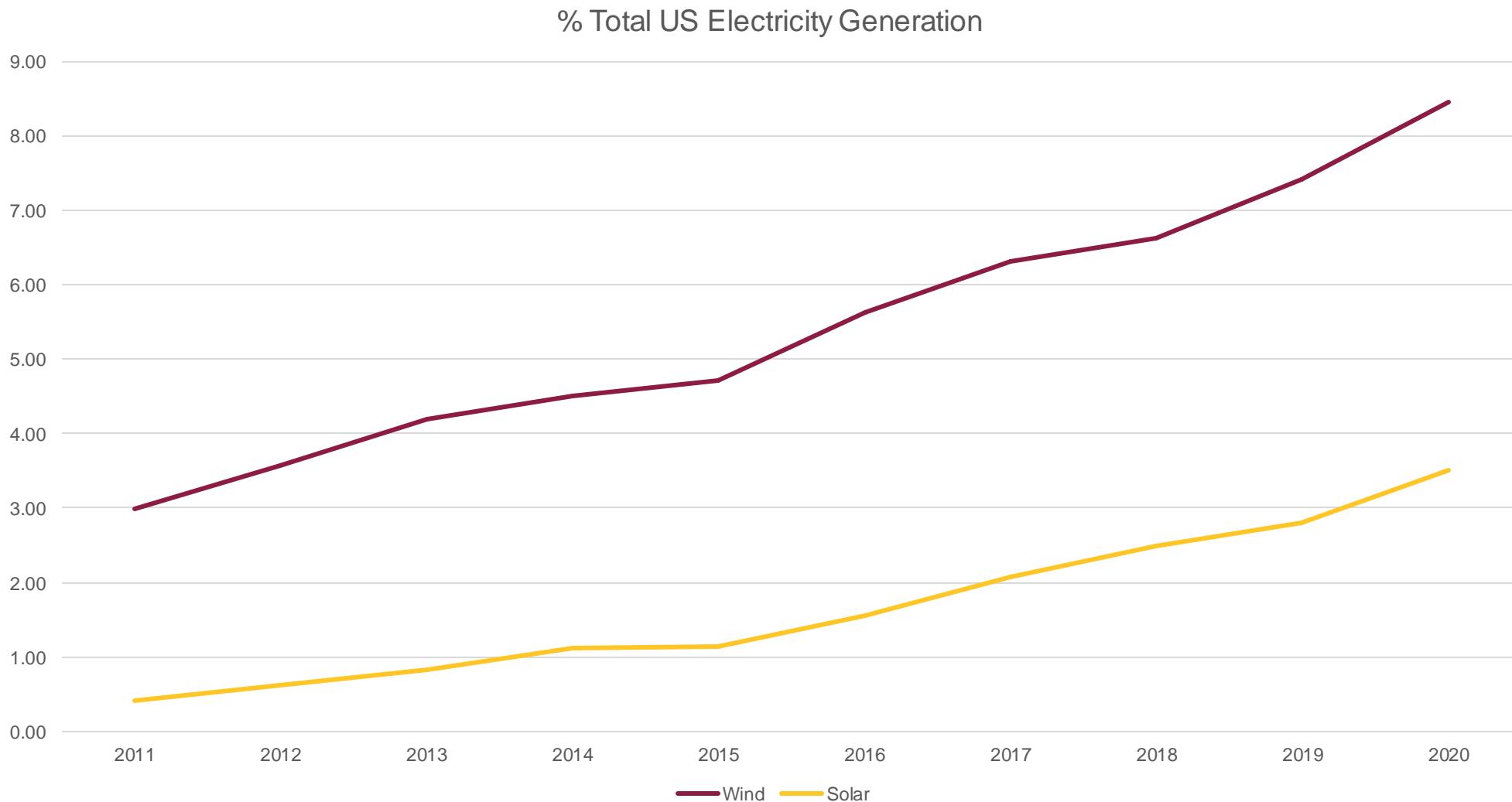
Solar, Wind, and Power Electronics

How do we interface renewable resources to the grid?

Evolution of Electricity Generation



Solar and Wind are Making Huge Gains

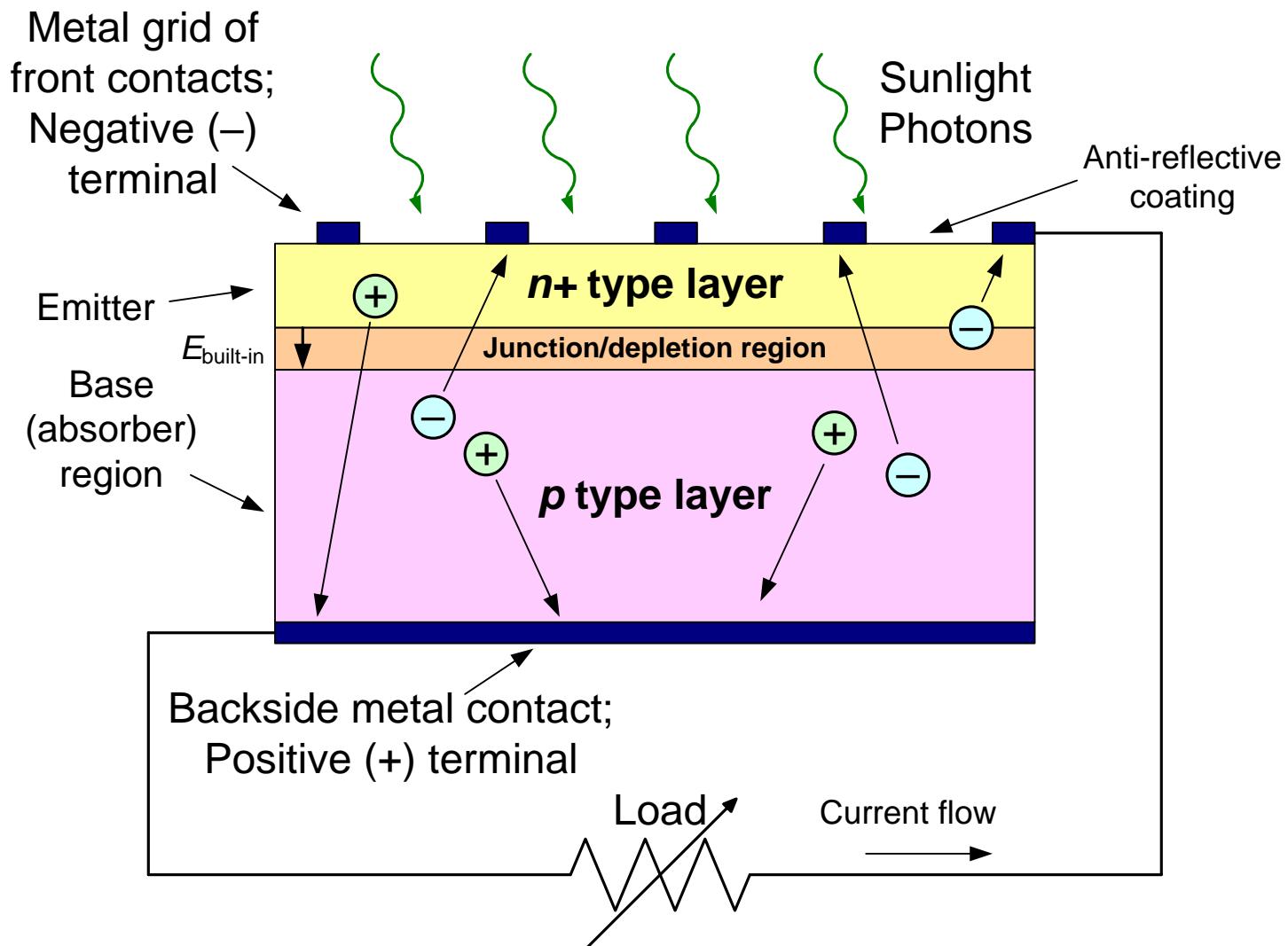


Module 2a

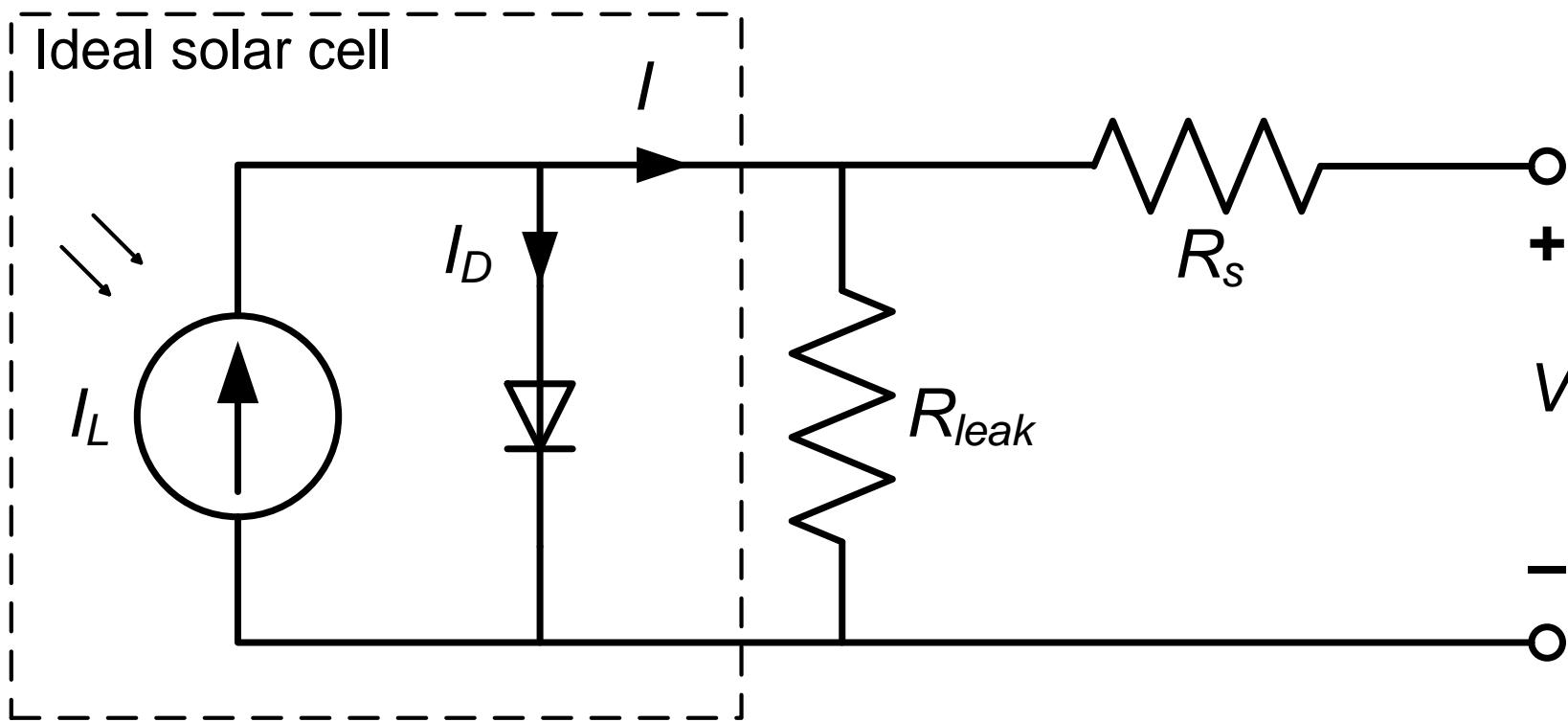
Solar Energy

How does it work and how do we connect it to the power system?

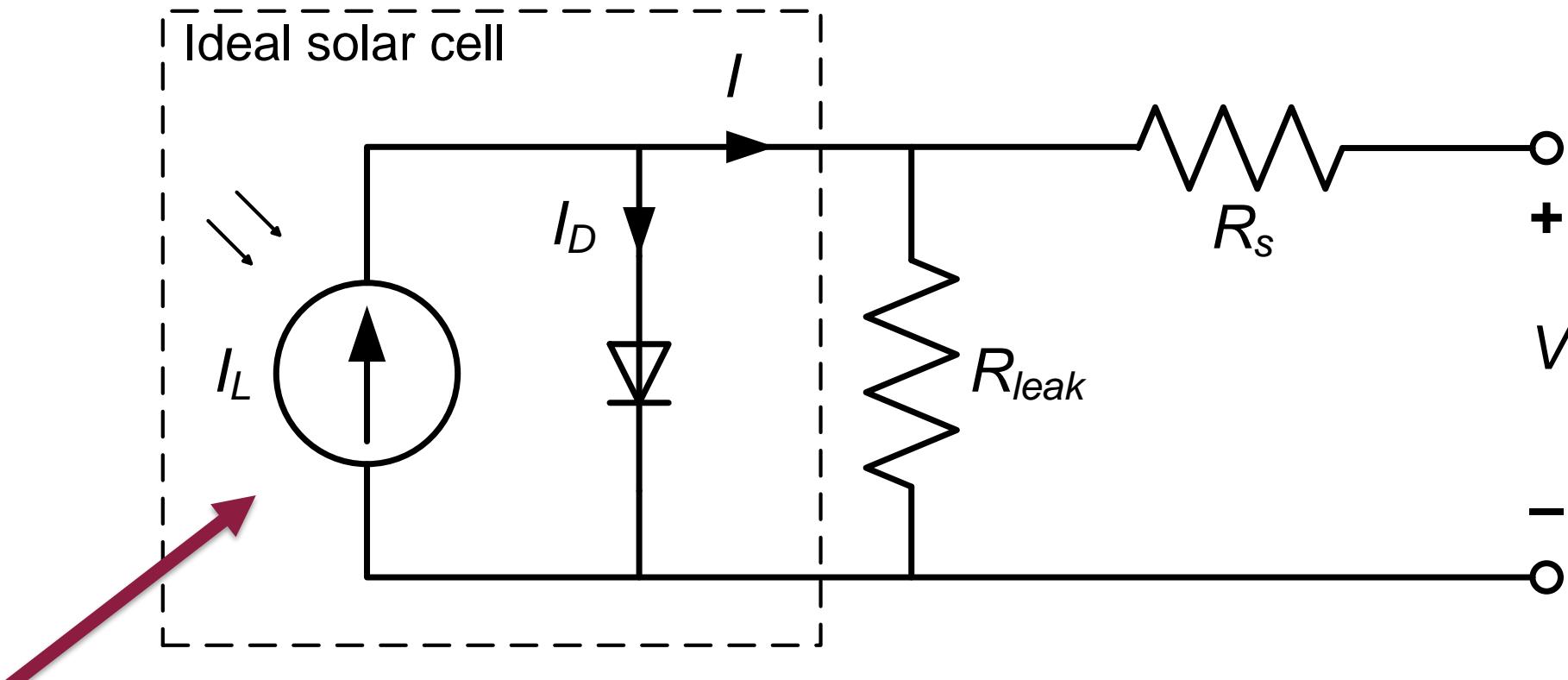
Solar PV Employs the Photoelectric Effect



Solar Cell Model

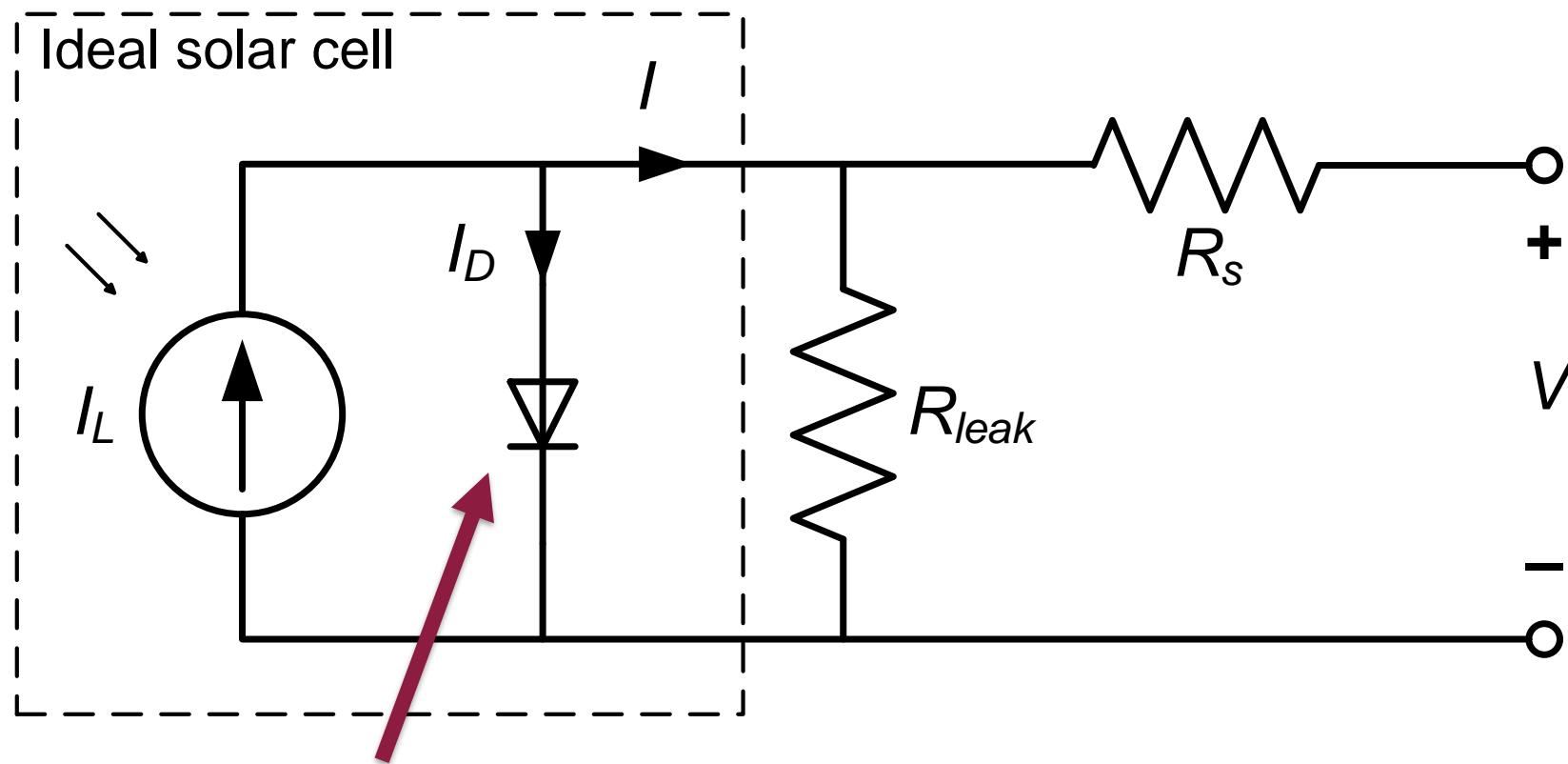


Solar Cell Model



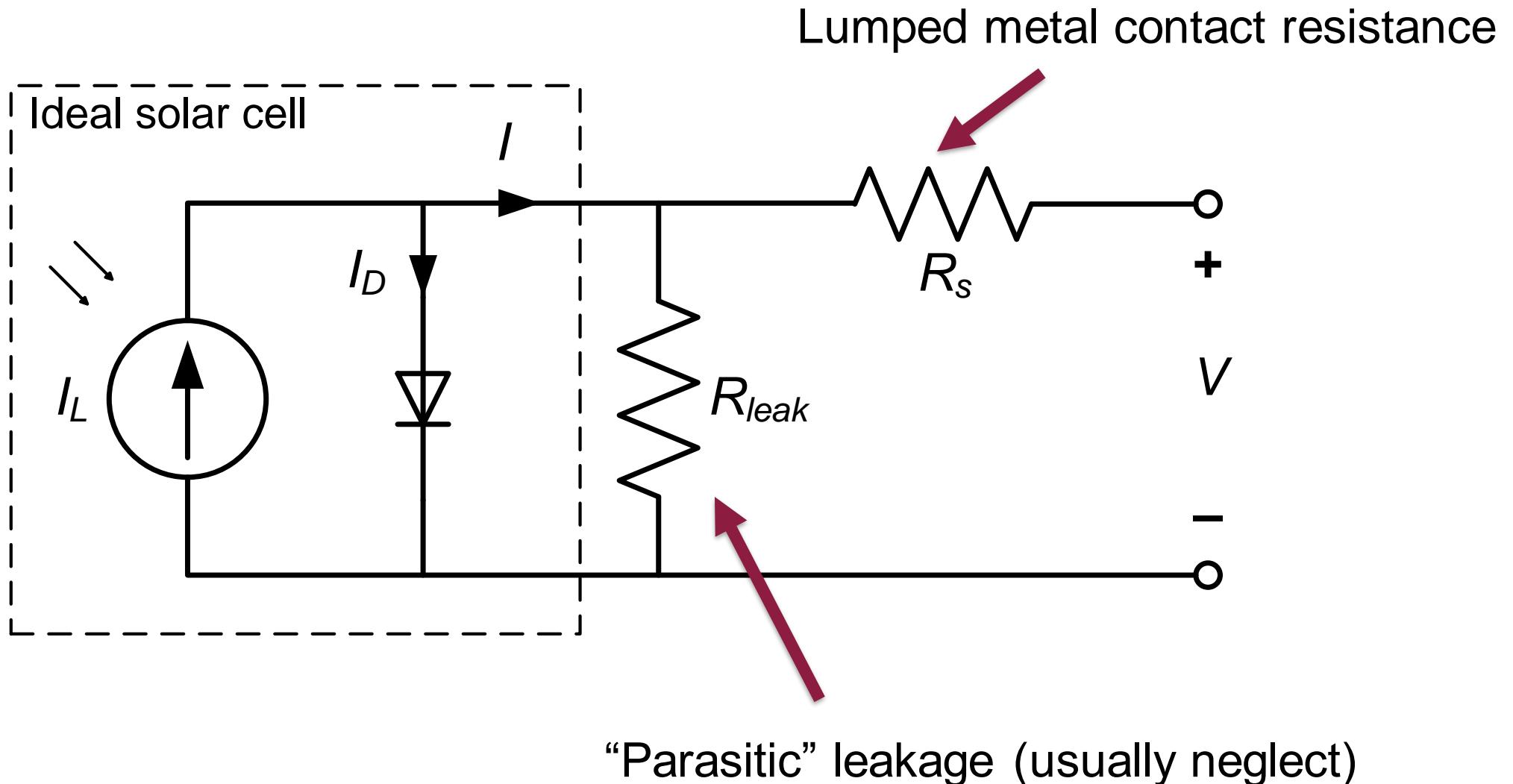
Direct conversion of photons to electricity

Solar Cell Model

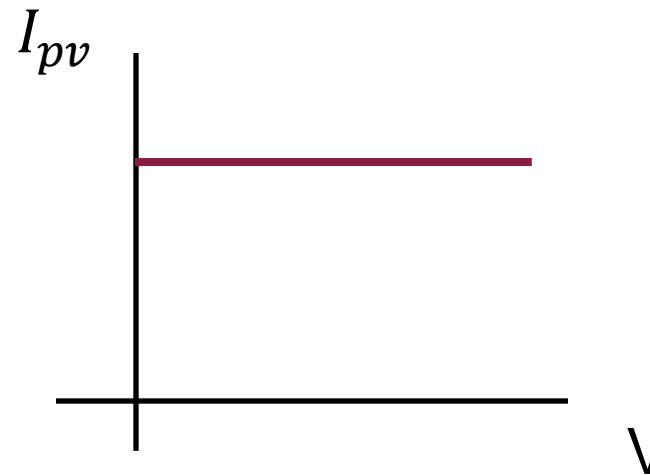
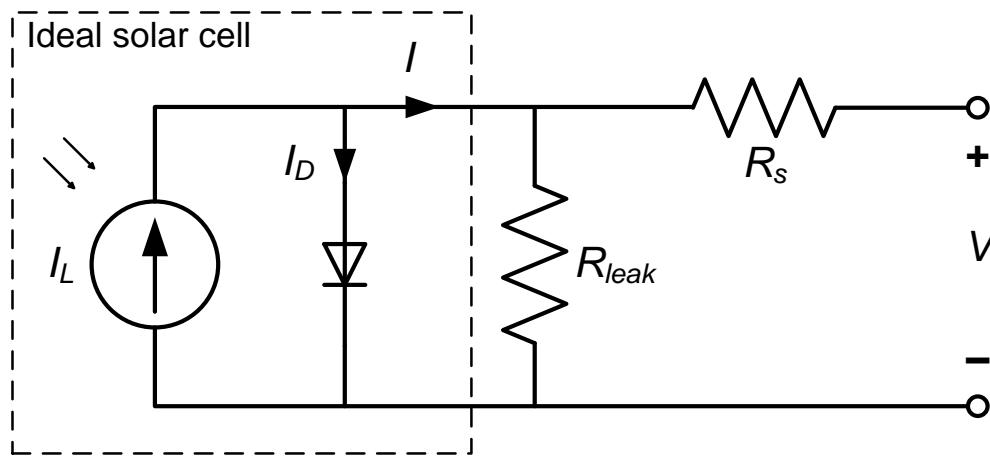


Diode due to pn structure

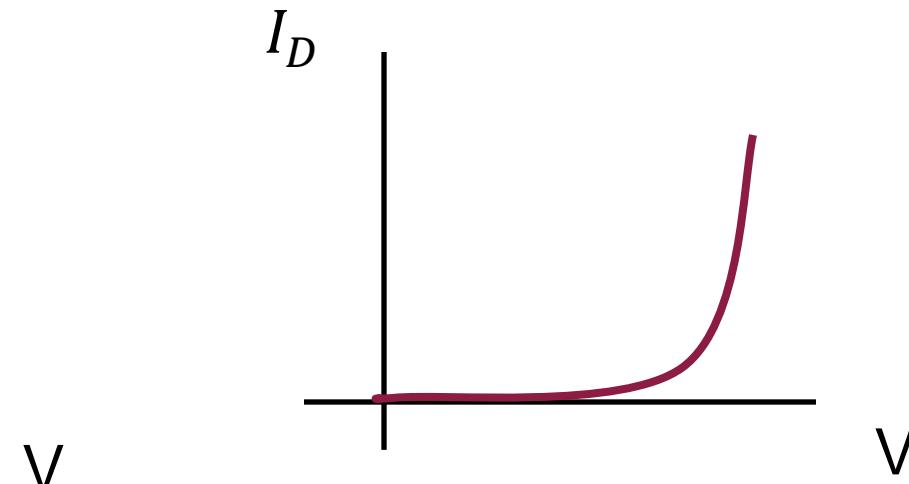
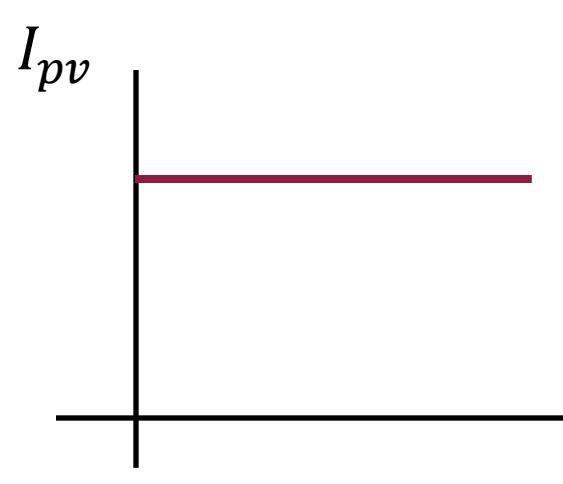
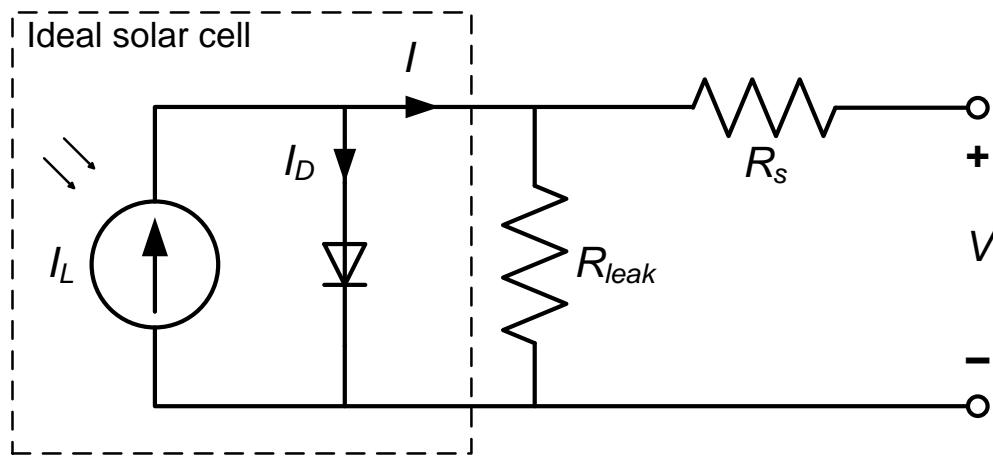
Solar Cell Model



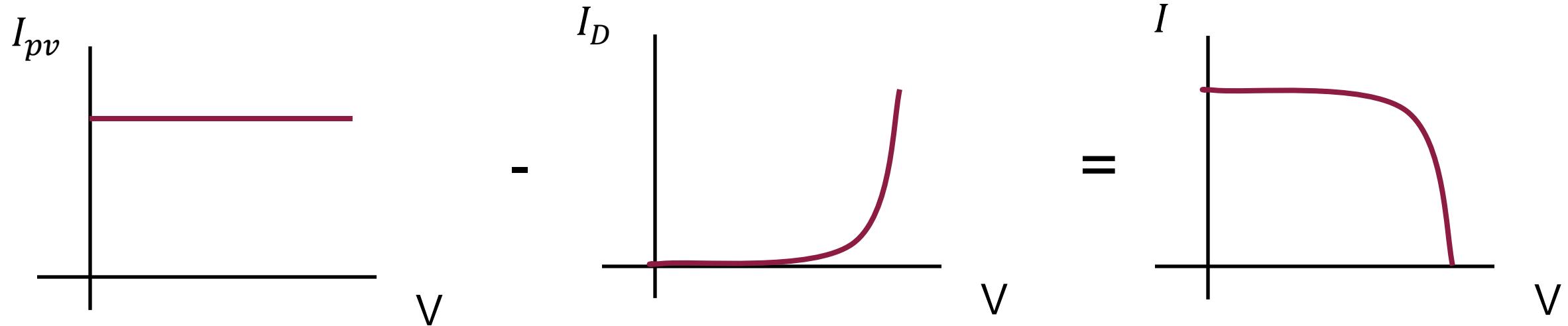
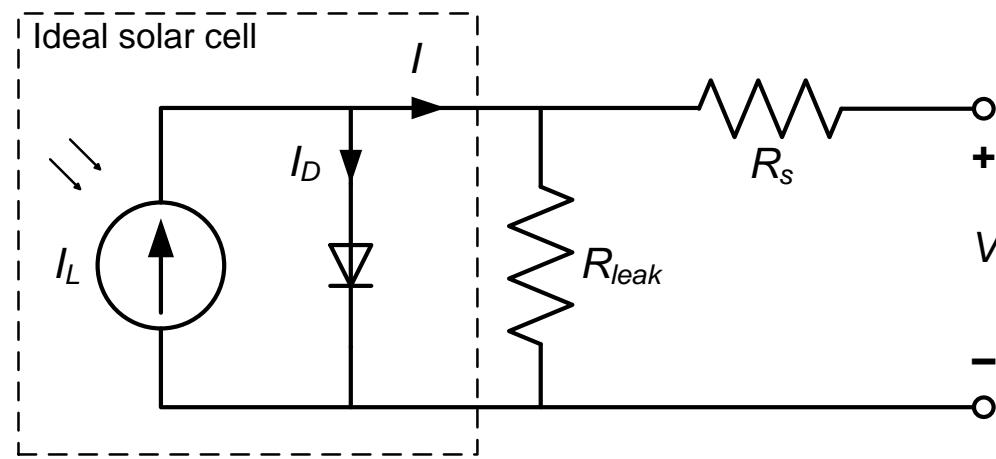
Solar Cell I-V Characteristic



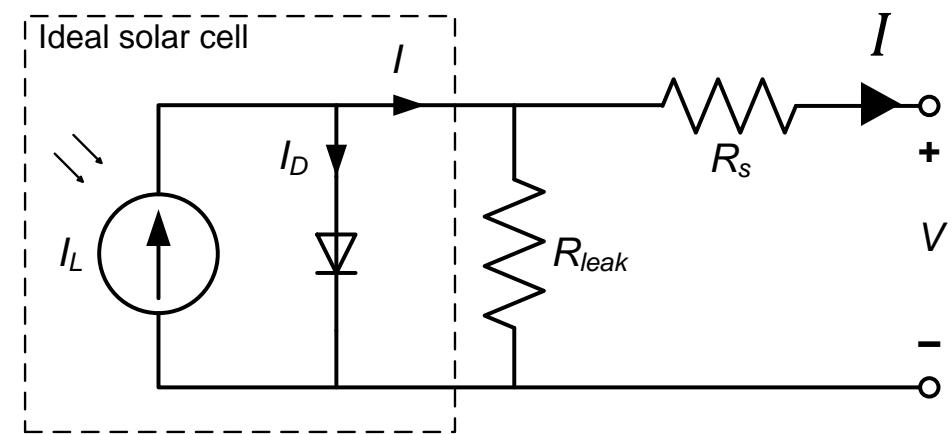
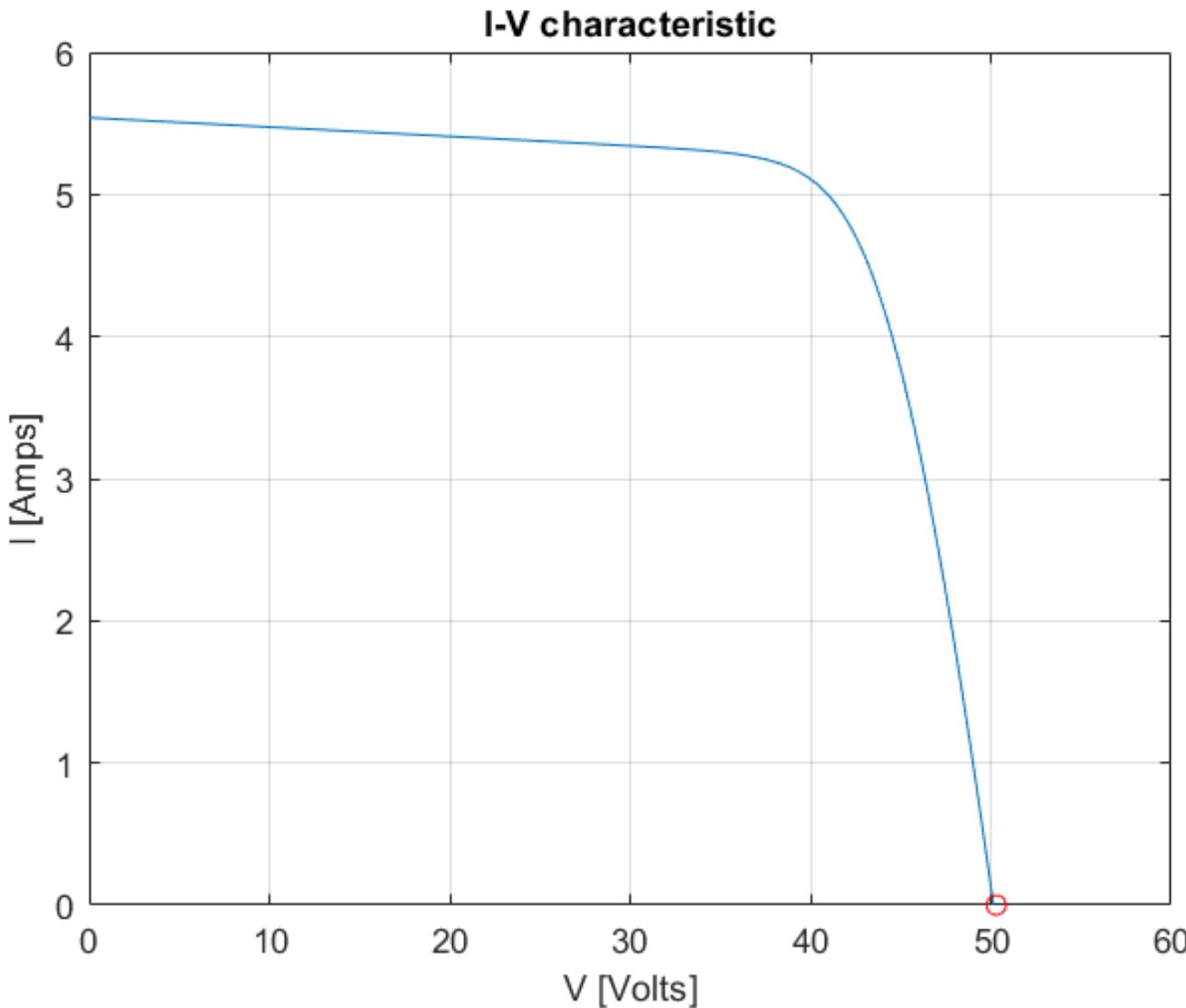
Solar Cell I-V Characteristic



Solar Cell I-V Characteristic

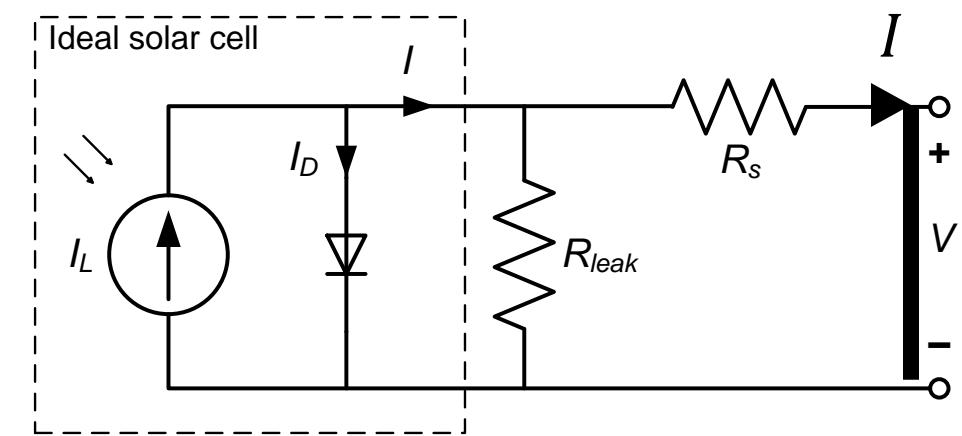
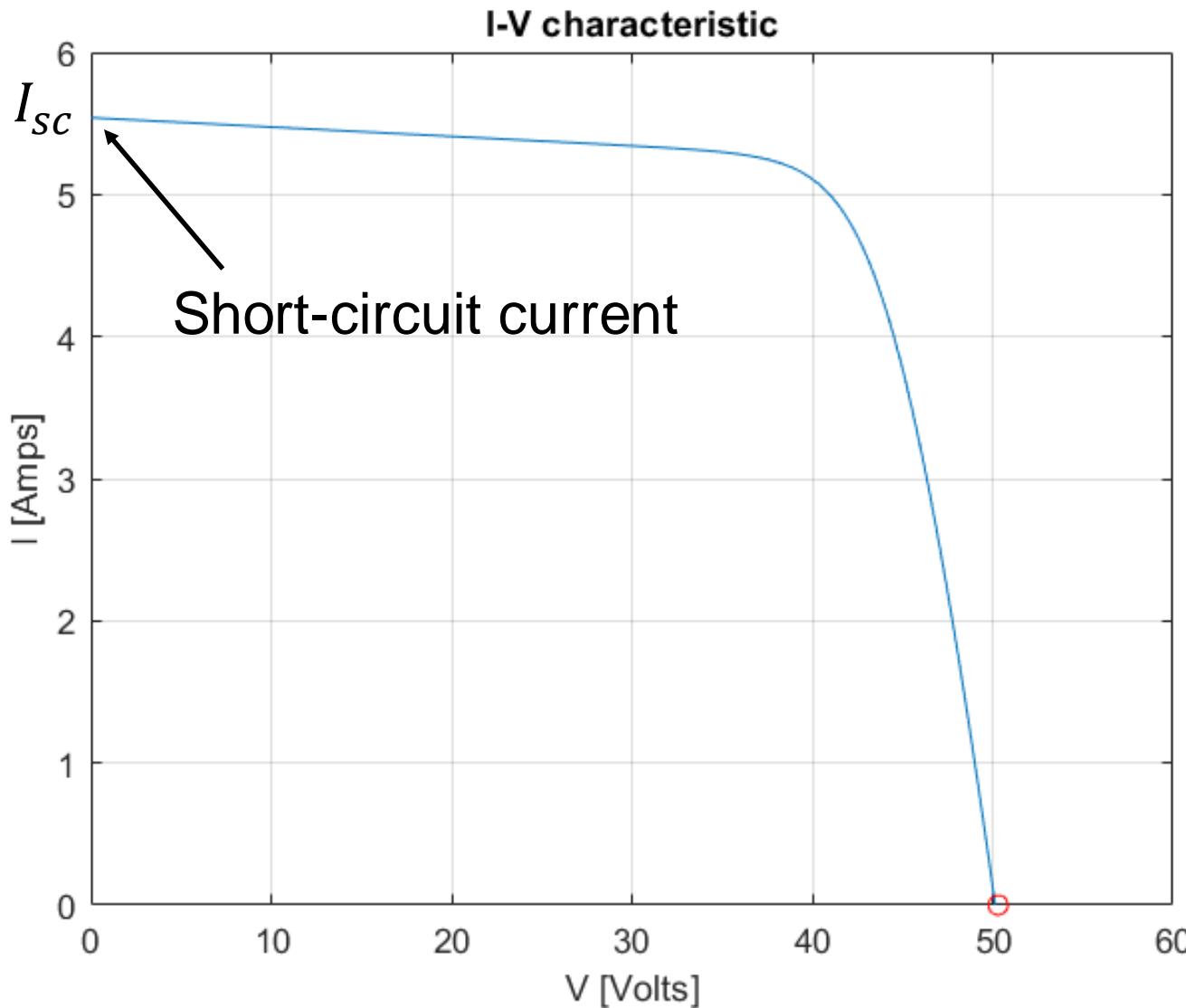


Key IV Curve Parameters



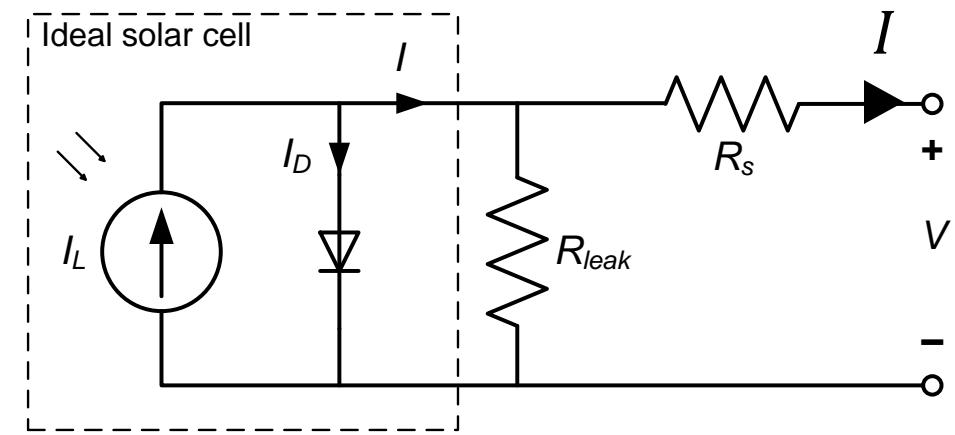
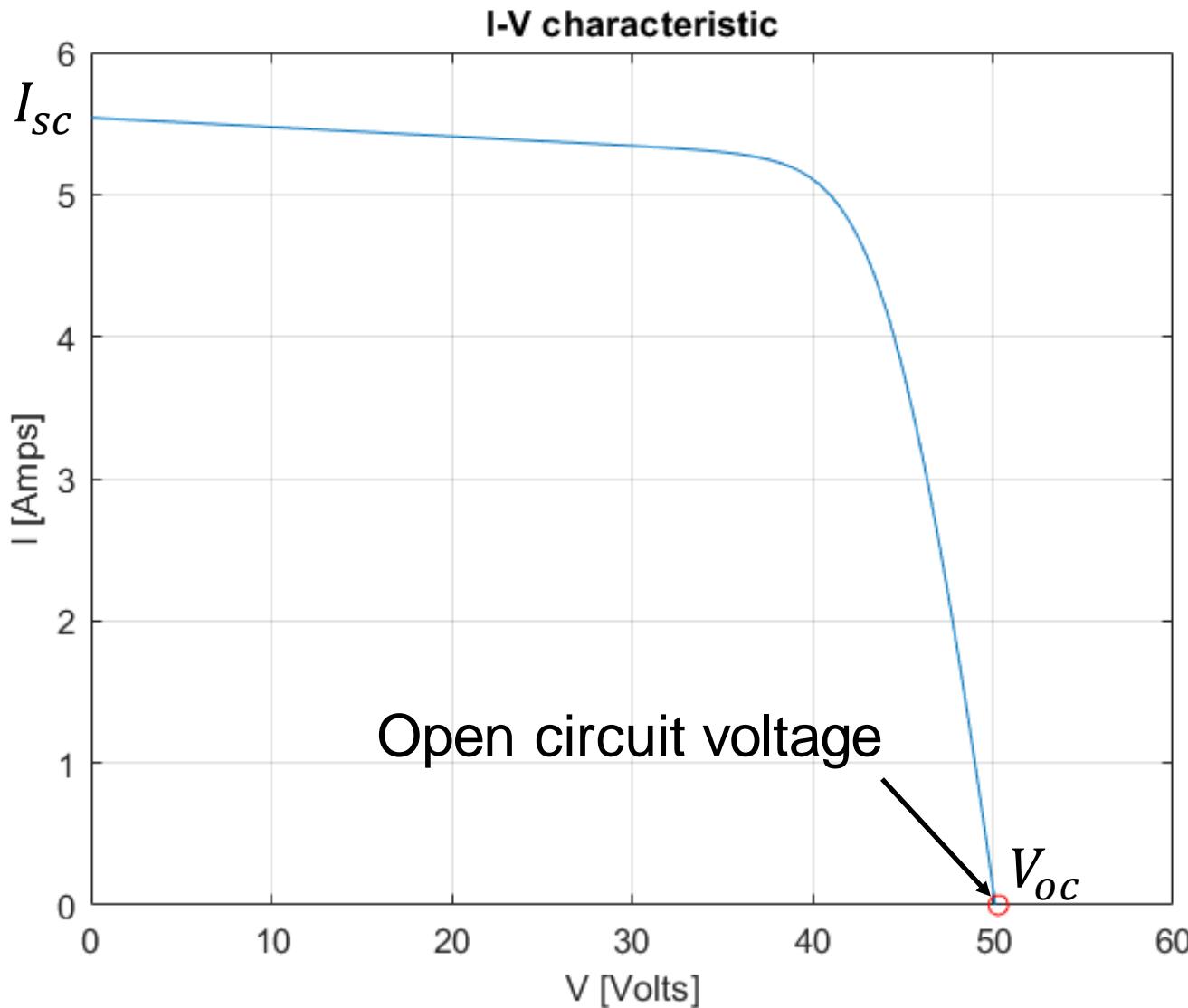
$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

Short-circuit Current



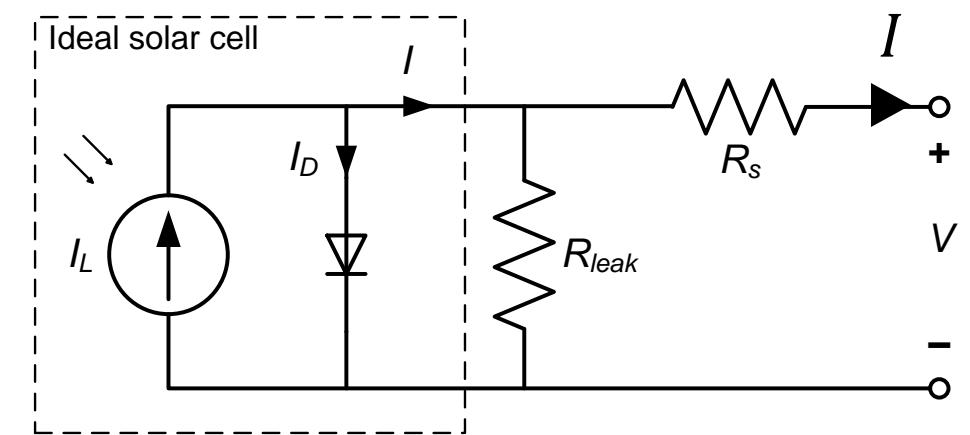
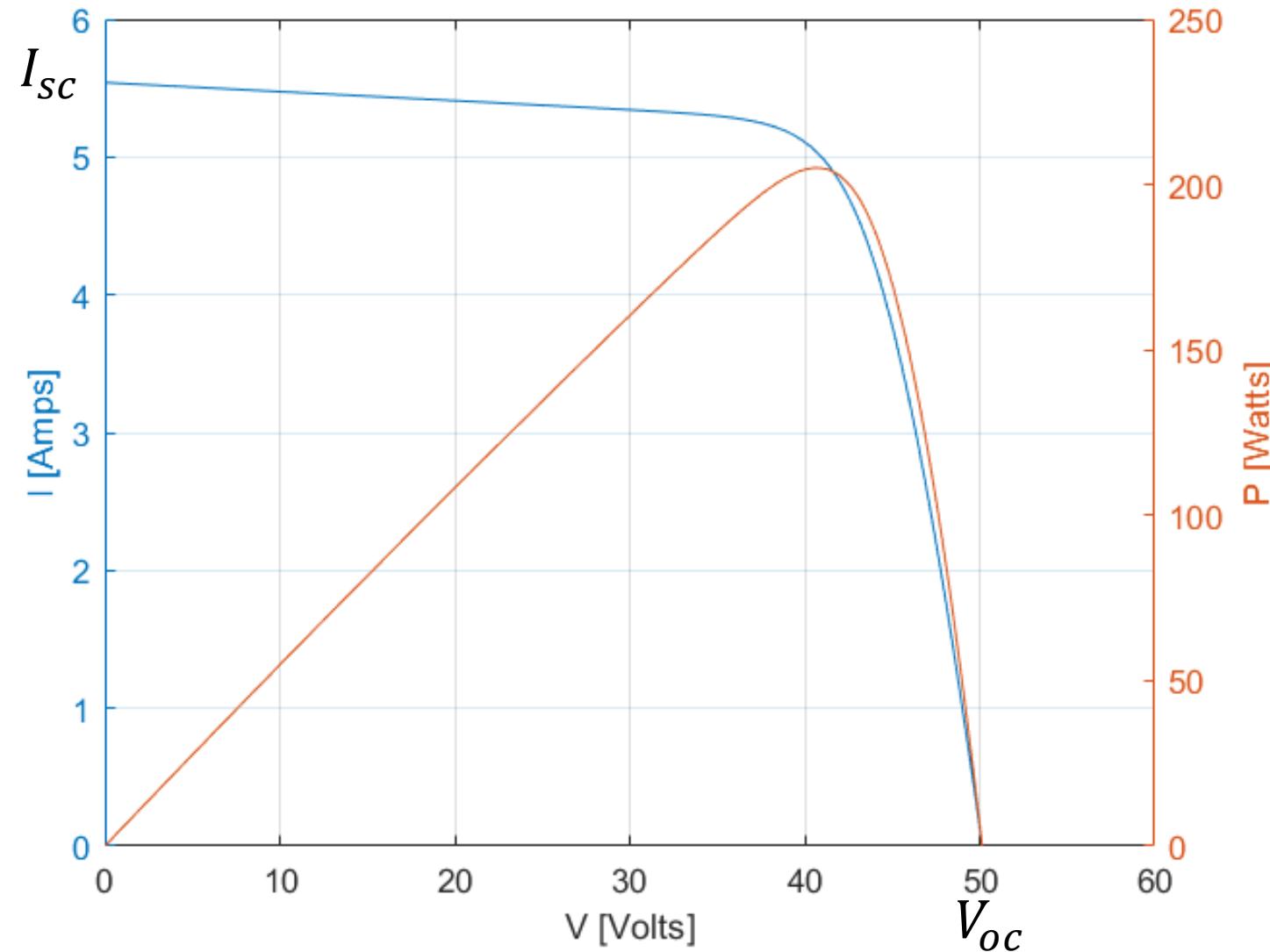
$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

Open Circuit Voltage



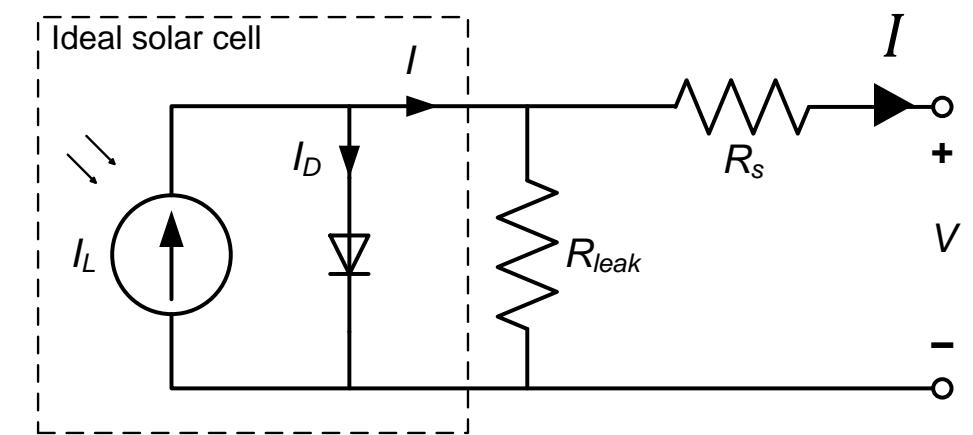
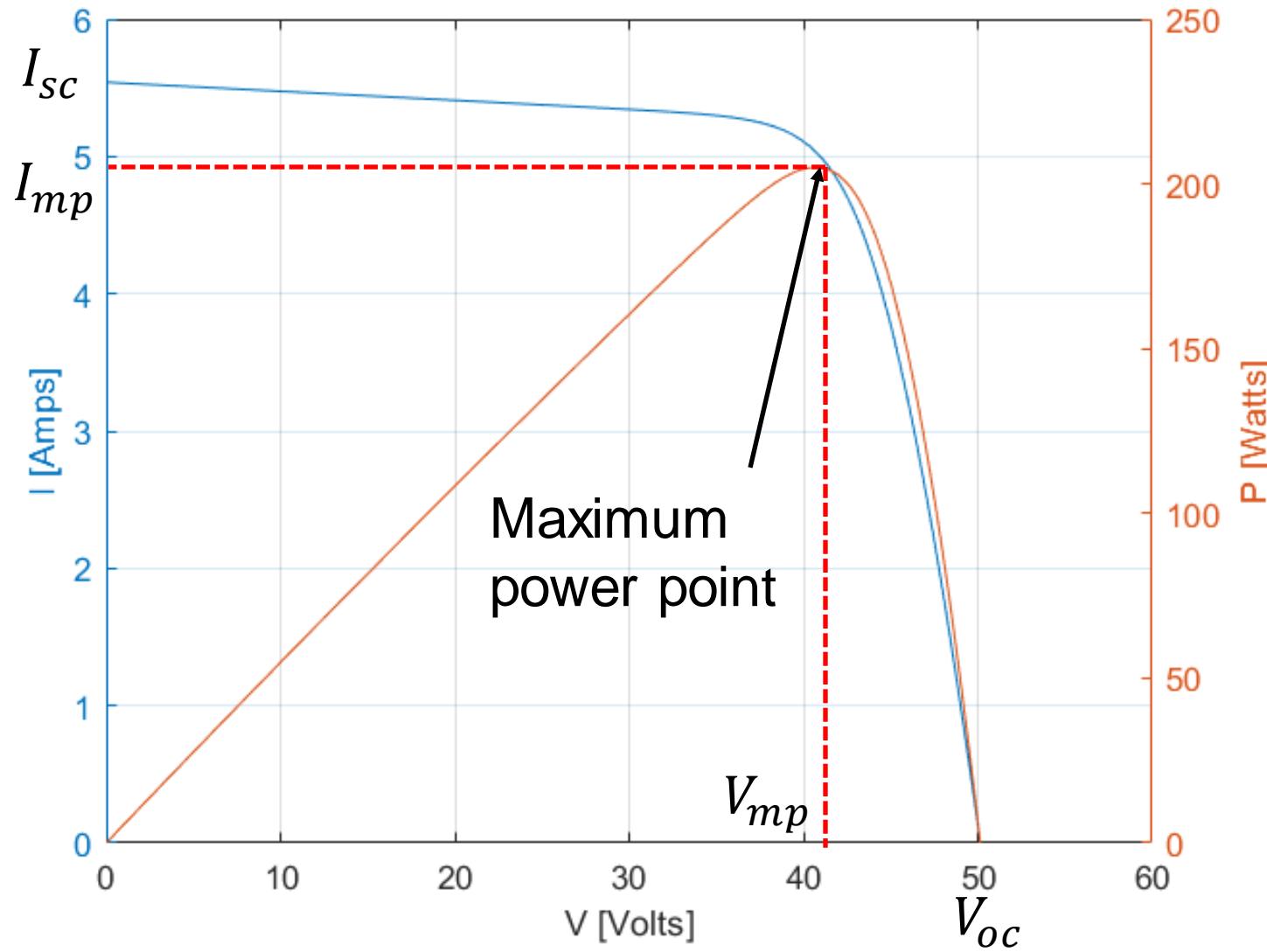
$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

Power Produced by a PV Cell



$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

Maximum Power Point



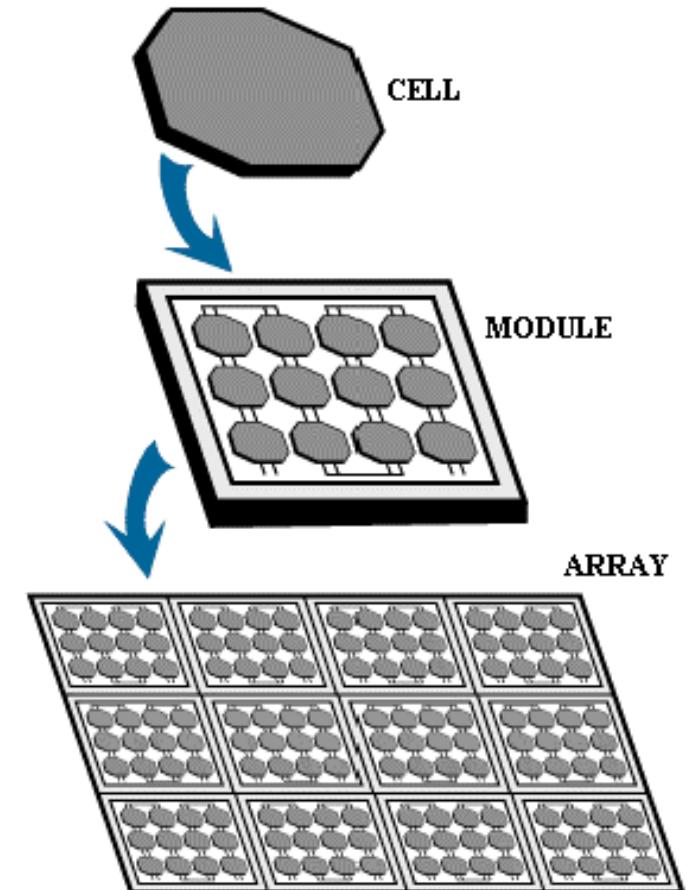
$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

Typical Silicon PV Cell Characteristics

- Open circuit voltage V_{oc} : 0.55 – 0.76V (@ 25°C)
- Max power voltage V_{MP} : 0.45-0.58V
- Short-circuit current I_{sc}
 - 4x4": 3 – 3.8 A
 - 5x5": 4.6 – 6 A
 - 6x6": 6.8 – 8.5 A
 - 8x8": 13 – 15 A
- Typical efficiency: ~15-20%
- Maximum theoretical efficiency: ~32%

Cells, Modules, Arrays

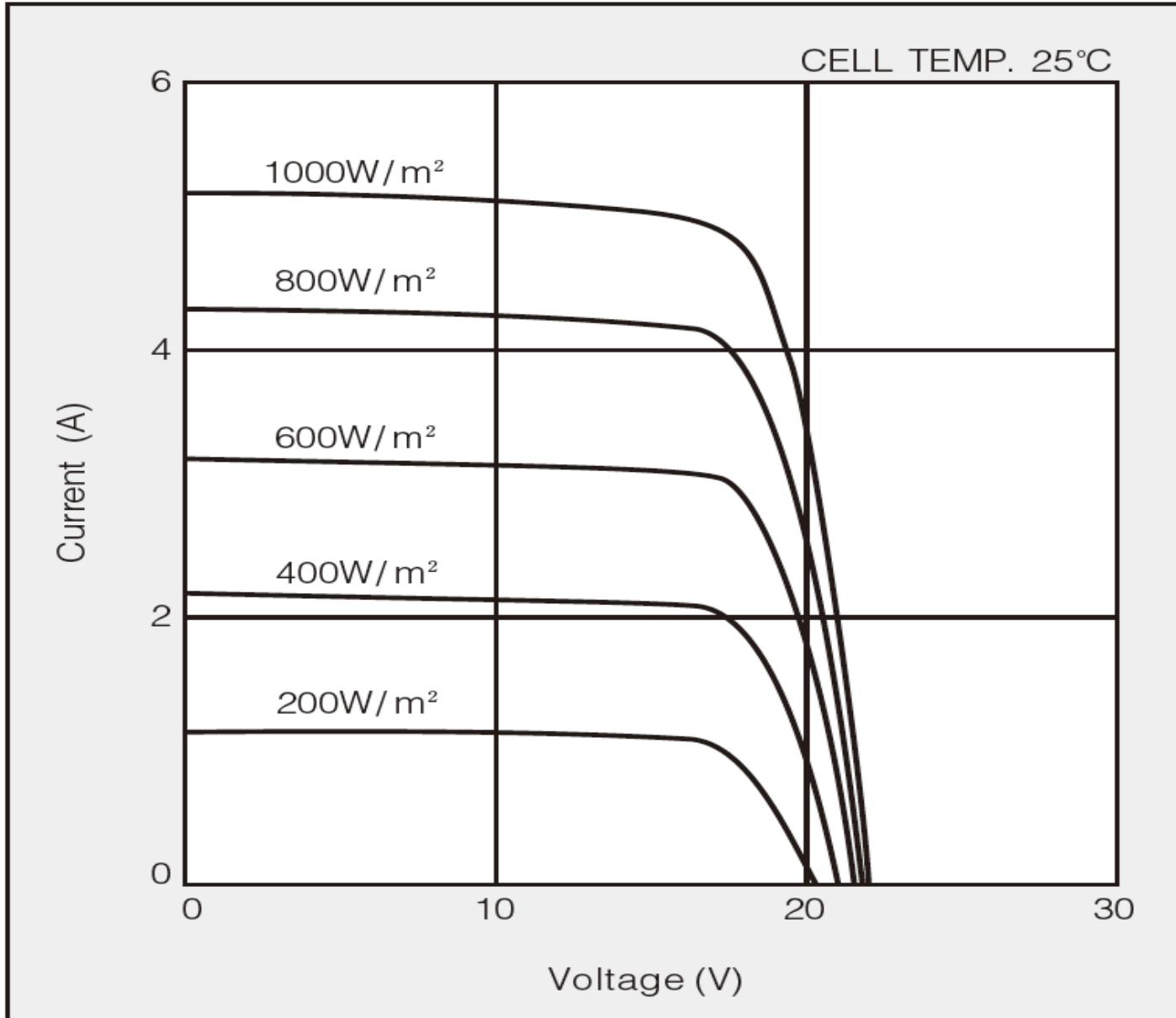
- Typically connect many cells in series to increase operating voltage



- Then connect modules in parallel/series for desired overall IV characteristic

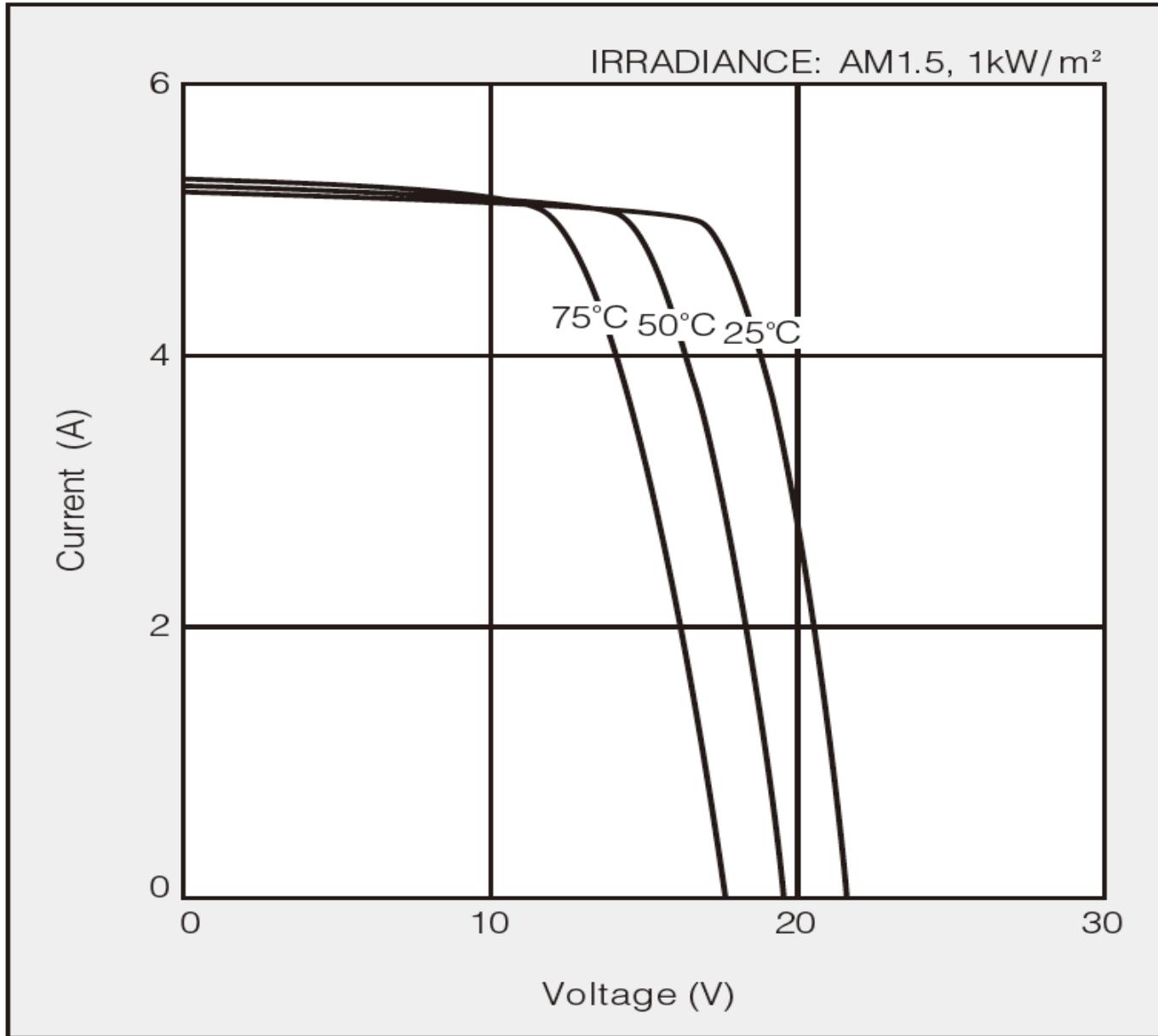
[This Photo](#) by Unknown Author is licensed under
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Solar Panel I-V Characteristic with Irradiance



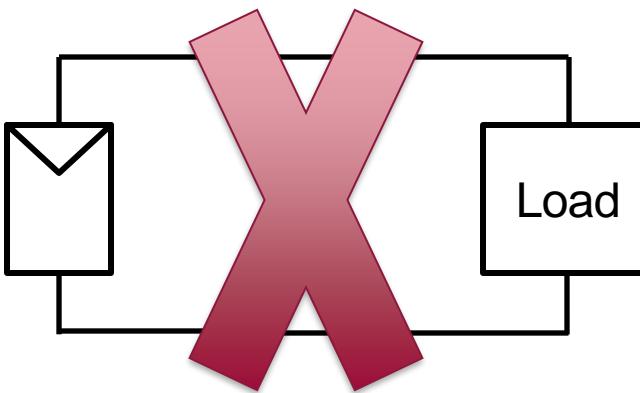
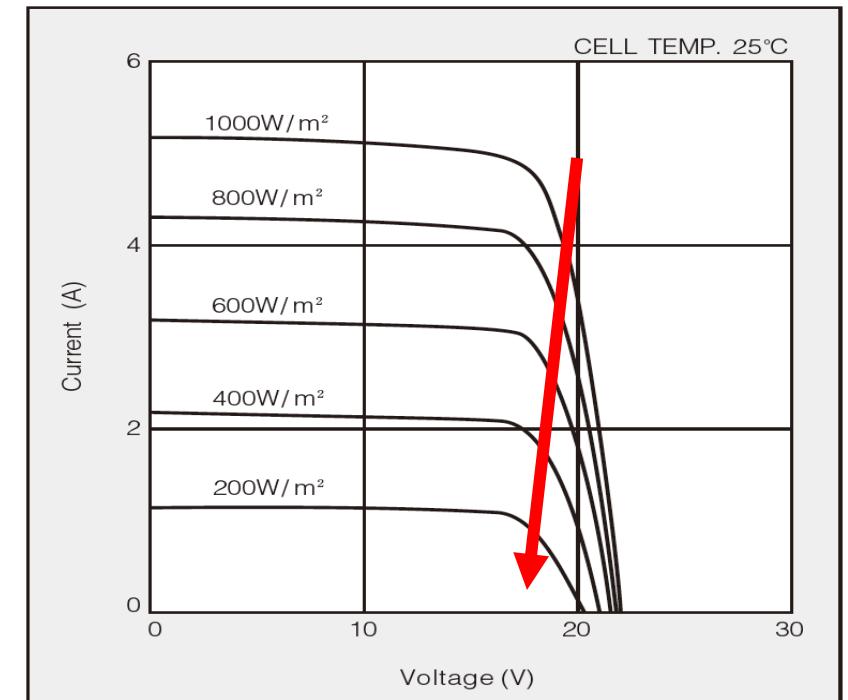
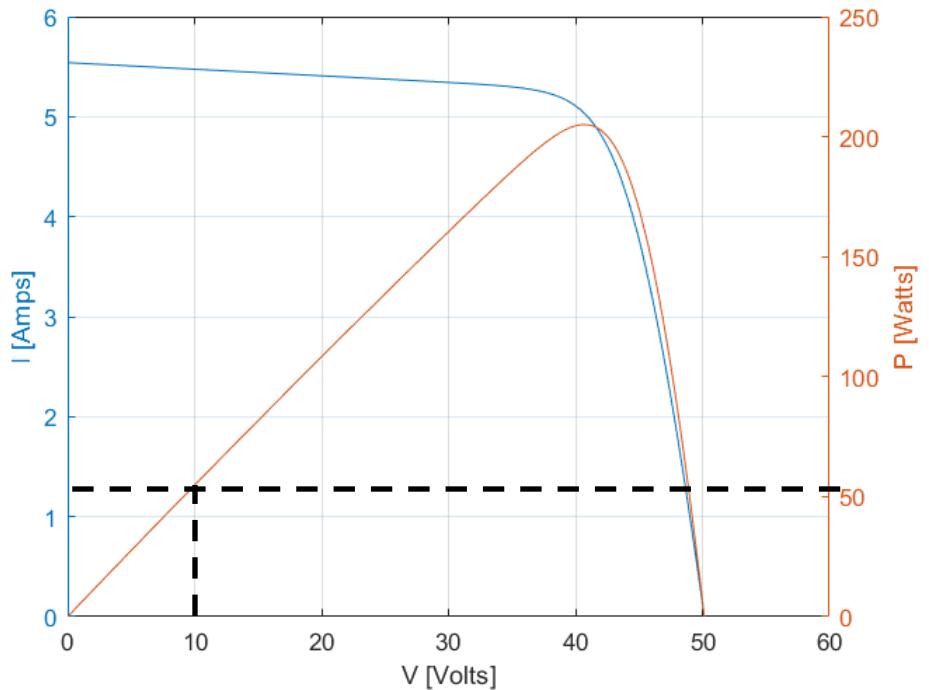
$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

Solar Panel I-V Characteristic w/ Temperature

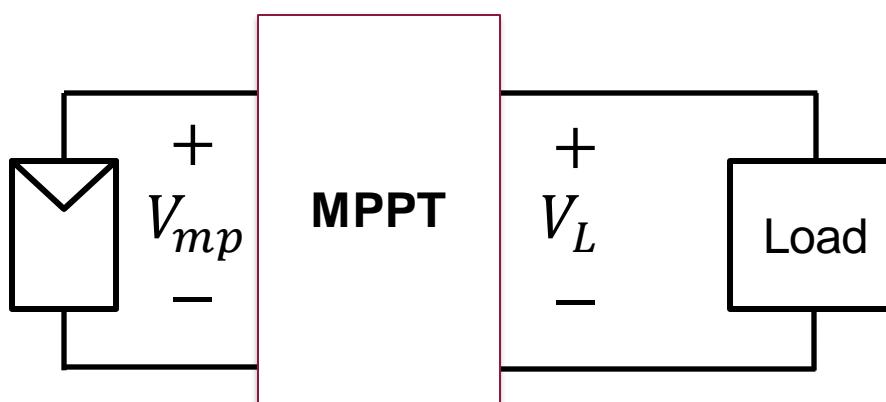
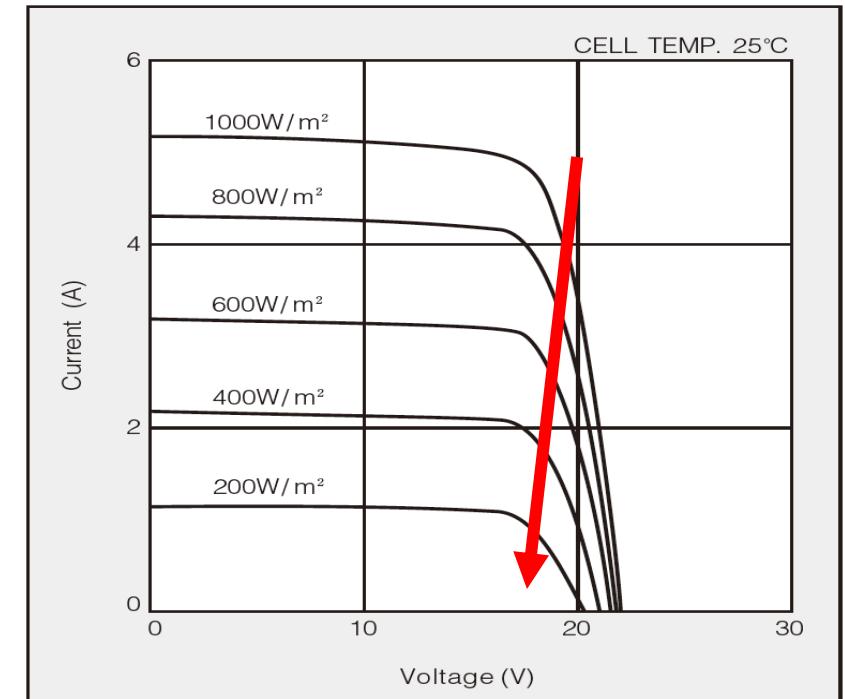
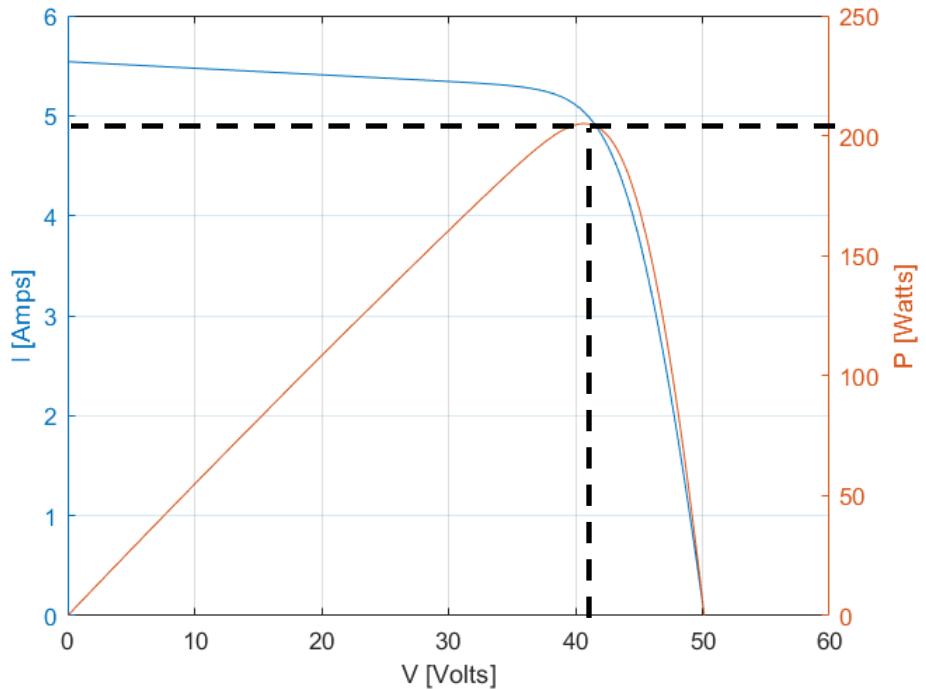


$$I = I_{pv} - I_0 \left[\exp\left(\frac{V}{V_t a}\right) - 1 \right]$$

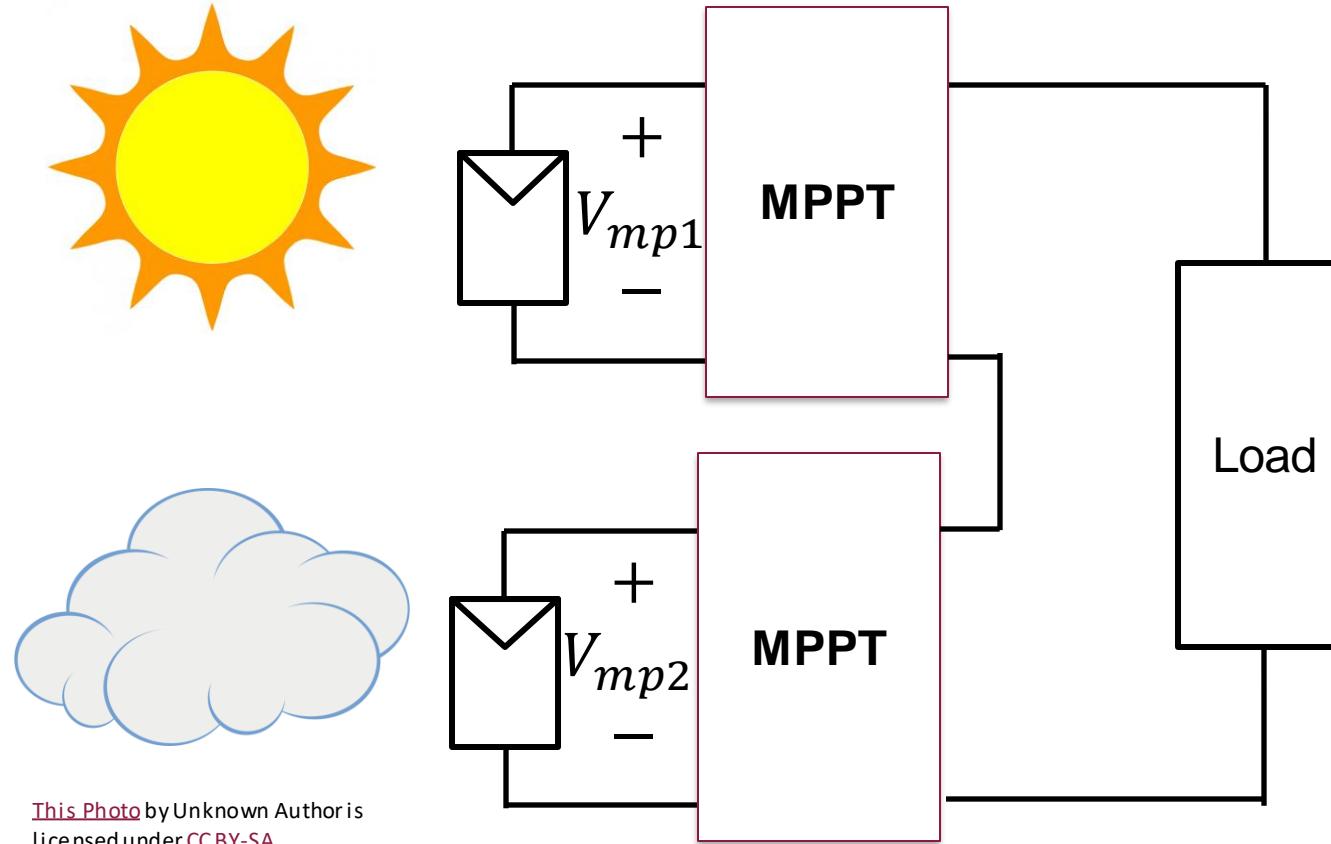
Direct Load Connection is Poor



Need a “Smart Block” to Track MPP



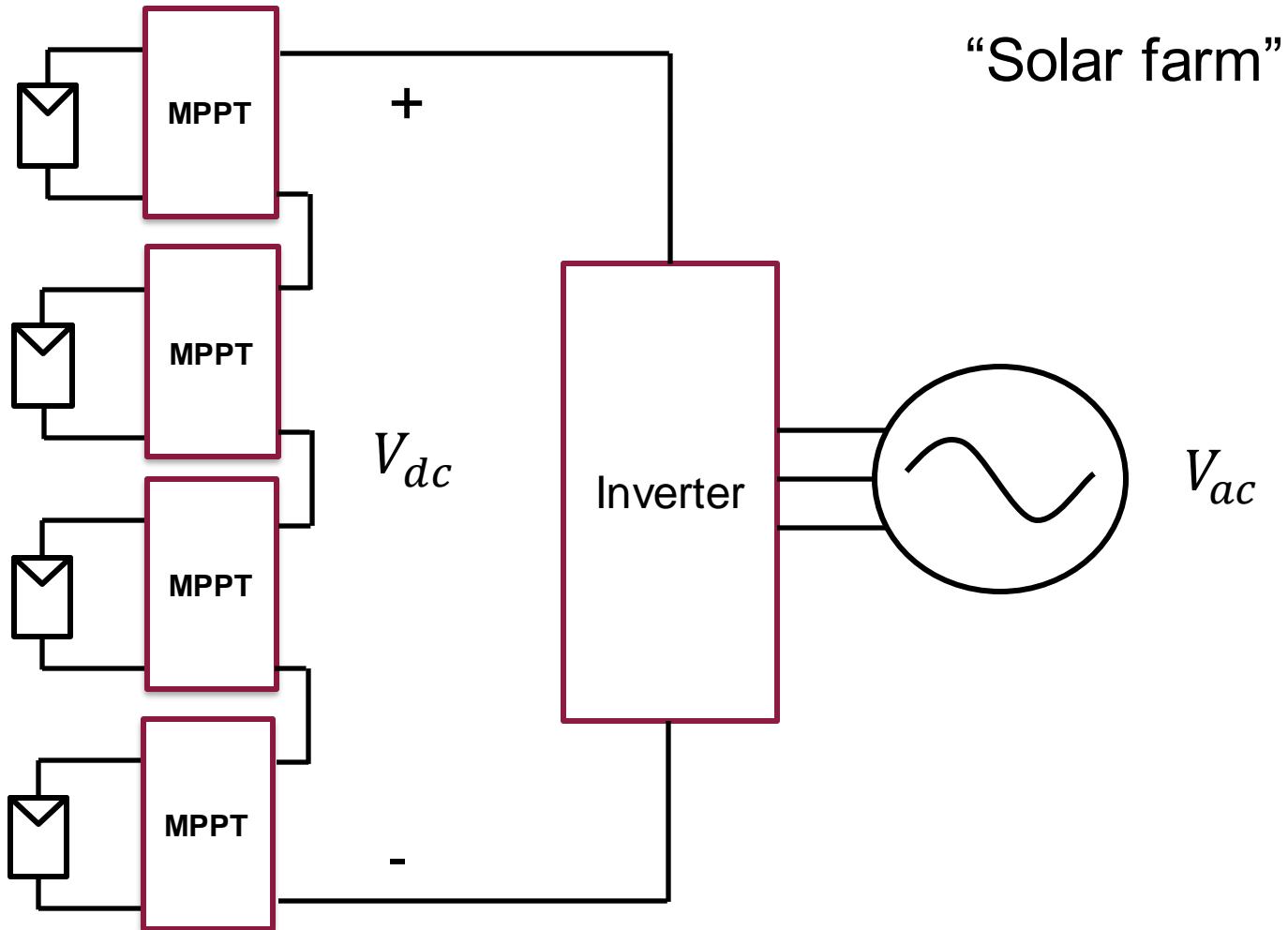
Distributed MPPT Common to Accommodate Different Weather



Inverter Converts dc to ac

These blocks are implemented via power electronics

No rotating masses,
no inertia



Conclusions

- Solar PV cells convert sunlight to electrical energy
- Characterized by short-circuit current, open-circuit voltage, and maximum power point
- Highly variable output, MPPT must be employed
- Output is dc, must be converted to ac for grid connection
- No rotating masses, so no contribution to system inertia

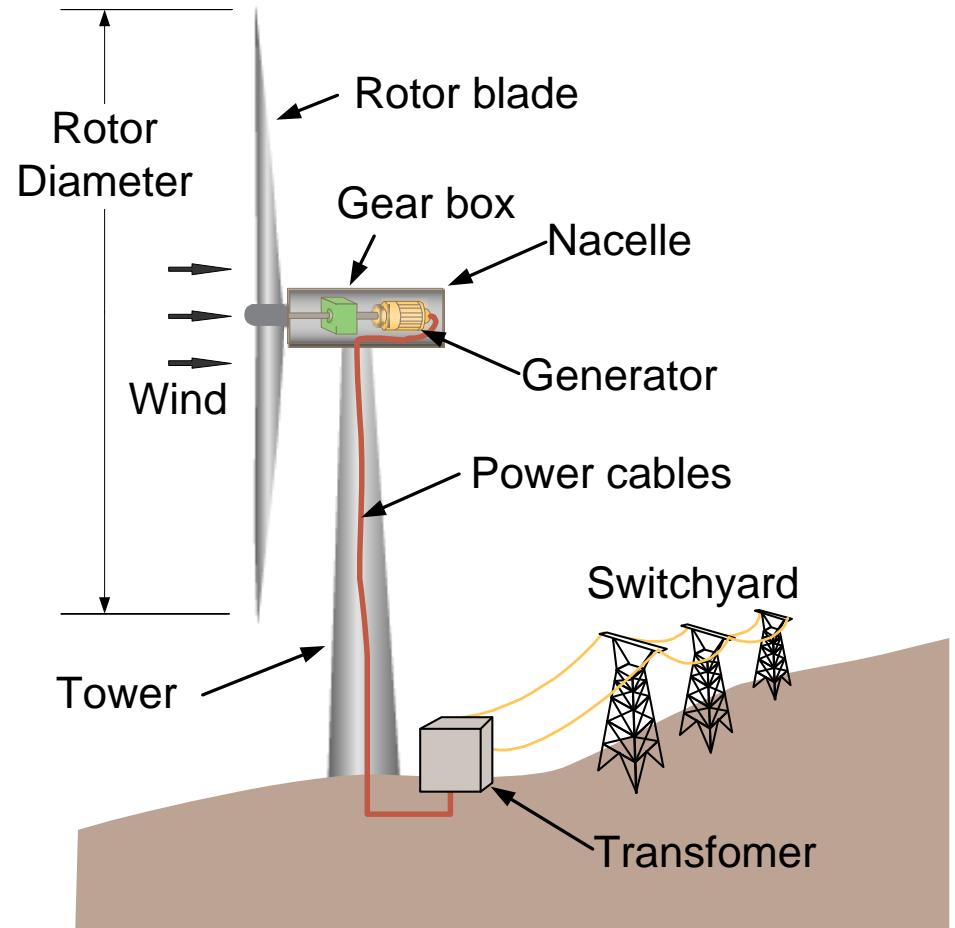
Module 2b

Wind Energy

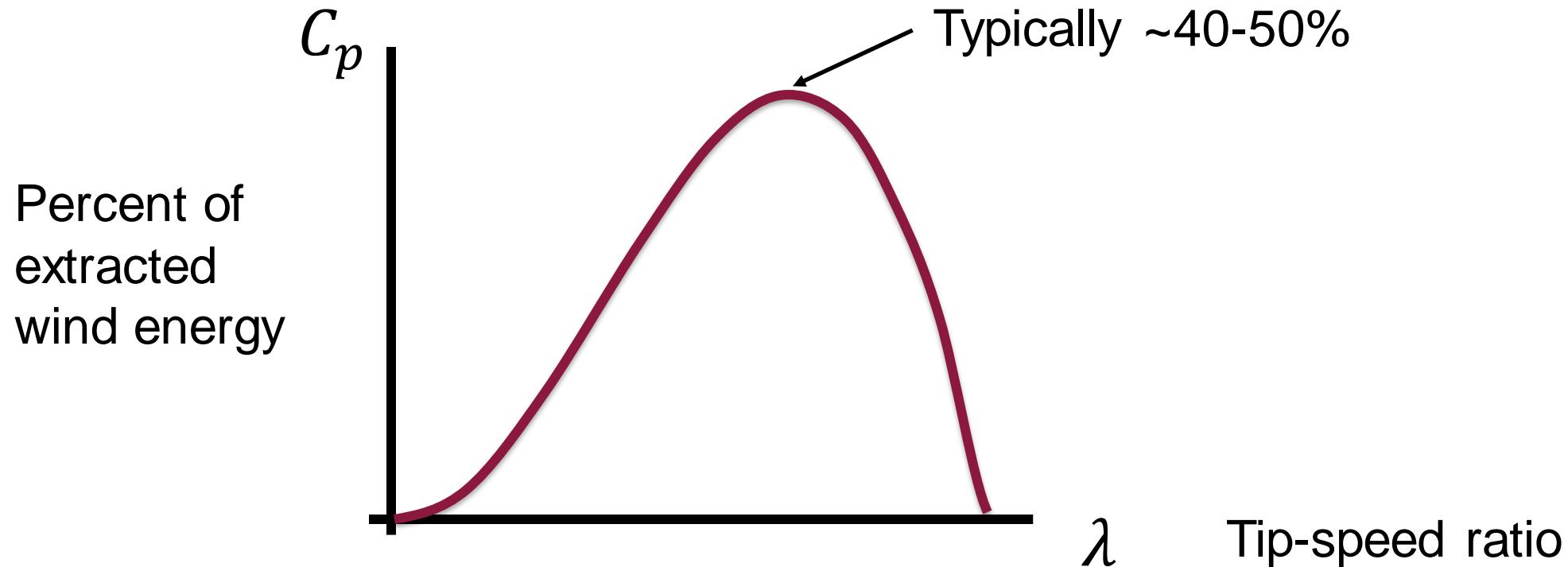
How does it work and how do we connect it to the power system?

Extract Kinetic Energy of Wind

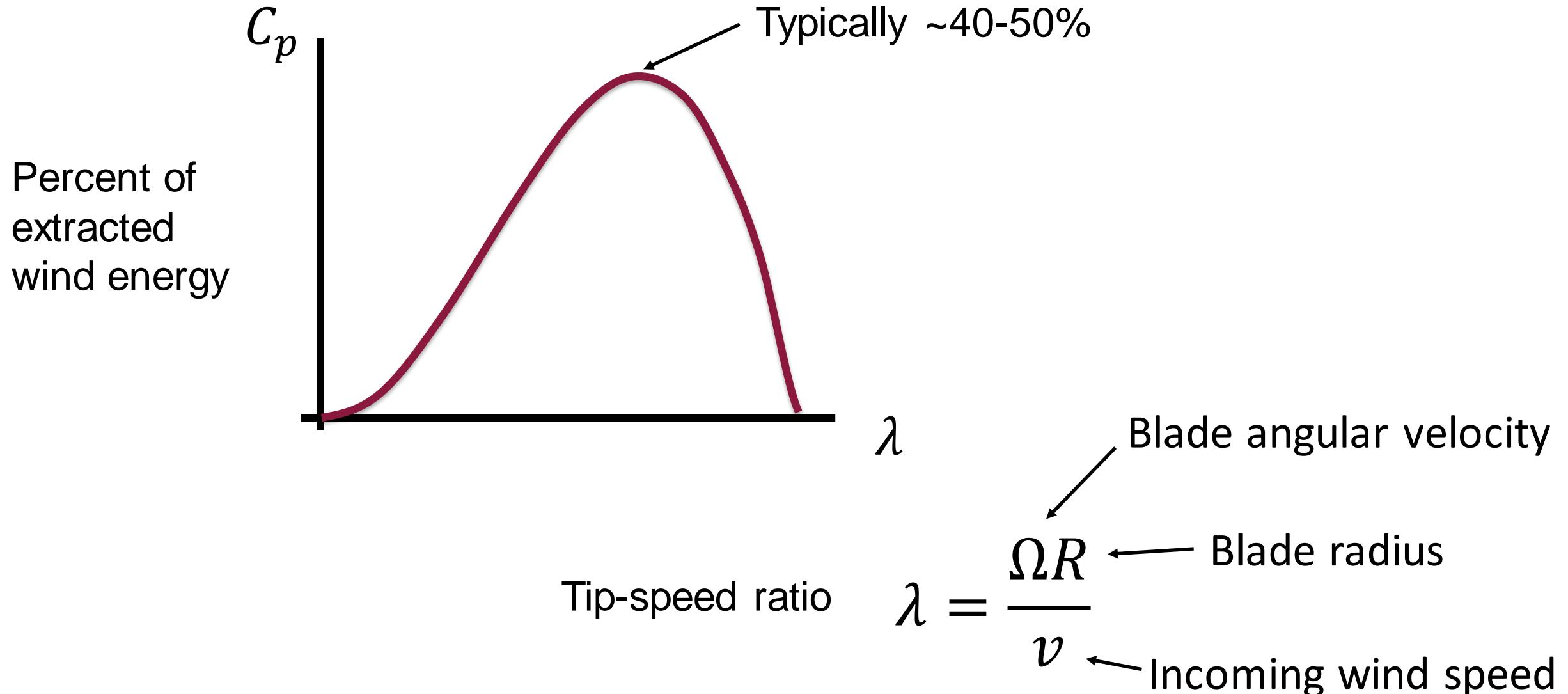
- Instead of hot high pressure gas in turbine, free flowing wind lifts blades, spins shaft
- ac machine converts motion to electricity



Turbine Performance Coefficient

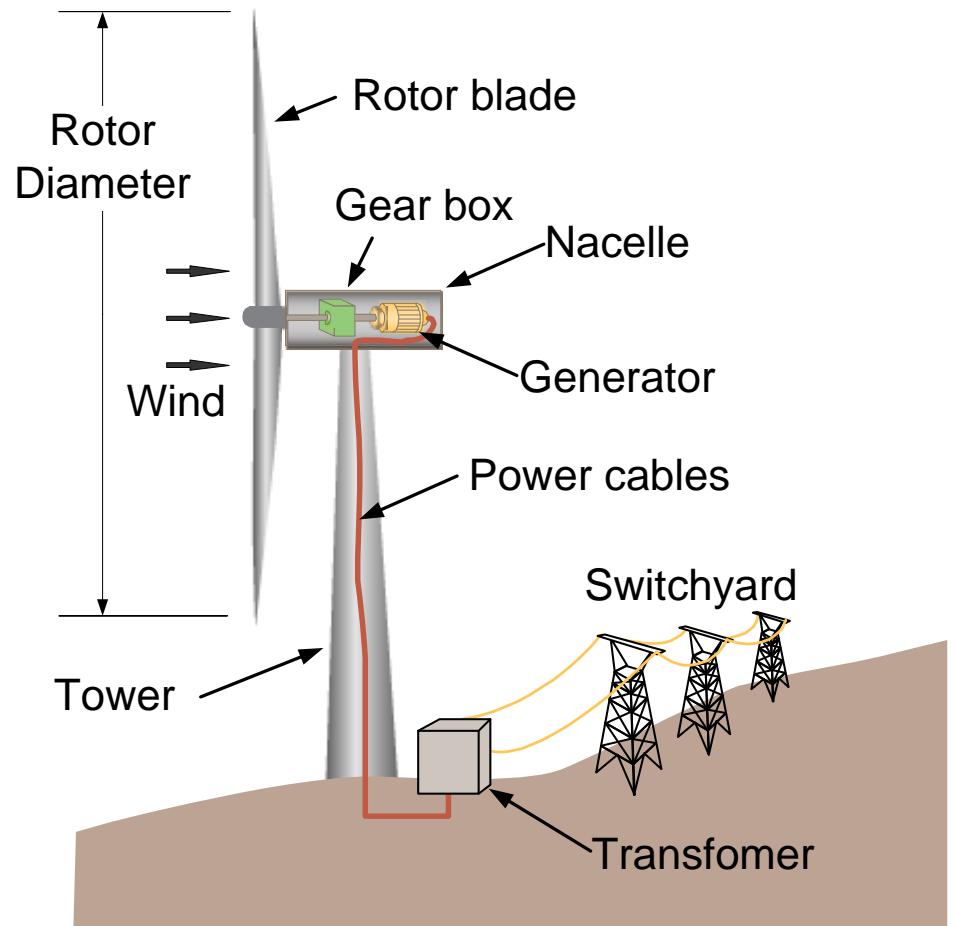


Turbine Performance Coefficient

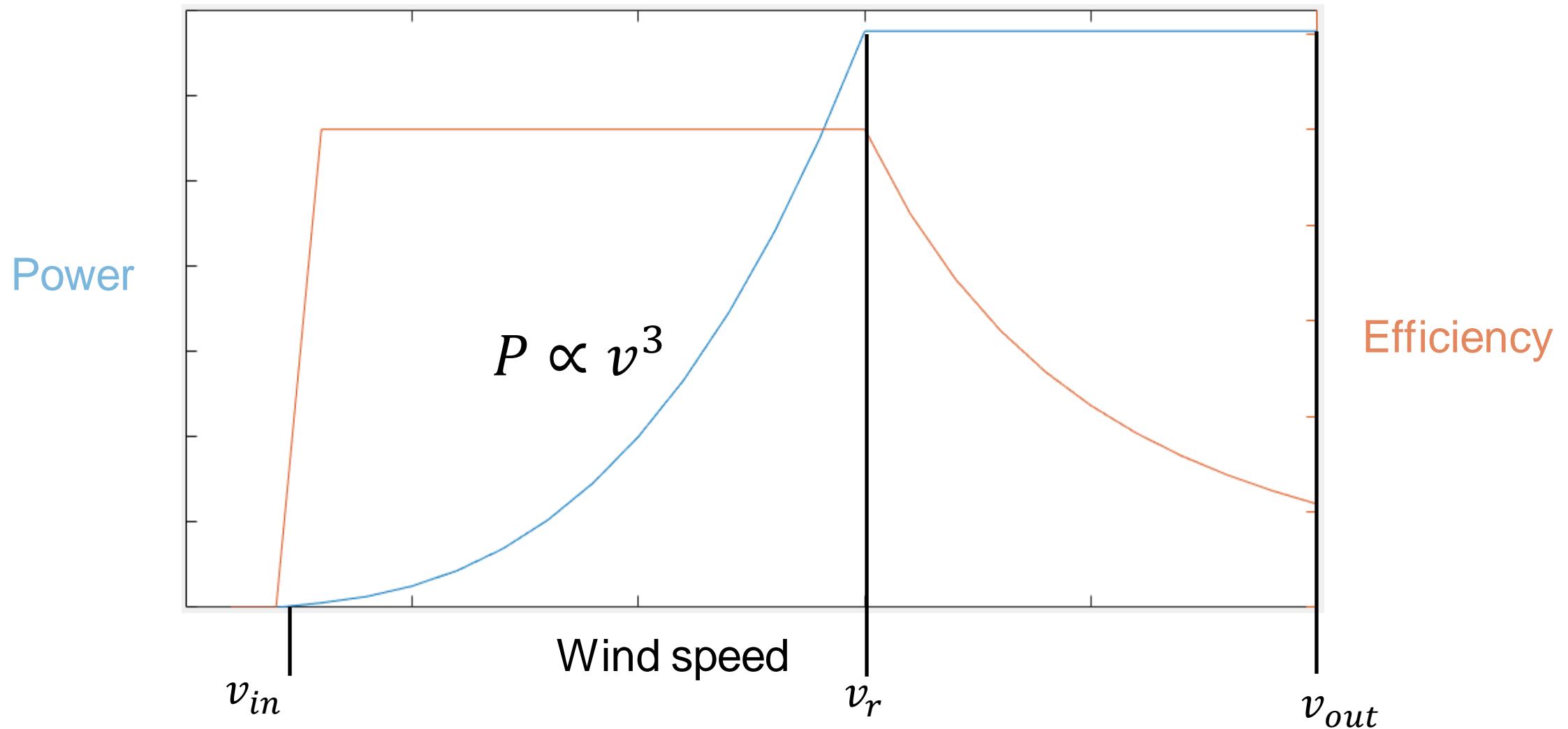


Fixed-Speed Wind Turbines (Type 1 and 2)

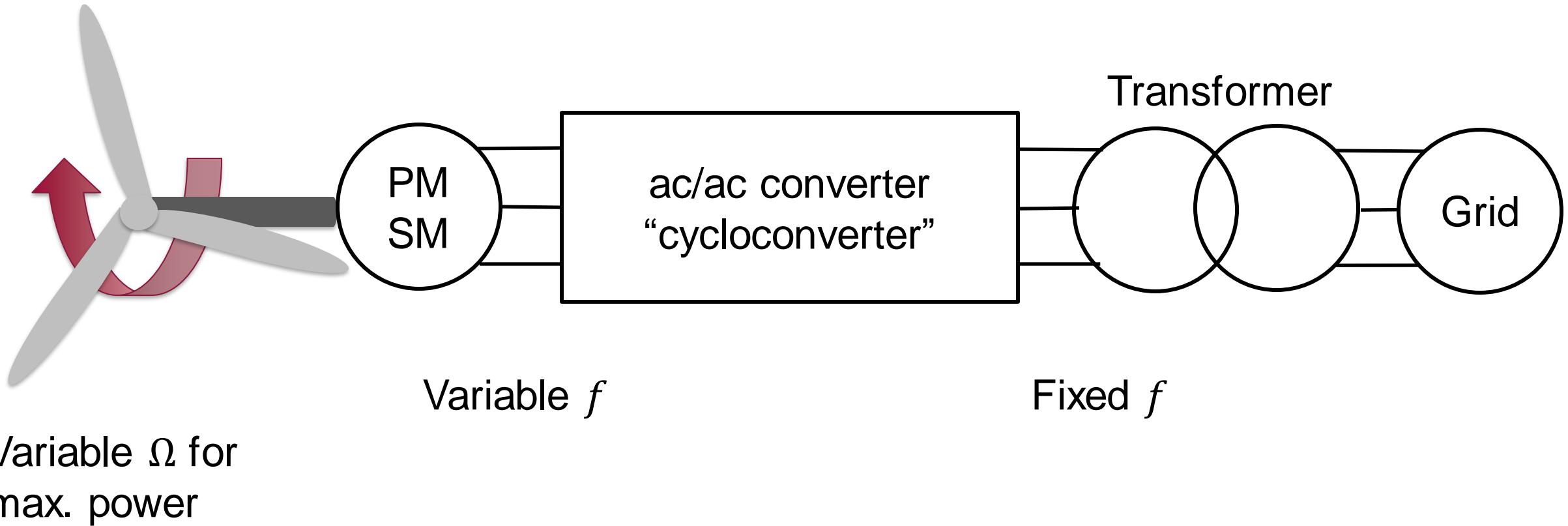
- Induction generator
- Direct power system connection
- Fixed speed (set by grid)
- Historically popular
- Only extract max. power at one wind speed
- Type 2: additional rotor resistors for improved gusting response
- Contribute inertia



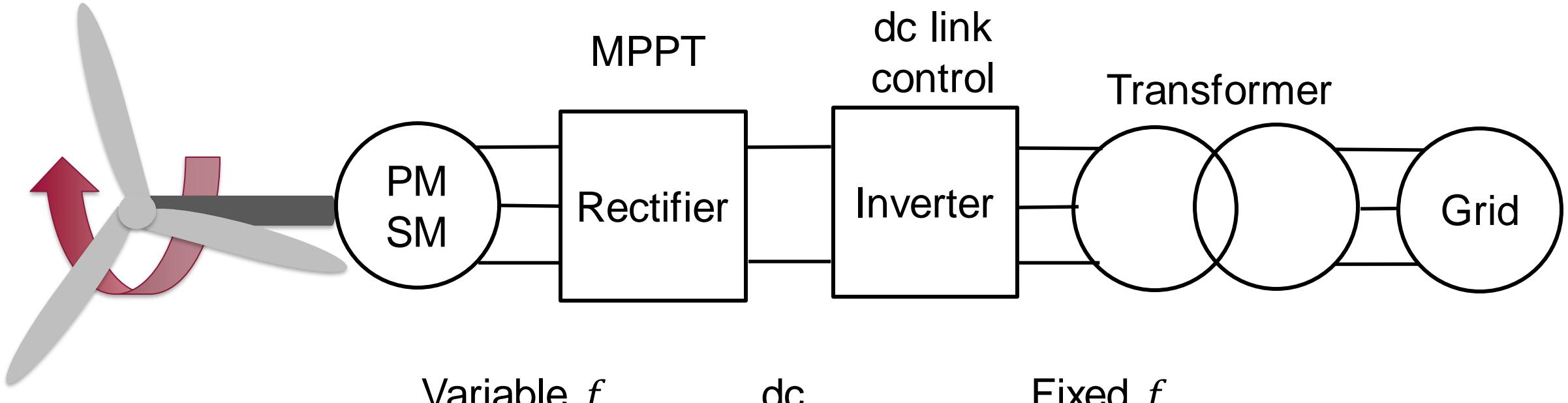
Ideal Variable Speed Power Characteristic



Variable Speed Turbine (Type 4)



Variable Speed Turbine (Type 4)



Variable Ω for
max. power

Turbine inertia does not contribute to system inertia!

Conclusion

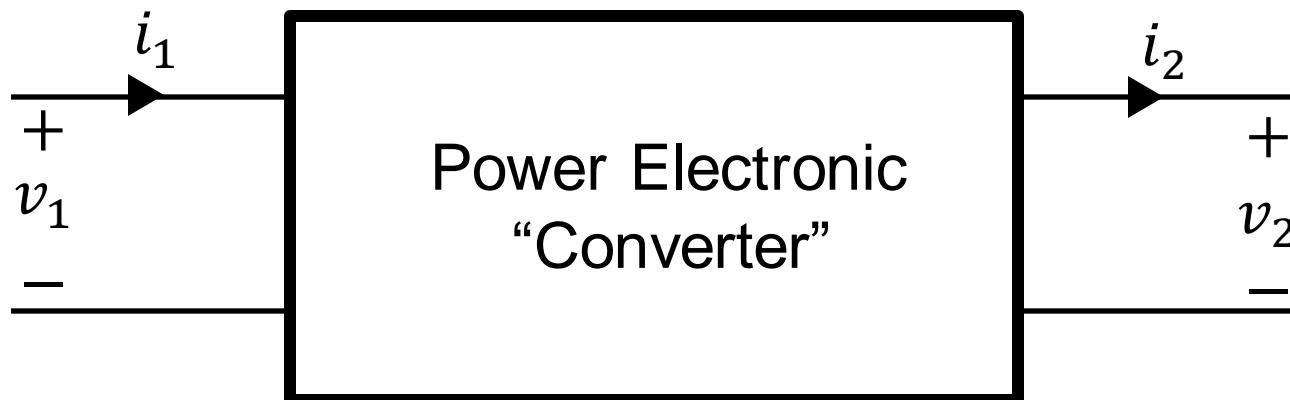
- Wind turbines convert kinetic energy of wind to electrical energy
- Turbine generators have inertia, but only fixed-speed turbines contribute inertia to power system
- Today, most generators are variable-speed to extract maximum power
- Power electronics connect turbines to grid, decoupling their inertia

Introduction to Power Electronics: dc/dc conversion

How do we transform and control the flow of electrical energy between dc ports?

General Idea of Power Electronics

Combine **active** electronic devices
and **passive** energy storage components to
efficiently transform and control the flow of energy
between **dissimilar** electrical ports



Four Classes of Power Conversion

	dc input	ac input
dc output	dc/dc	Rectifier
ac output	Inverter	Cycloconverter

Conversion doesn't always happen directly. E.g. ac-dc-ac or dc-ac-dc

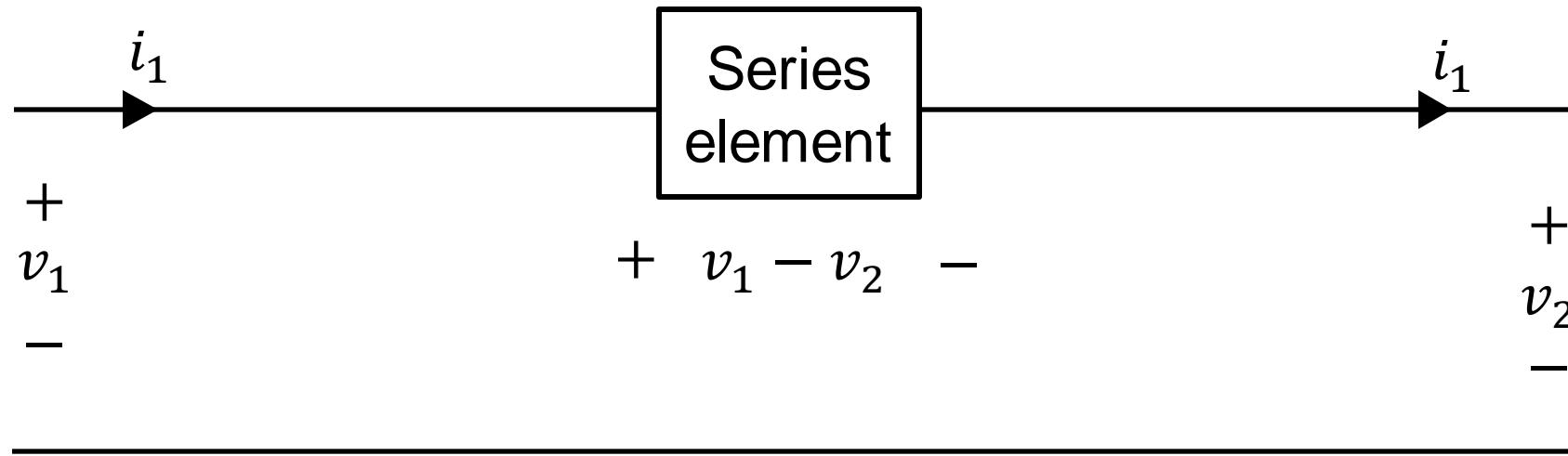
Four Classes of Power Conversion

	dc input	ac input
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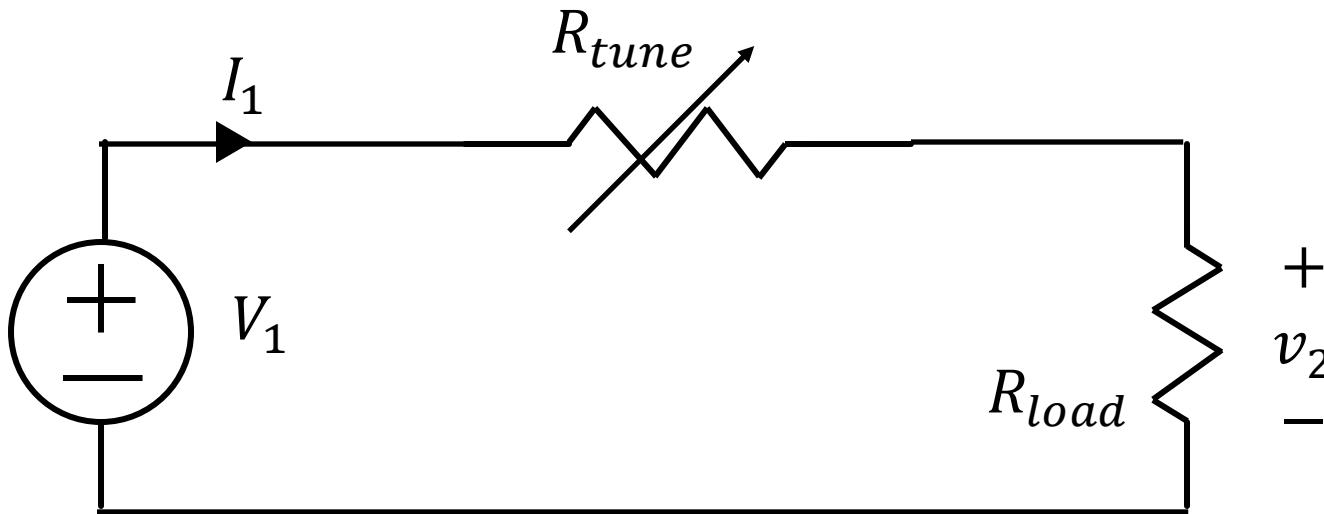
“Input” port is supplied power, “Output” port extracts power

Conversion doesn't always happen directly. E.g. ac-dc-ac or dc-ac-dc

Simplest Conversion Between dc Voltages



Using a Tunable Series Resistor



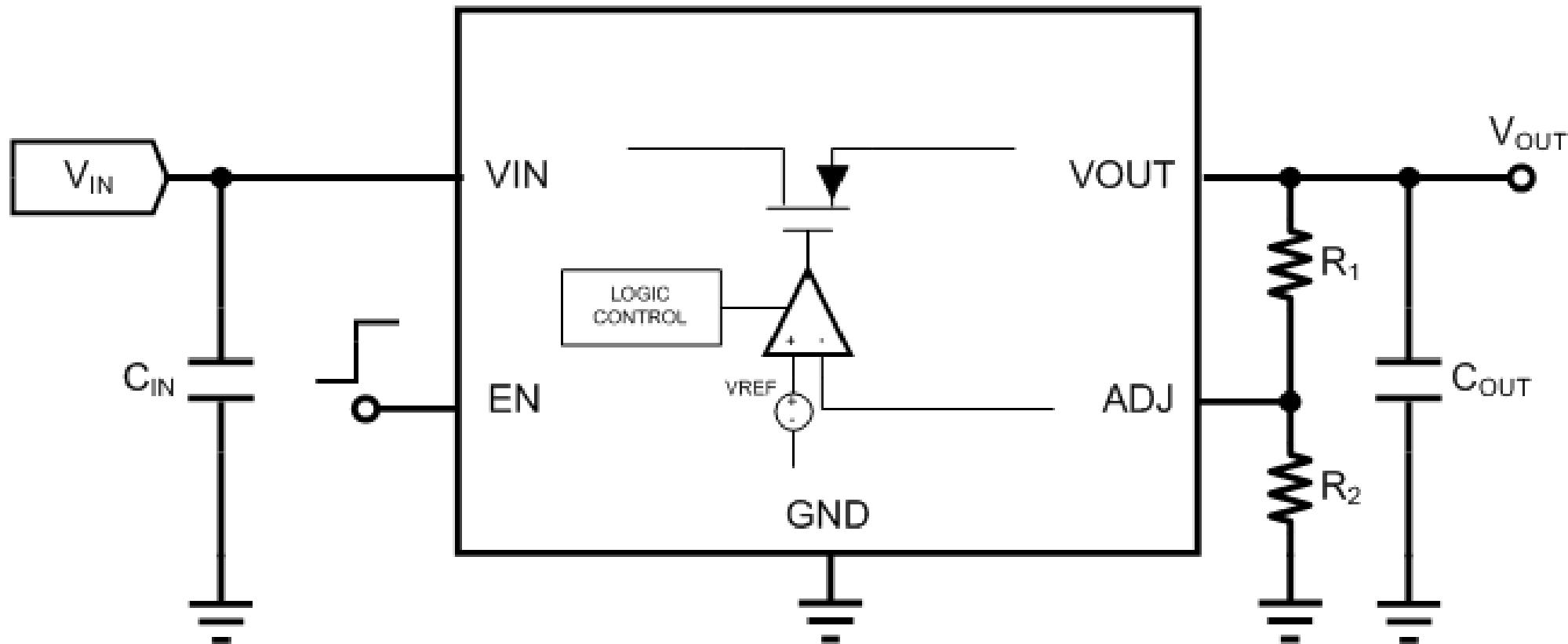
$$v_2 = \frac{R_{load}}{R_{load} + R_{tune}} v_1$$

$$\eta = \frac{V_2 I_1}{V_1 I_1} = \frac{V_2}{V_1}$$

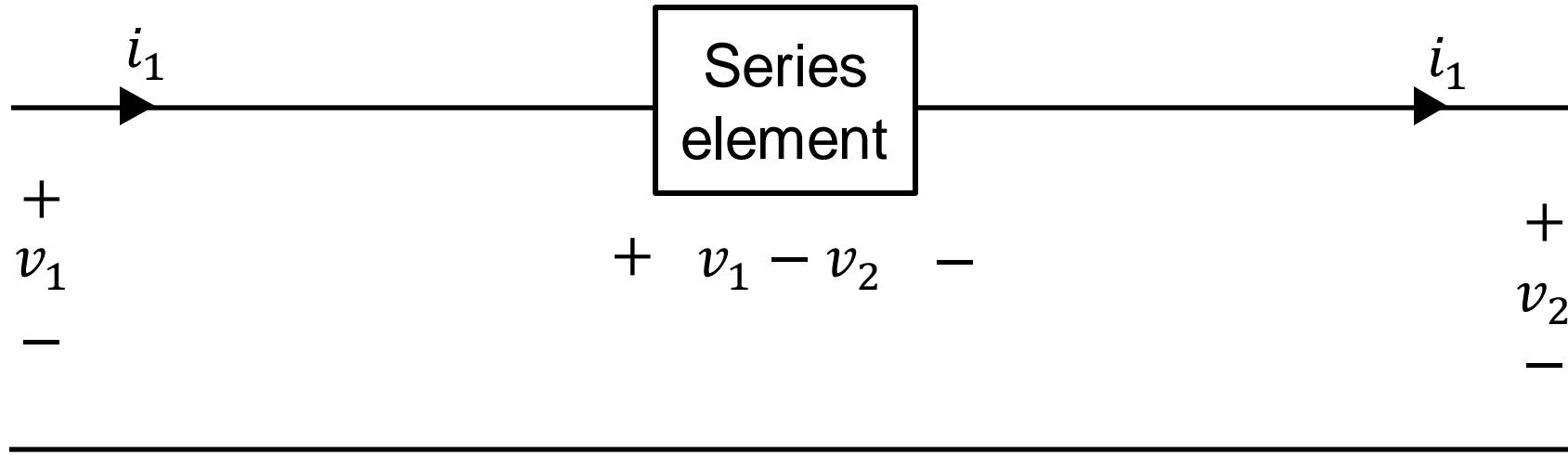
If $V_2 = 5V$, $V_1 = 10V$, $\eta = 50\%$!

Using a Regulated Current Source – “LDO”

$$\eta = V_{out} / V_{in}$$



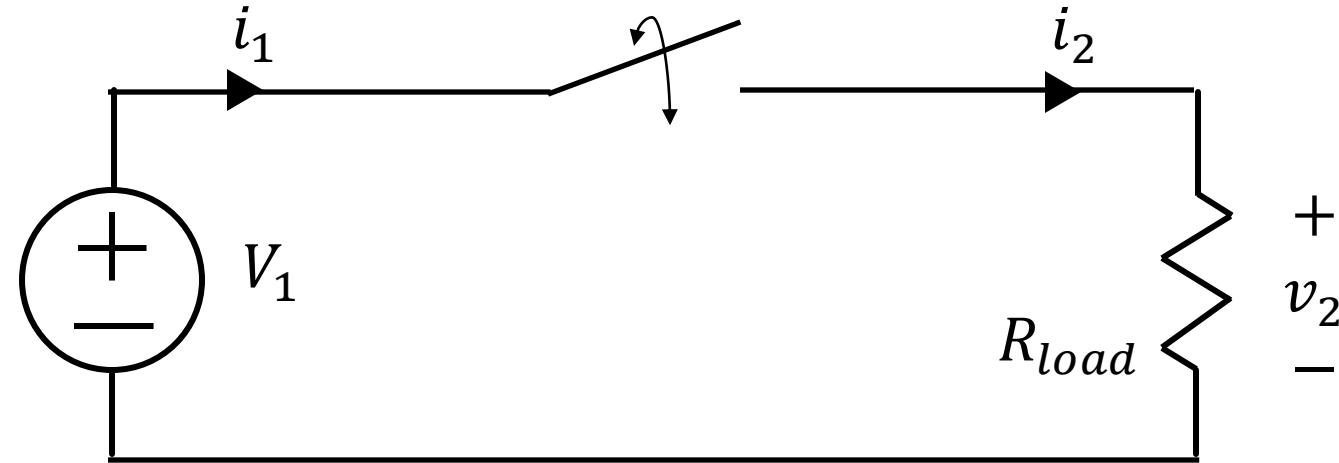
Simplest Conversion Between dc Voltages



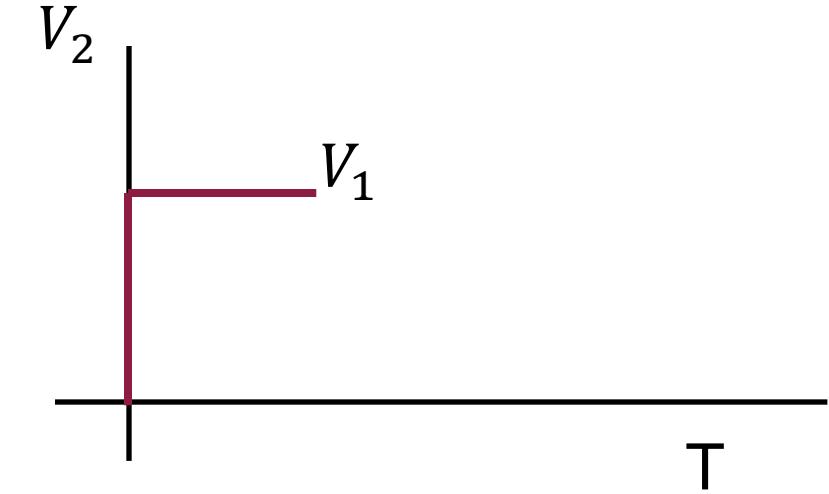
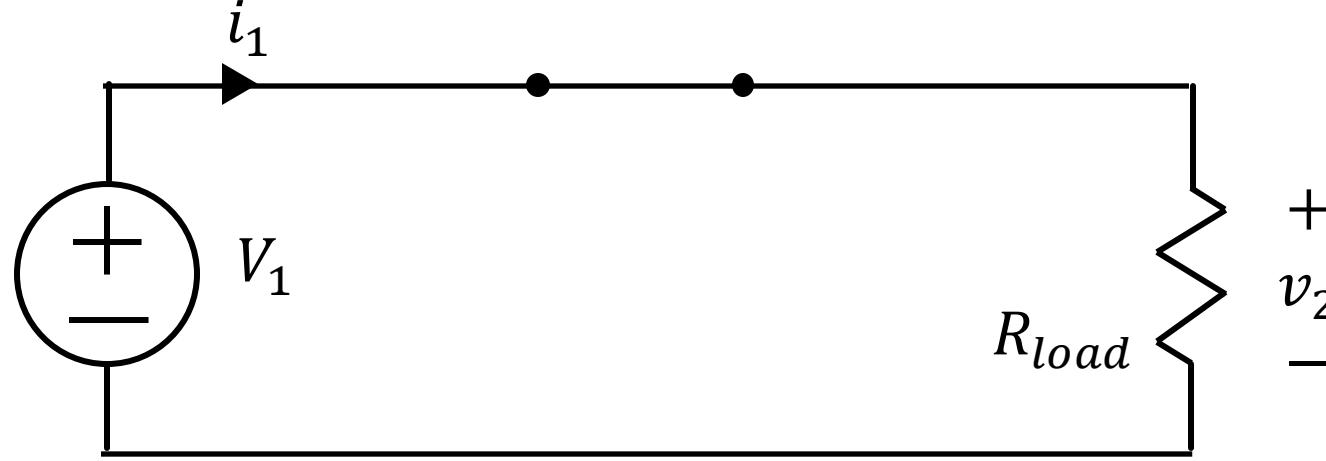
$$\eta = \frac{V_2 I_1}{V_1 I_1} = \frac{V_2}{V_1}$$

If $V_2 = 5V$, $V_1 = 10V$, $\eta = 50\%$!

What if Series Element was a Switch?

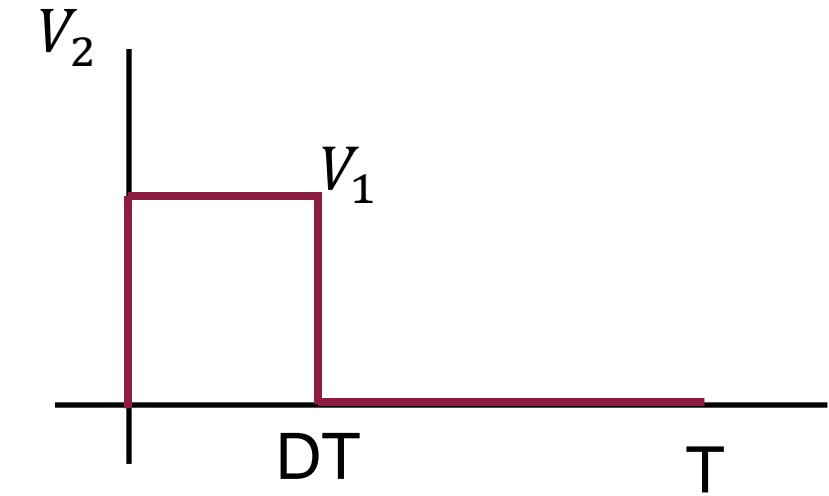
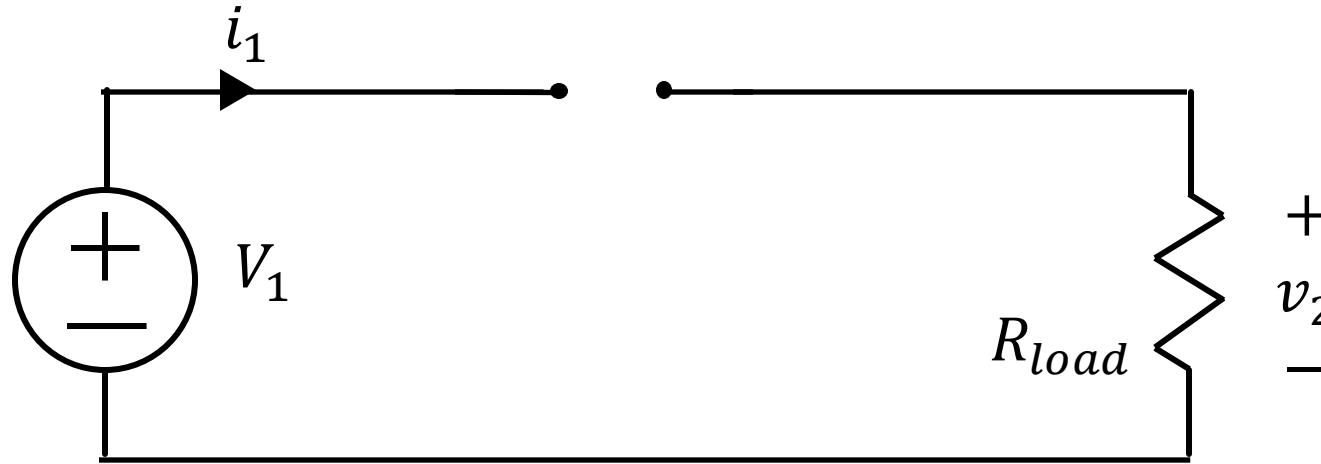


Switch Closed, No Voltage Drop



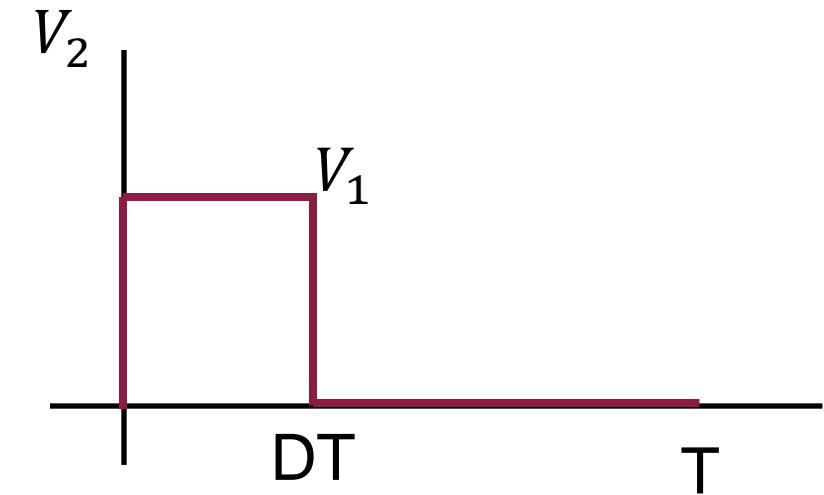
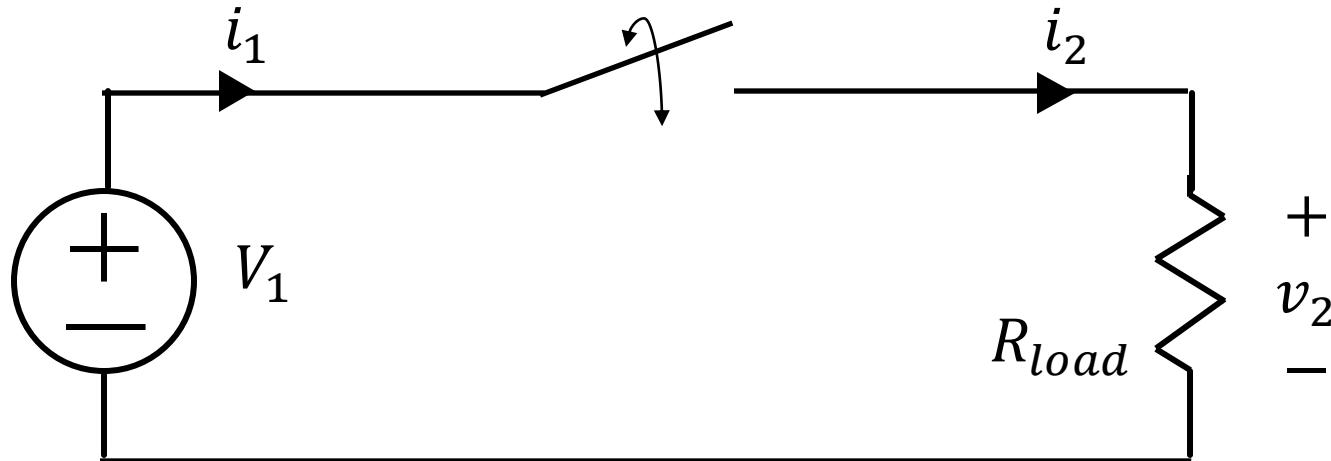
Ideal switch has zero voltage drop, no power loss

Switch Open, No Current Flow



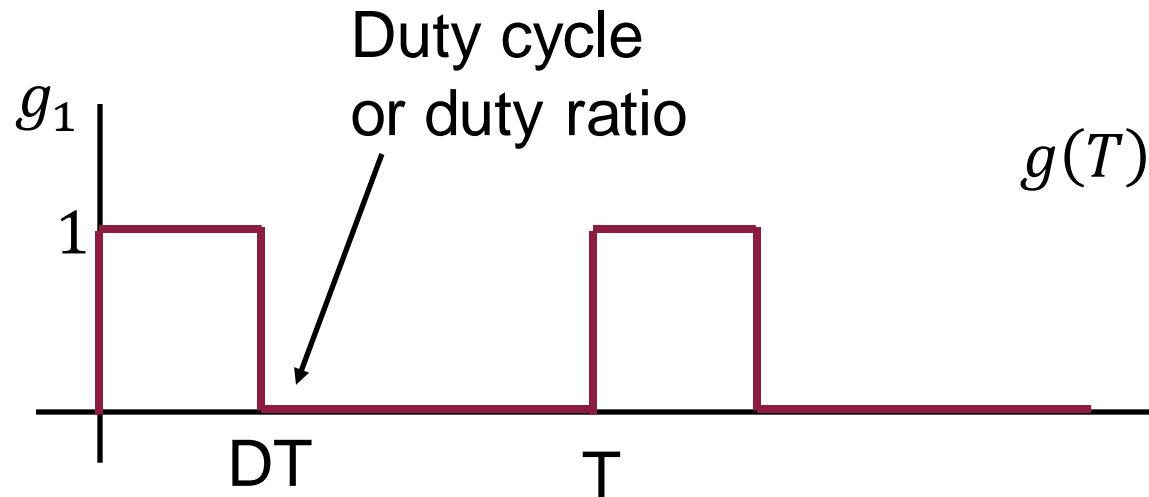
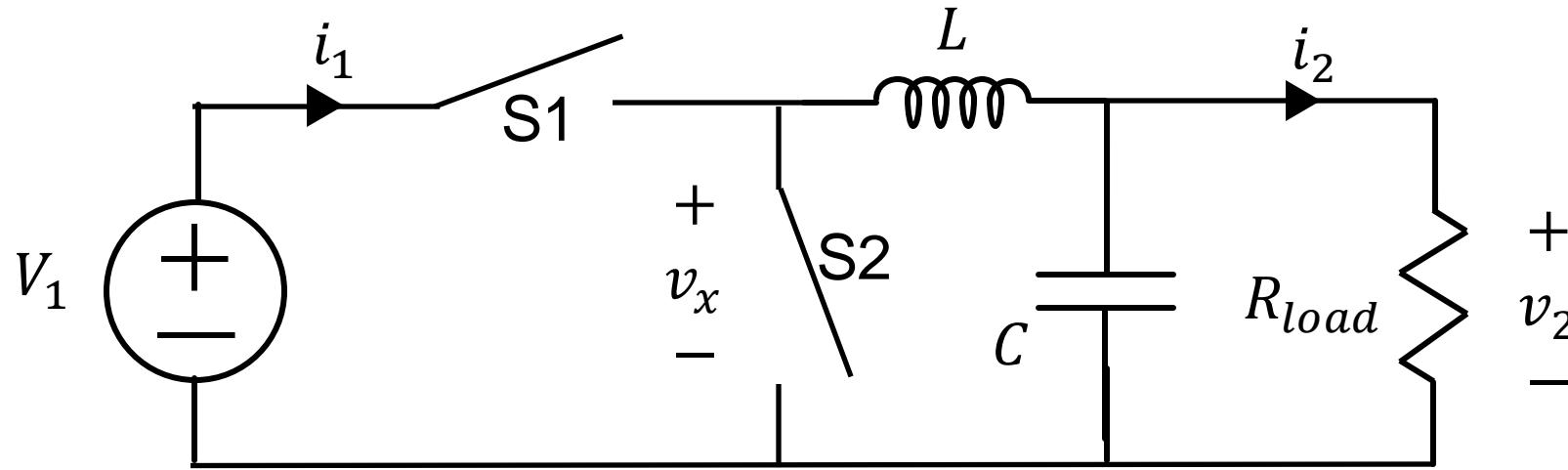
Ideal switch has zero current flow, no power loss

An Efficient but Noisy dc/dc Converter

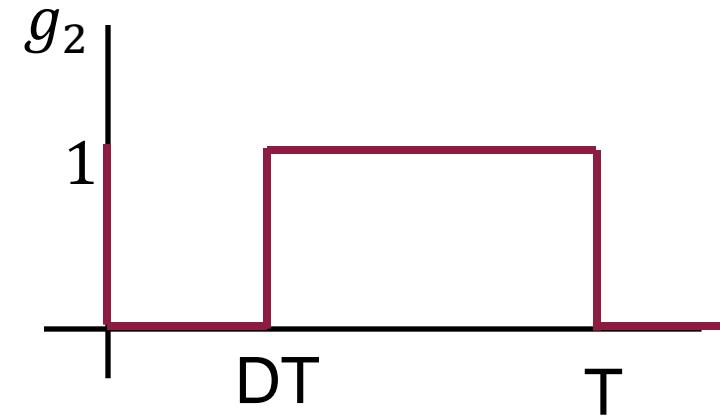


1. Conversion is lossless
2. Average output voltage is DV_1 -- controllable!
3. Output voltage is ac (we've made an inverter)
4. Input current is ac

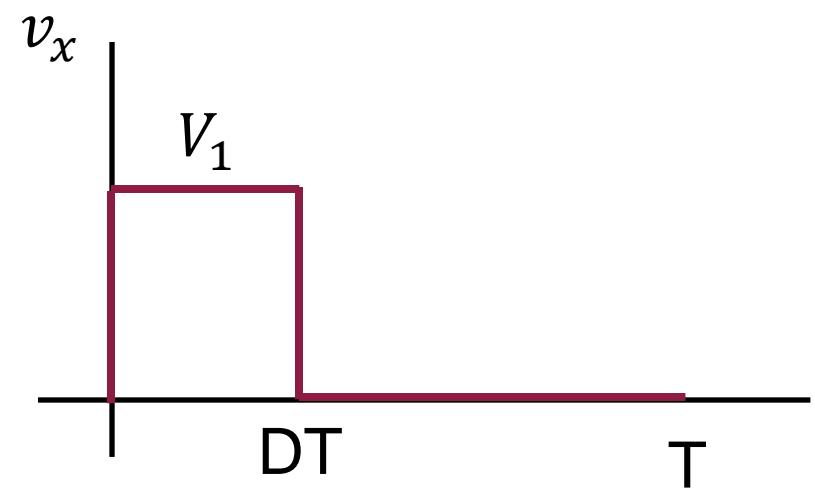
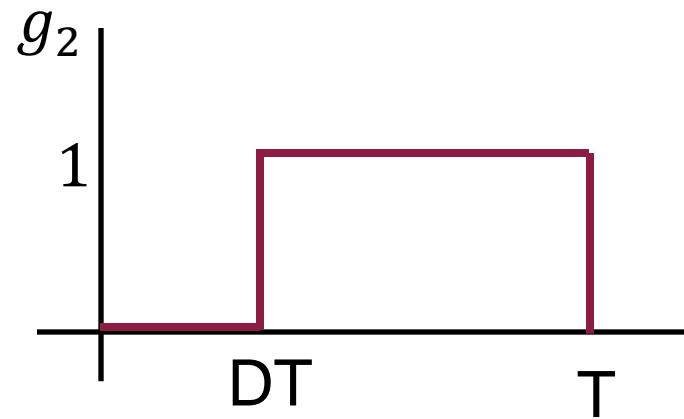
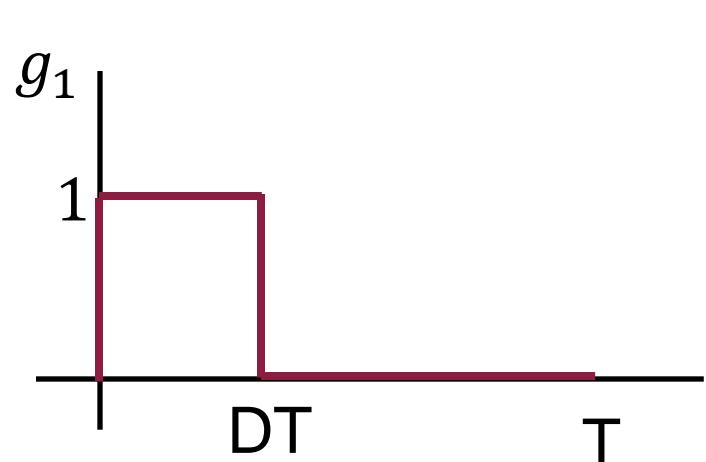
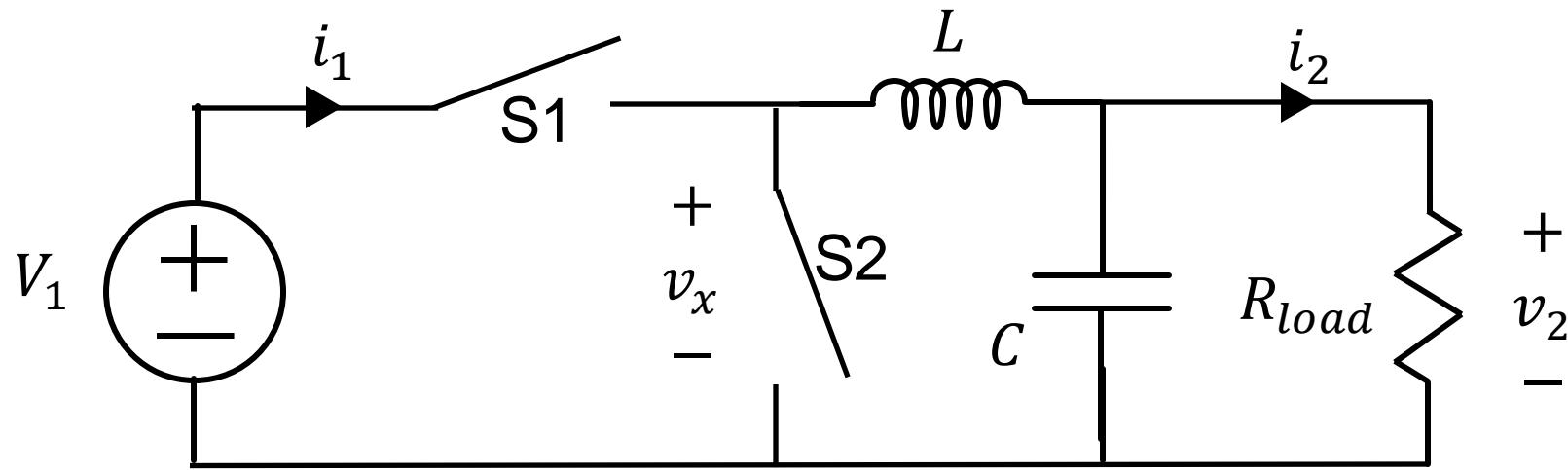
The “Buck” Converter



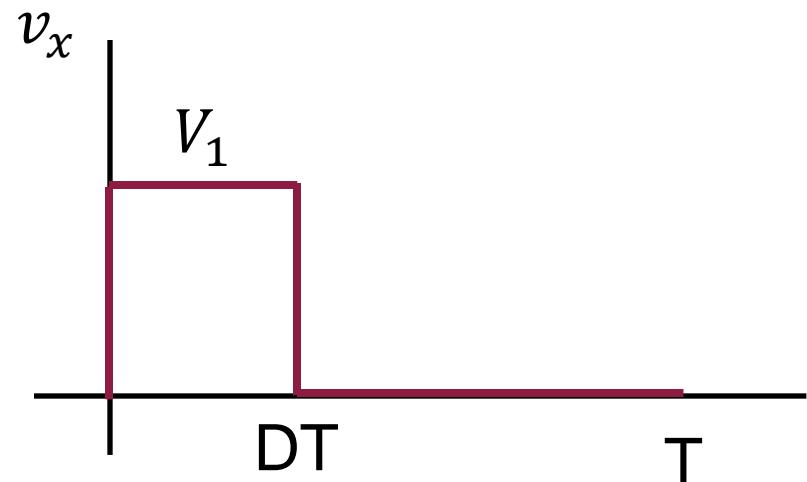
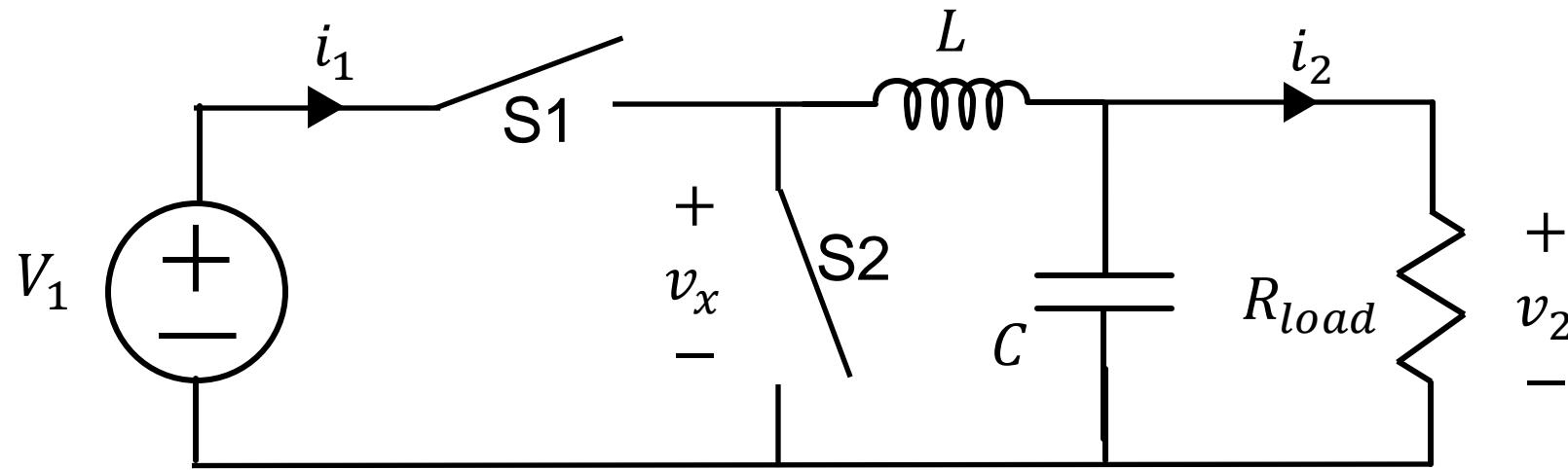
$$g(T) = g(0)$$



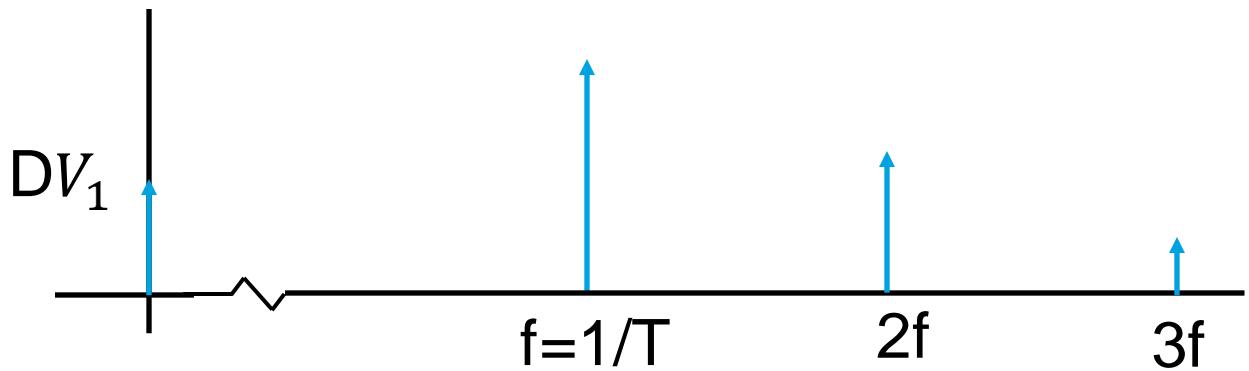
The “Buck” Converter



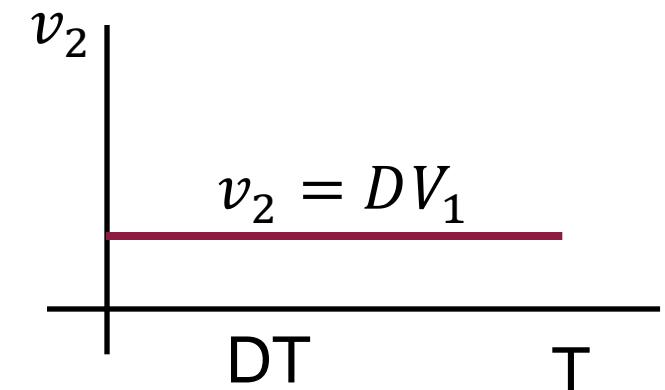
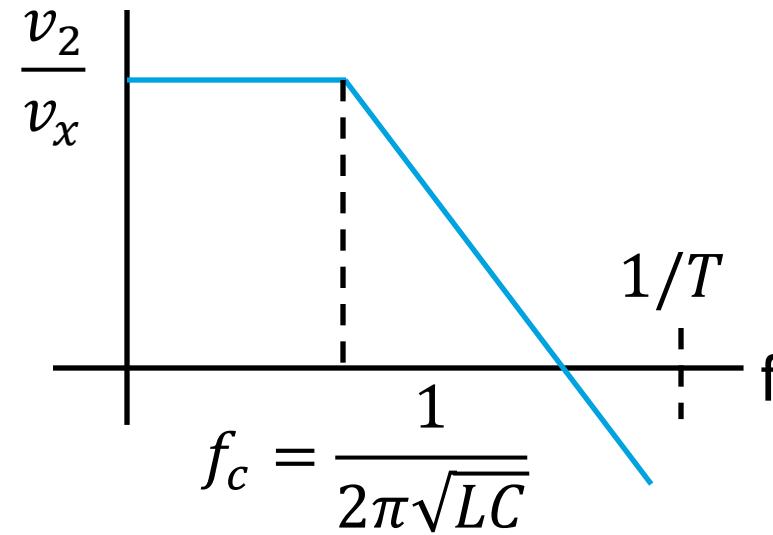
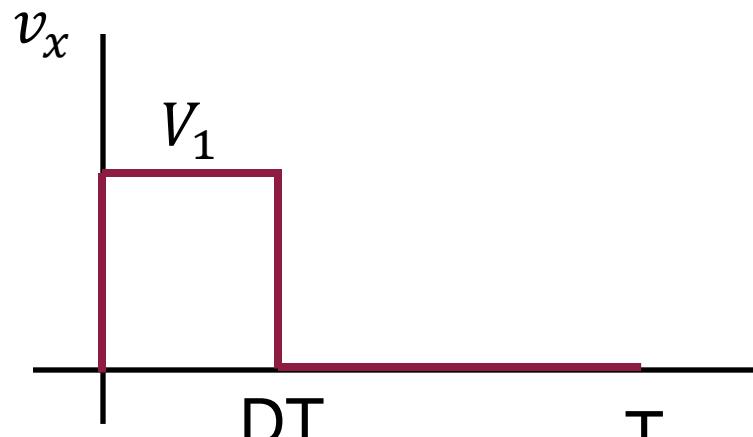
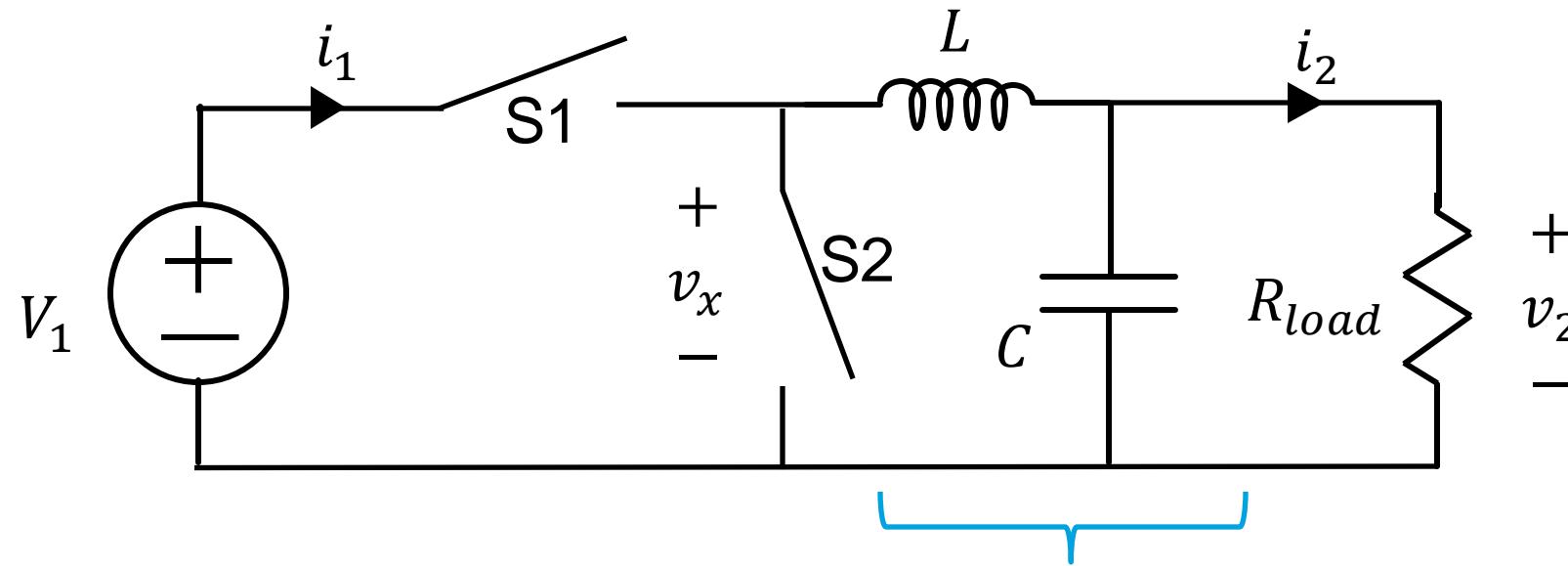
Harmonic Content of Switch Voltage



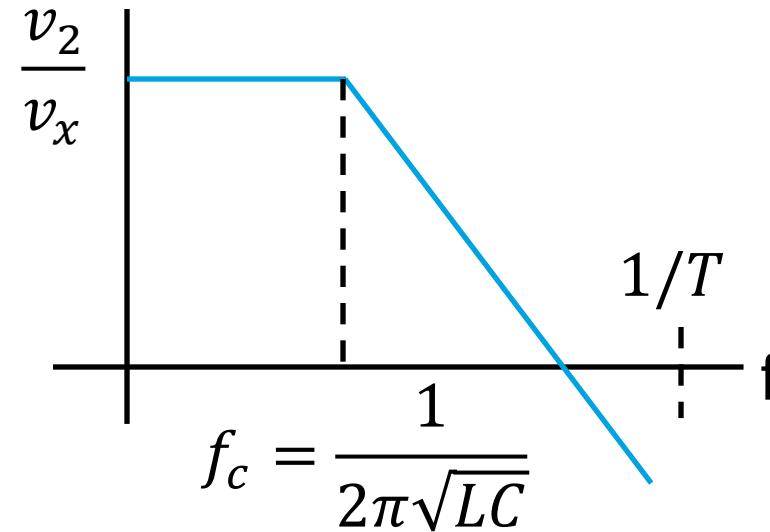
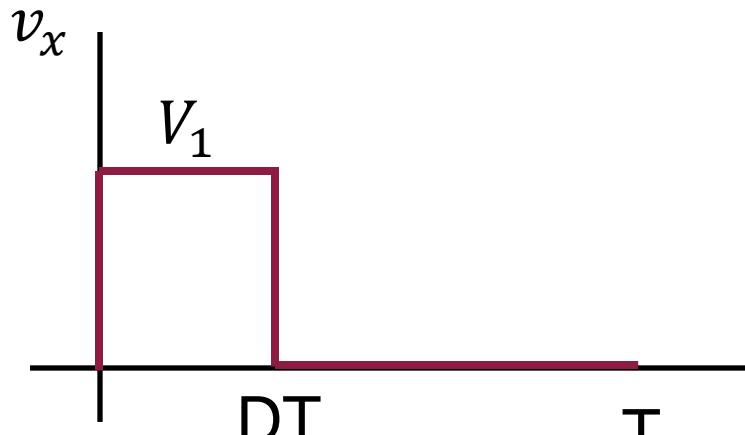
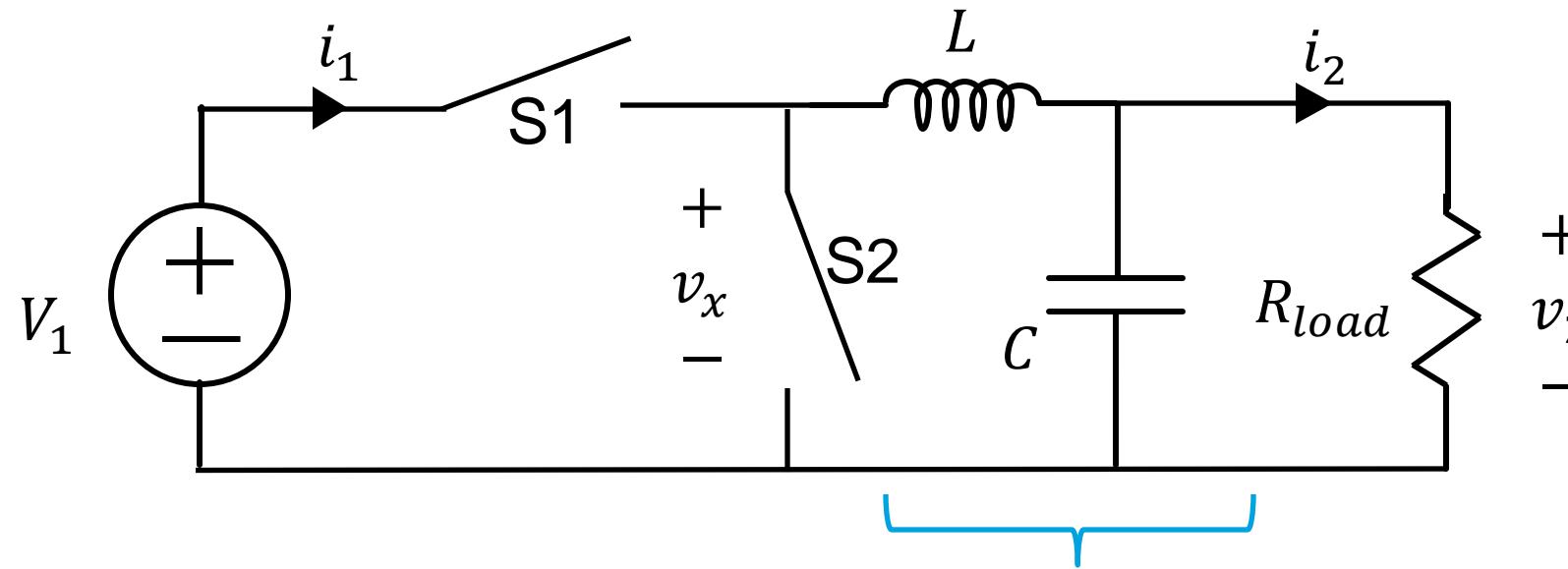
Harmonic amplitude



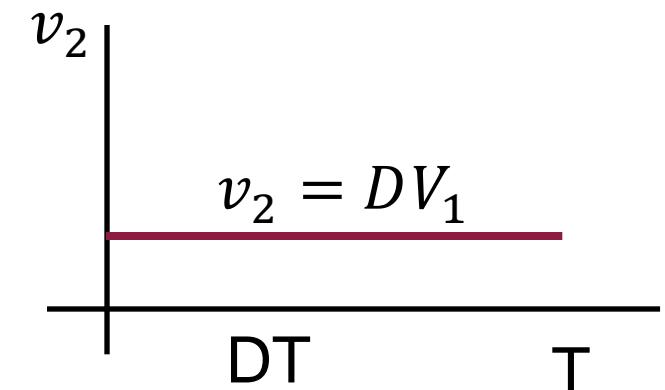
LC Branch Filters Harmonics



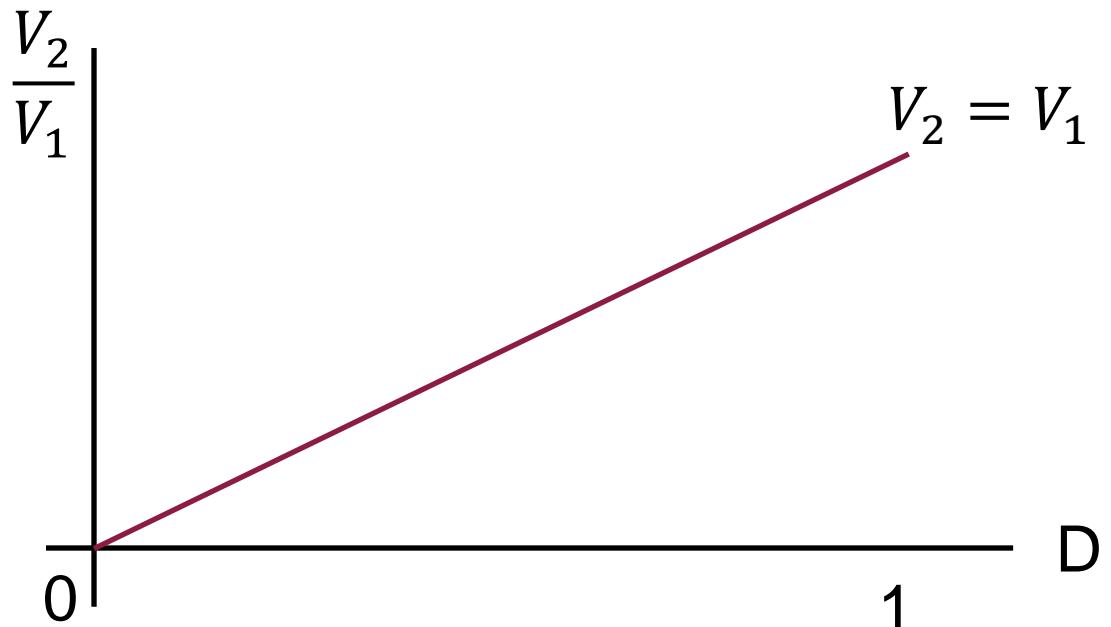
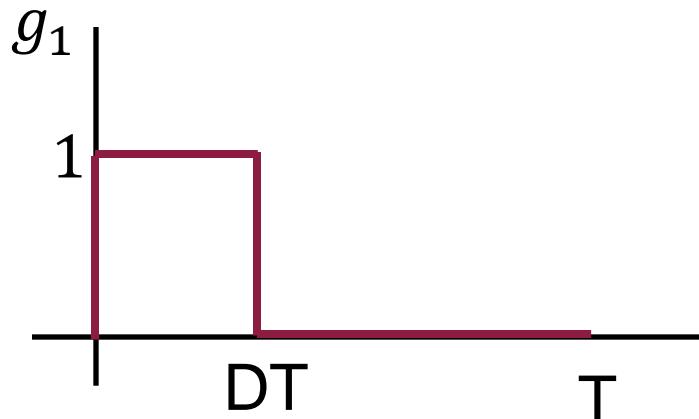
Very High Efficiency Achievable



$\eta > 80\%$ typical
 $\eta > 99\%$ achievable

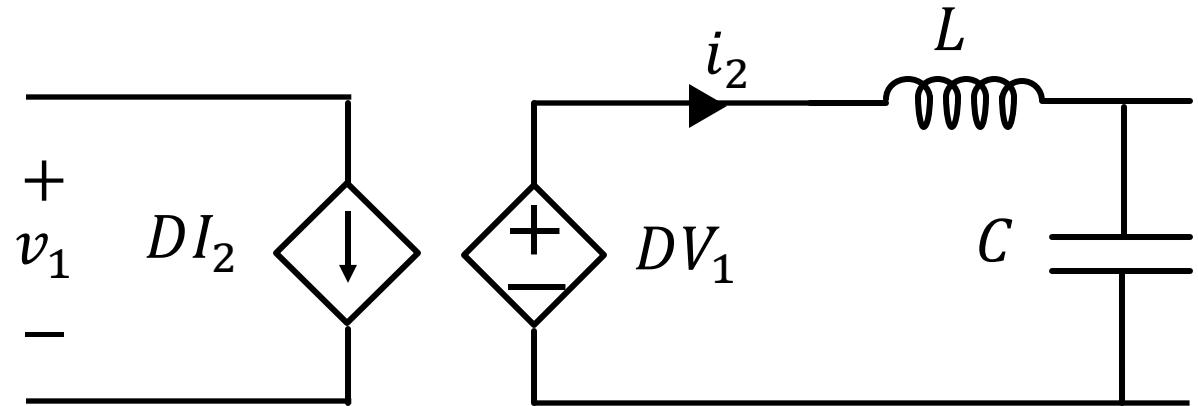
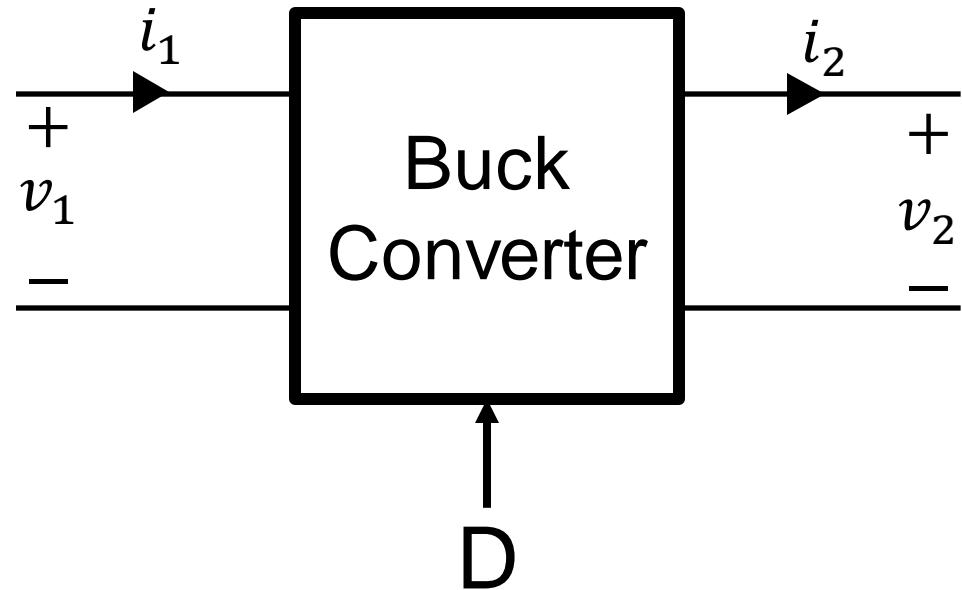


“Pulse Width Modulation” (PWM)



D is either constant or varied **much** more slowly
than the switching period

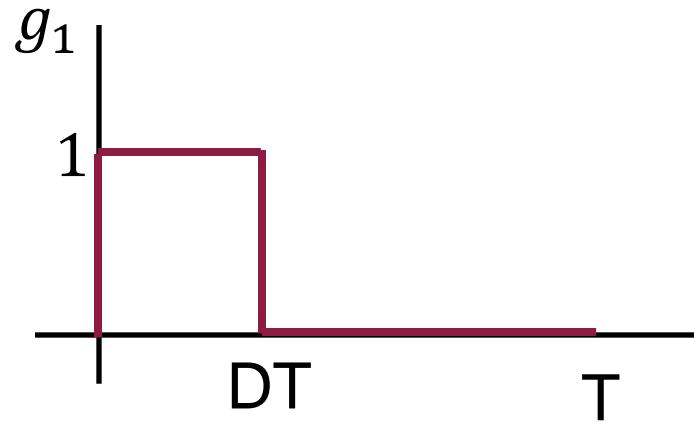
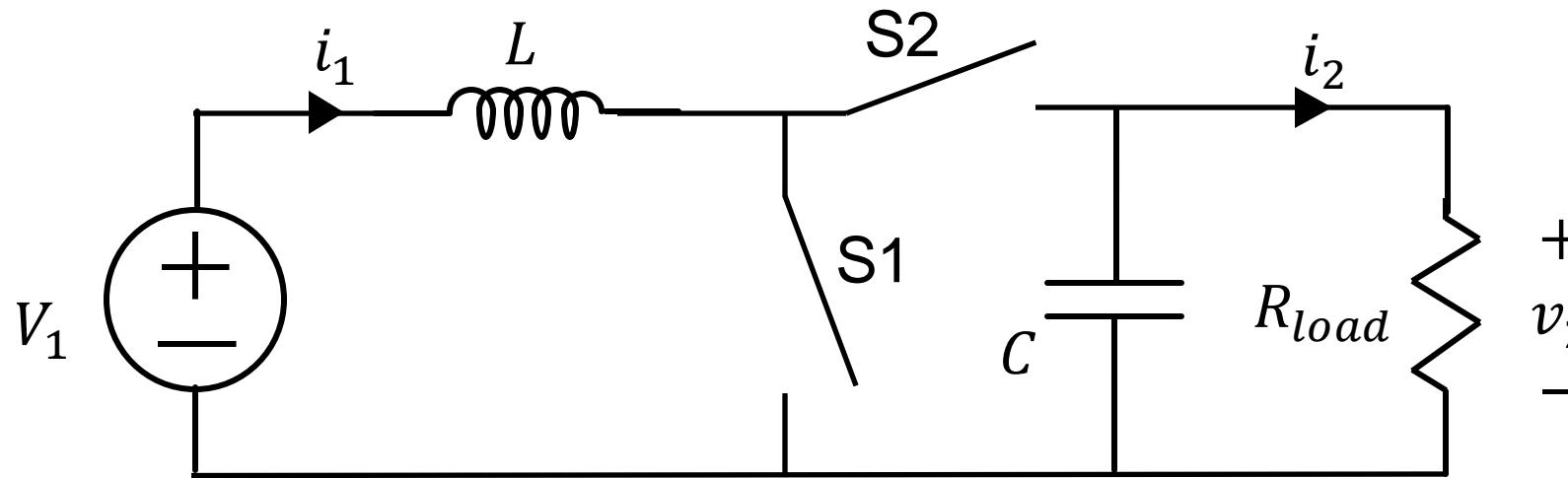
Averaged Buck Converter Model



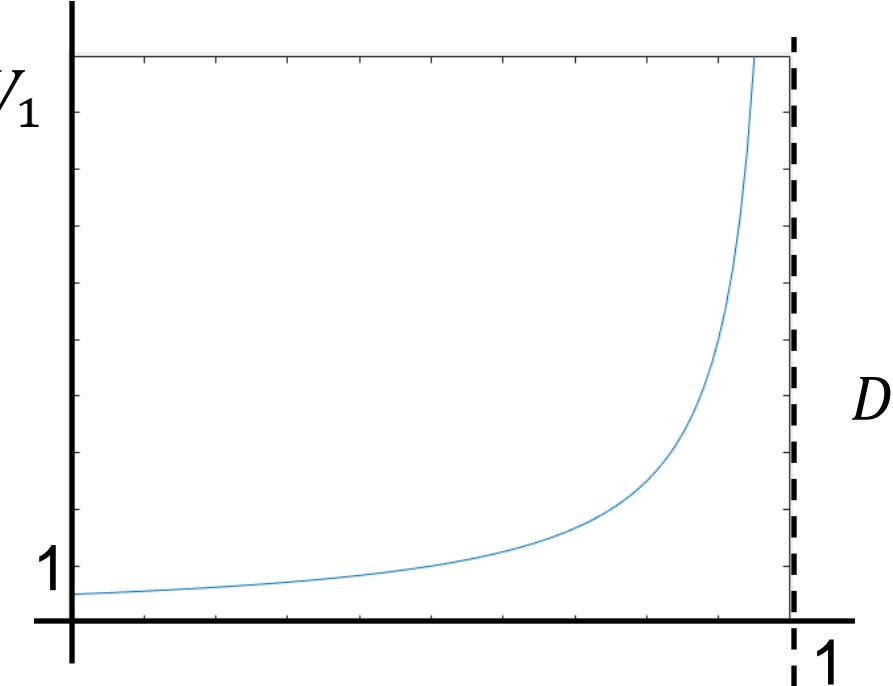
Typically $D \in [0.05, 1]$

Reduces or “bucks” or “chops”
input voltage

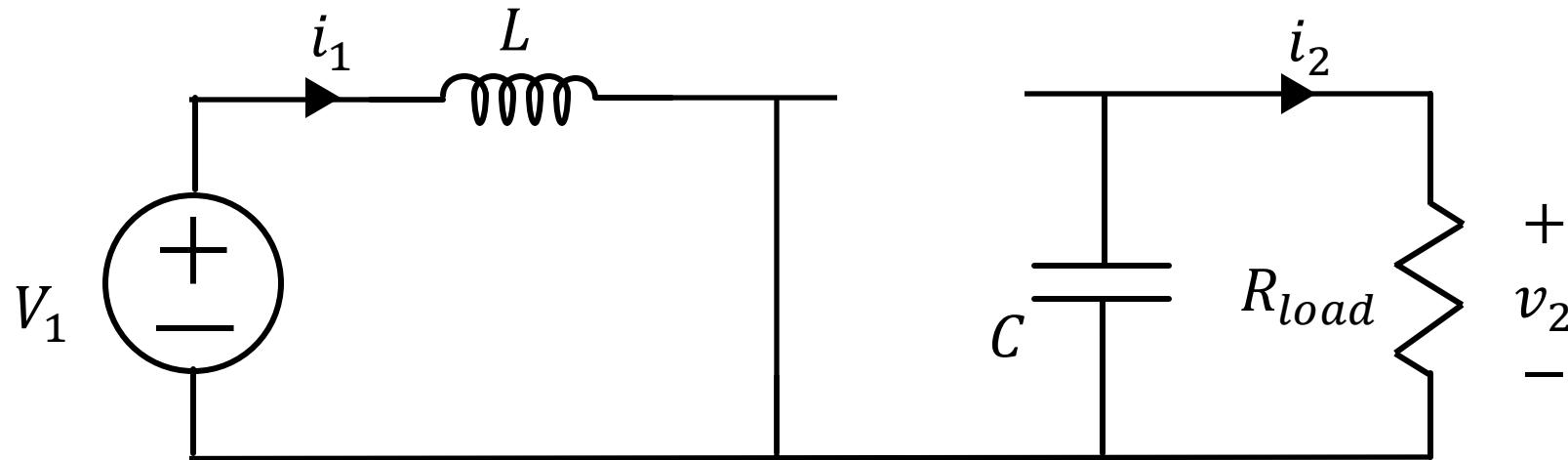
The “Boost” Converter



$$V_2 = \frac{V_1}{1 - D}$$

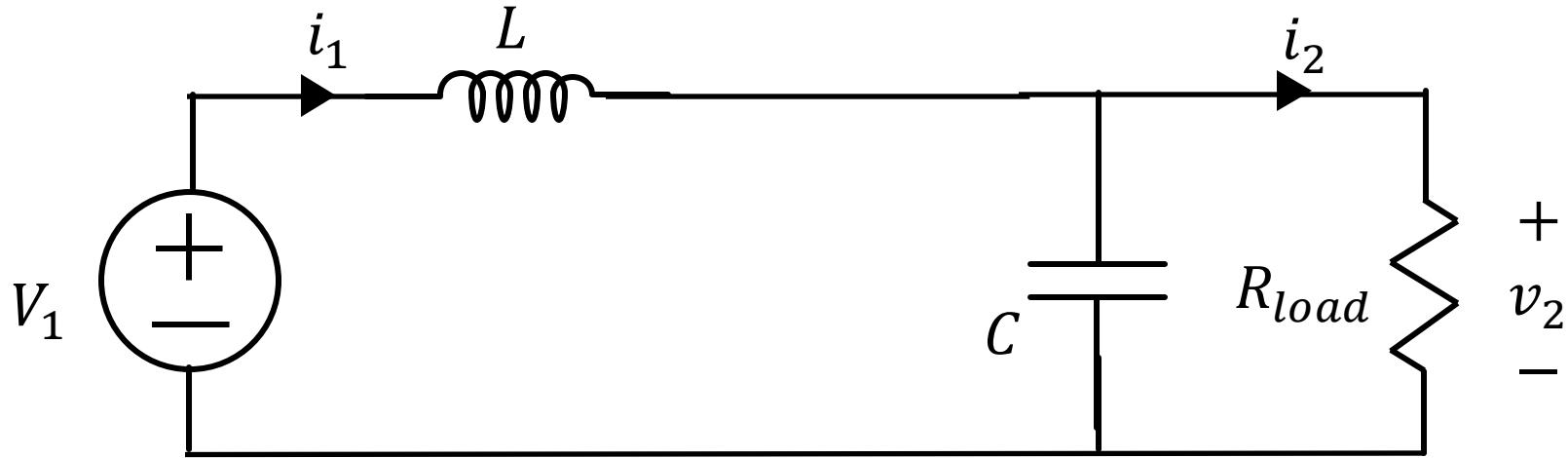


The “Boost” Converter



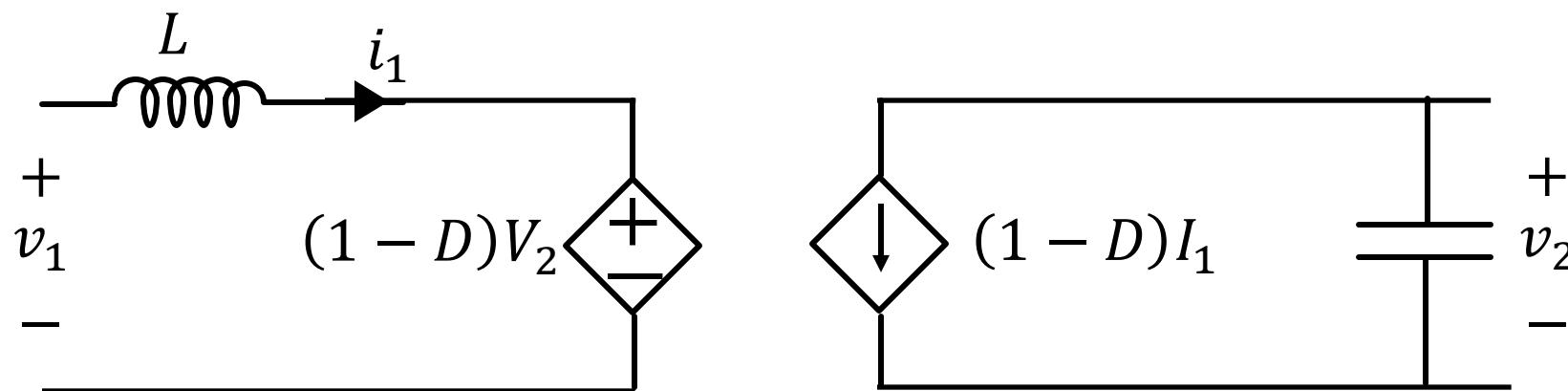
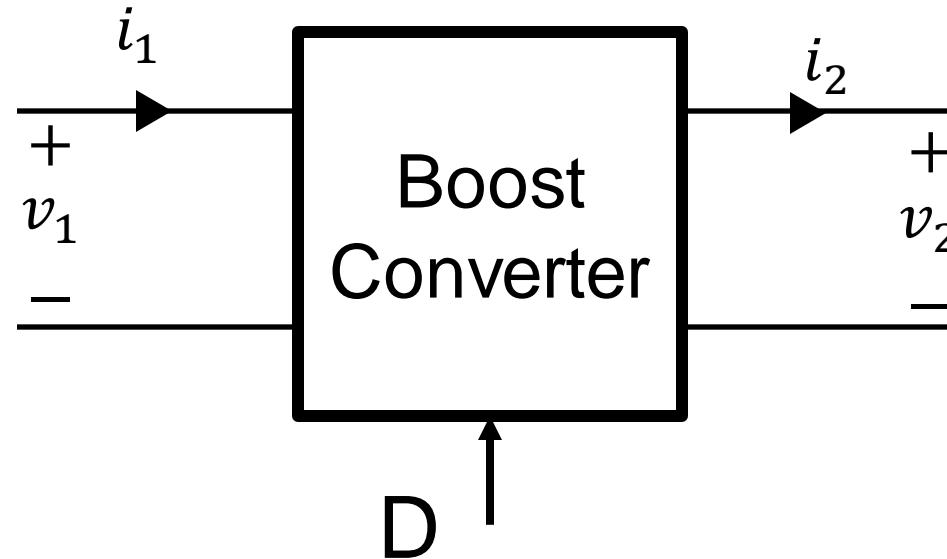
Energy transferred from V_1 into L

The “Boost” Converter

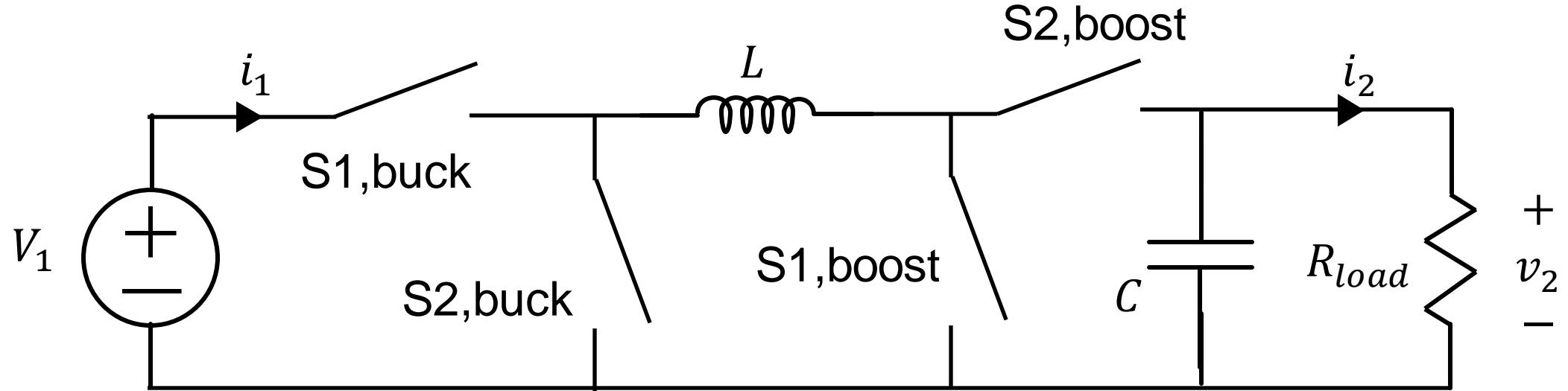


Energy transferred from V_1 and L into output

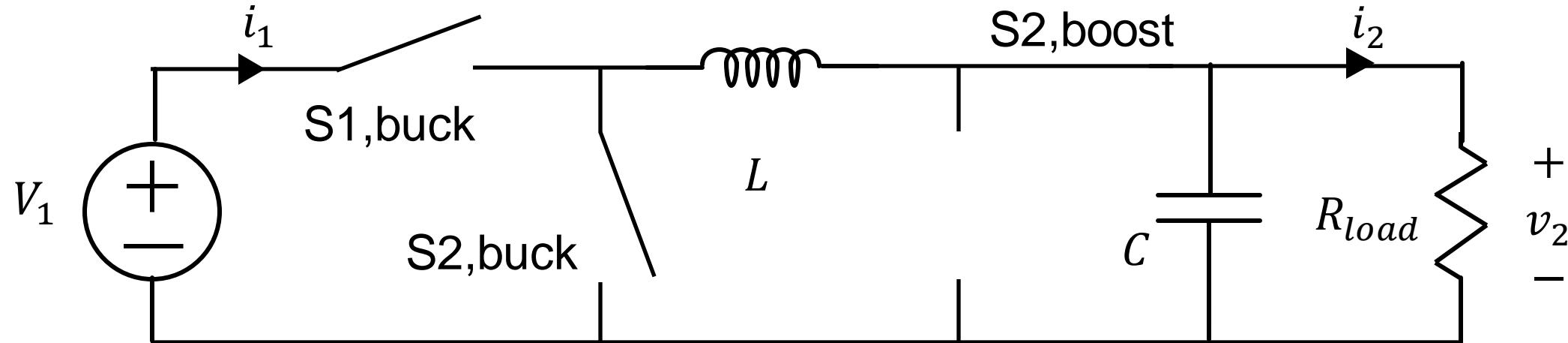
Averaged Boost Converter Model



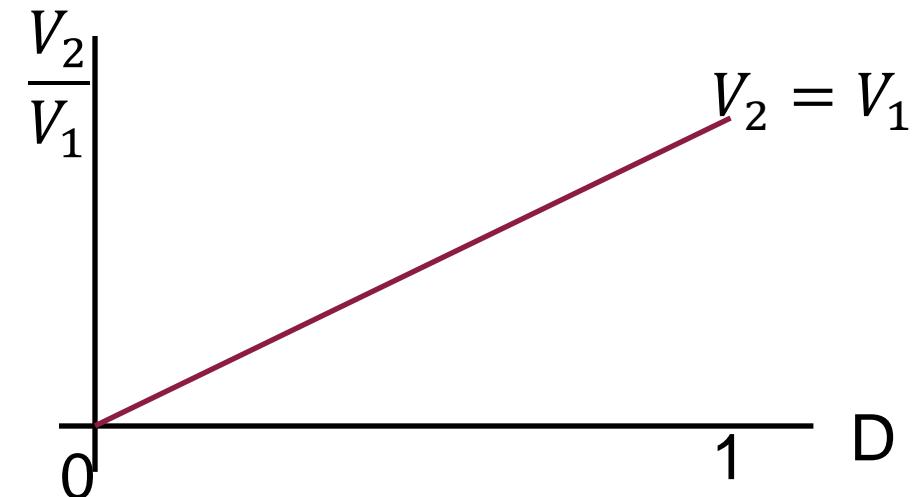
Non-inverting Buck-Boost



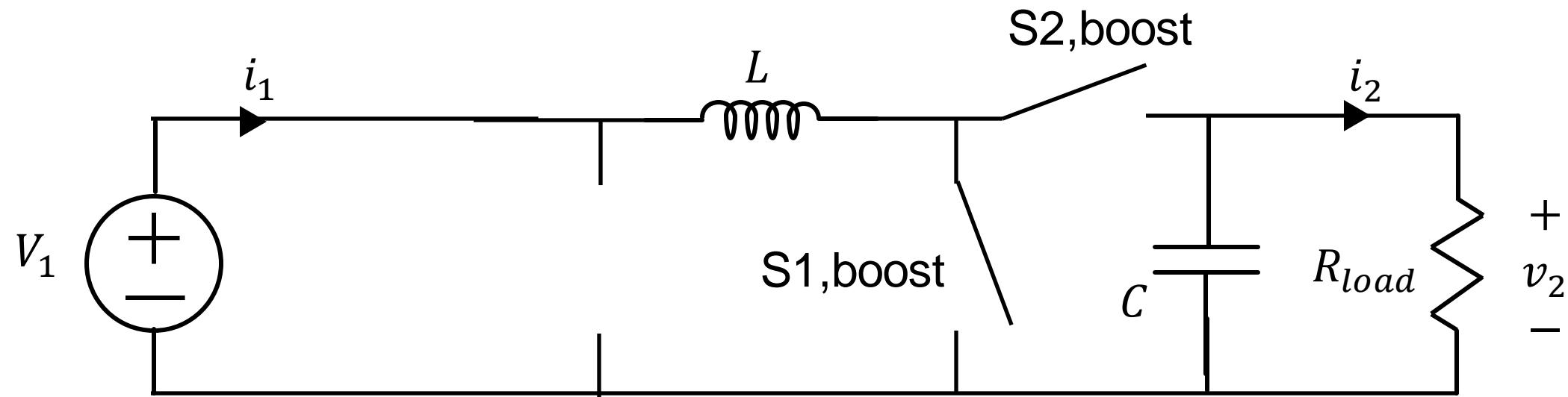
Non-inverting Buck-Boost – Buck Operation



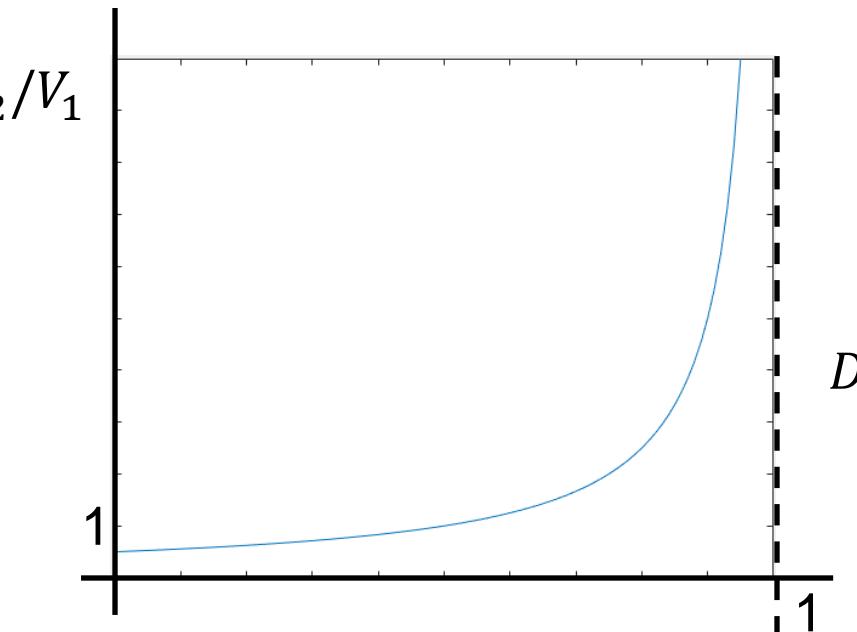
Hold S2,boost on,
PWM buck switches



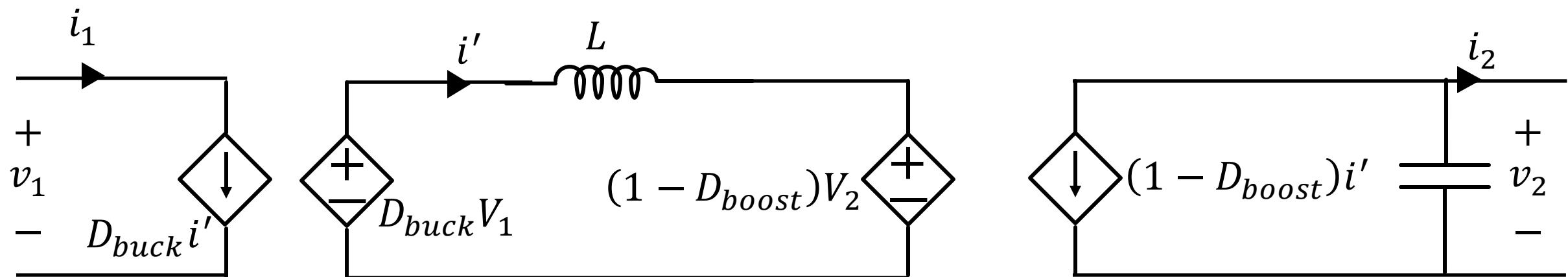
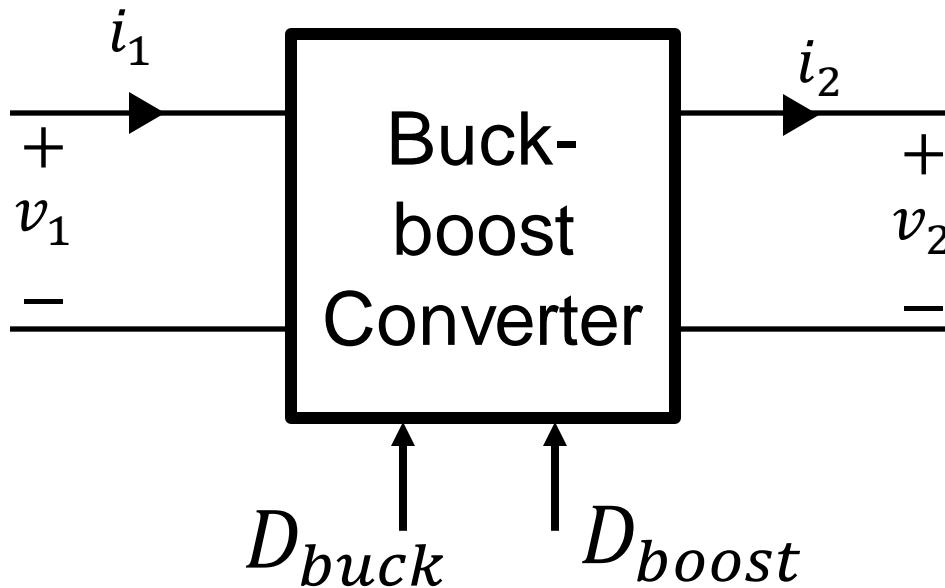
Non-inverting Buck-Boost – Boost Operation



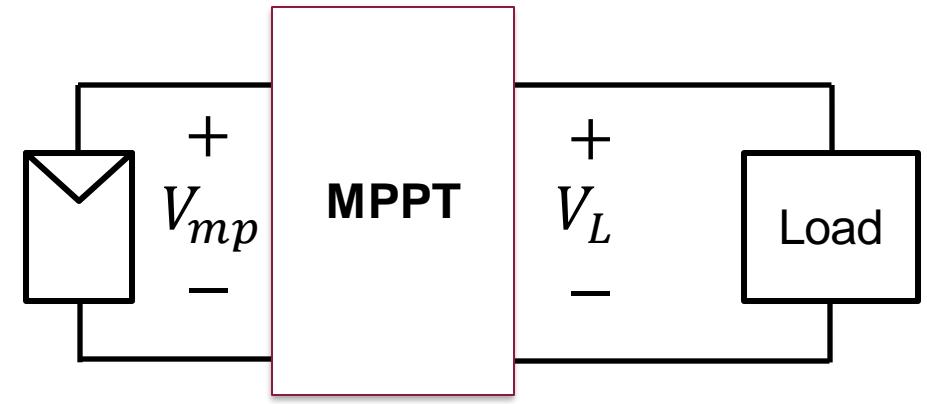
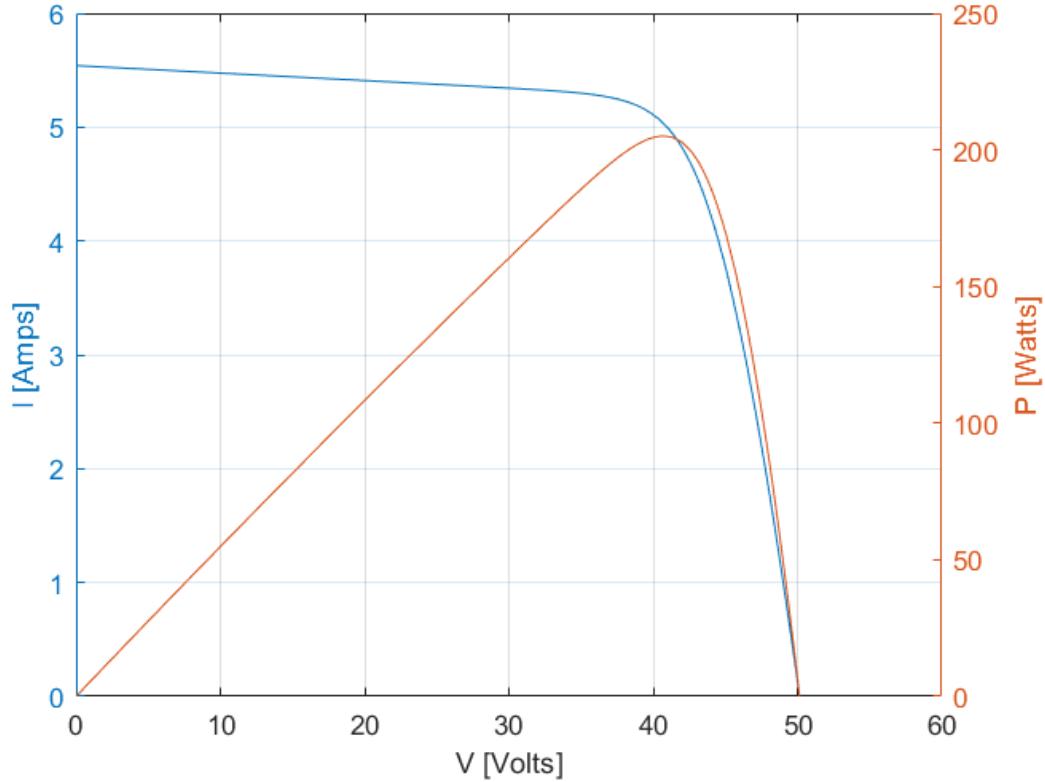
Hold $S1, \text{buck}$ on,
PWM boost switches



Averaged Buck-Boost Converter Model



Application: Solar PV MPPT



$$V_{mp} = 40V$$
$$V_L = 100V$$

Use boost converter, $D = 0.6$

Conclusion

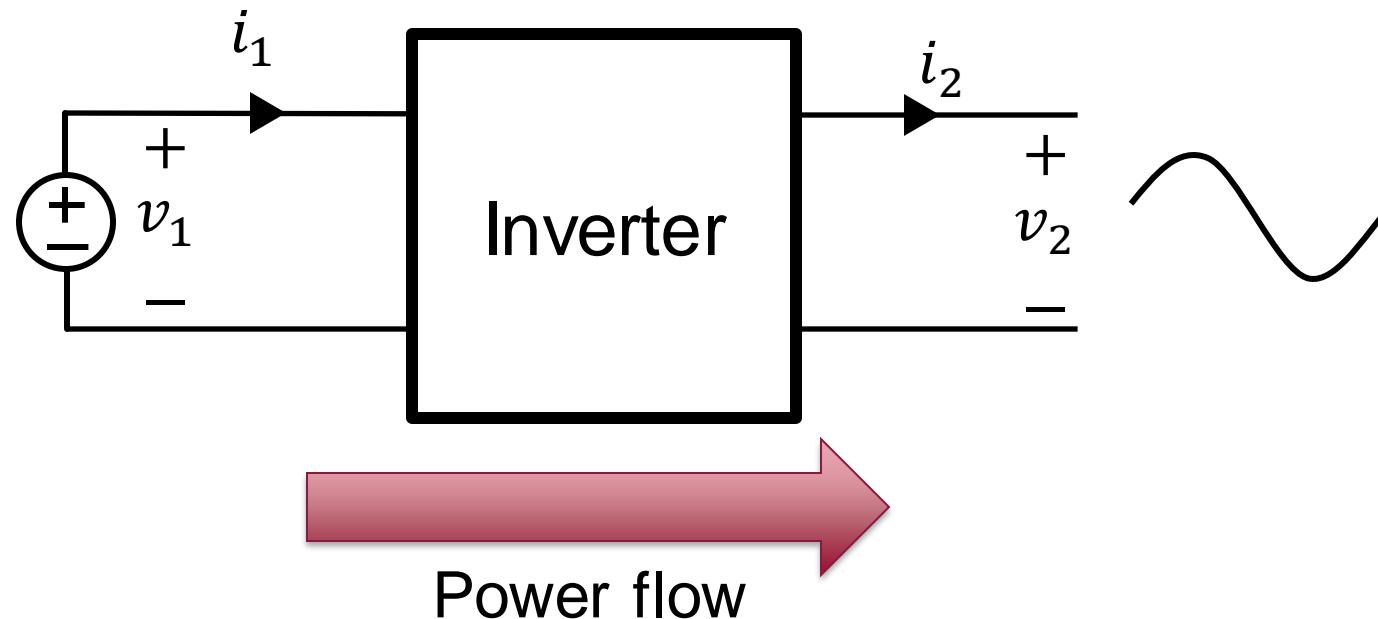
- Power electronics combine active electronic switches with passive energy storage components
- Very high efficiency dc/dc conversion is achievable
- The buck, boost, and non-inverting buck-boost are popular dc/dc conversion topologies
- These are widely used for solar PV MPPT.

Introduction to Power Electronics: Inverters

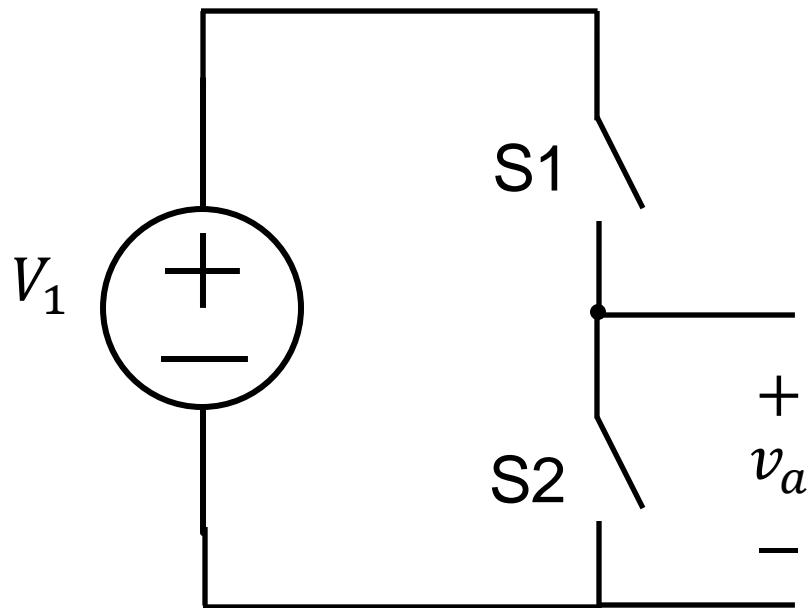
How do we transform and control the flow of electrical energy between a dc port and an ac port?

dc/ac Conversion: PWM Inverters

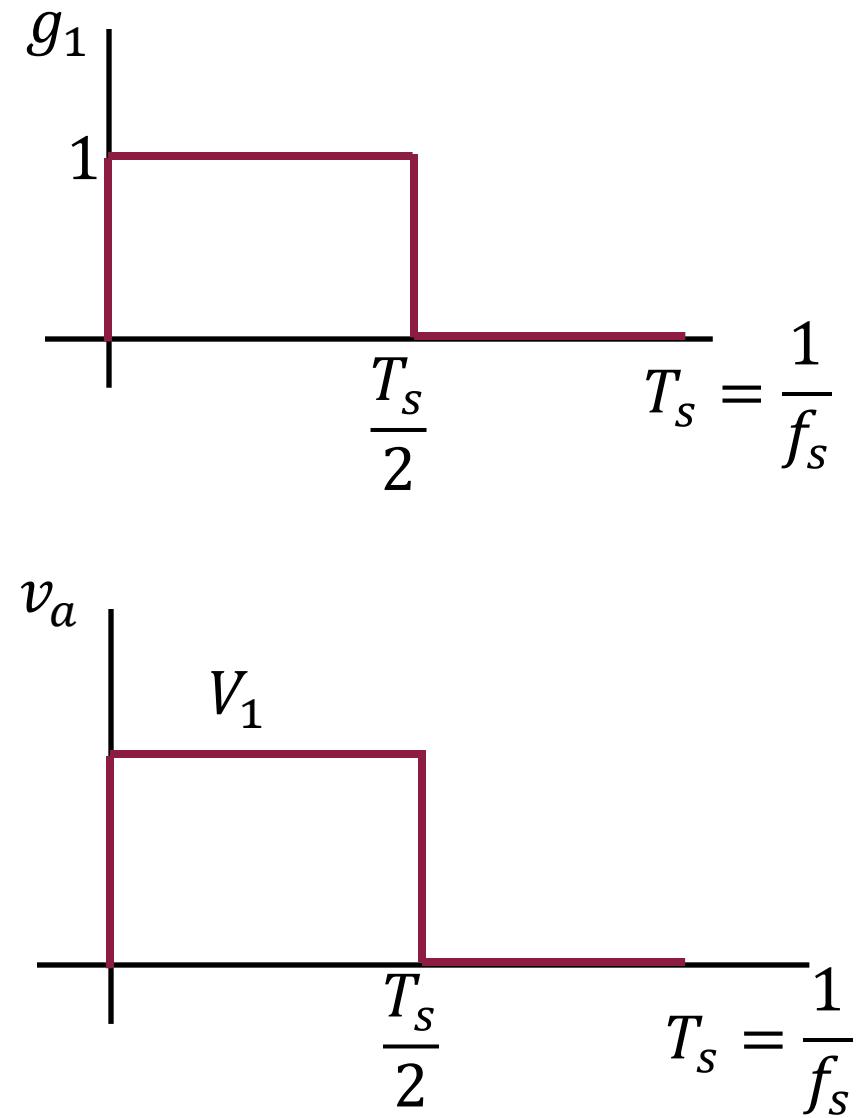
- Objective: produce a low-distortion sinusoidal voltage from a dc source



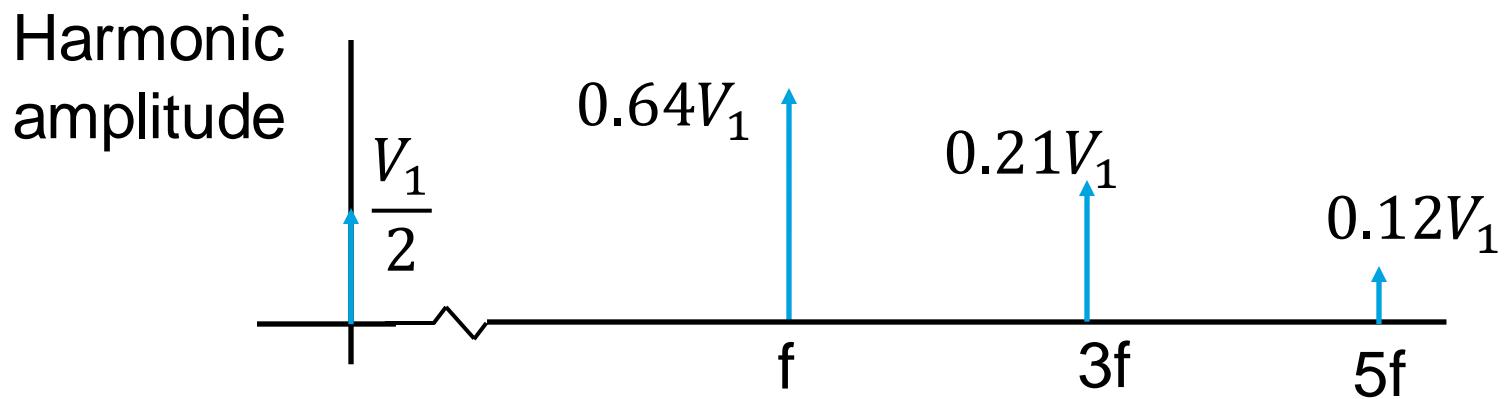
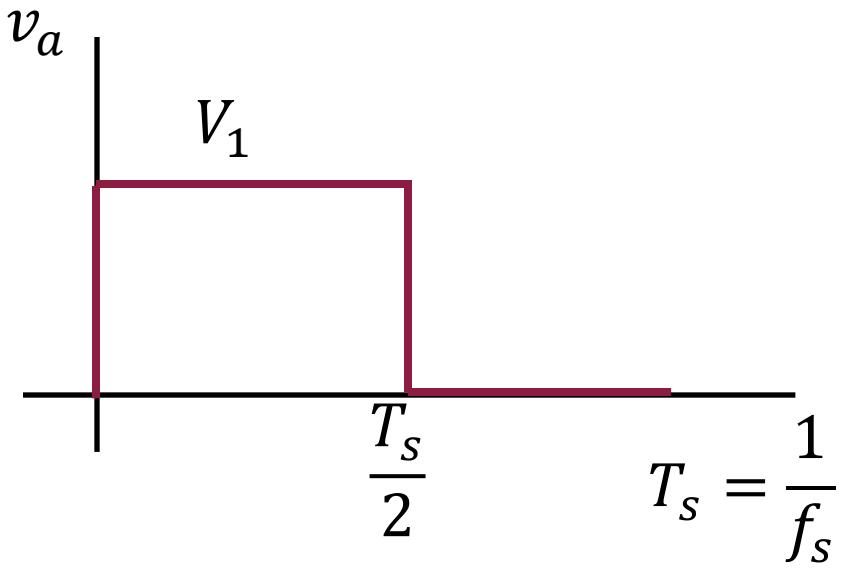
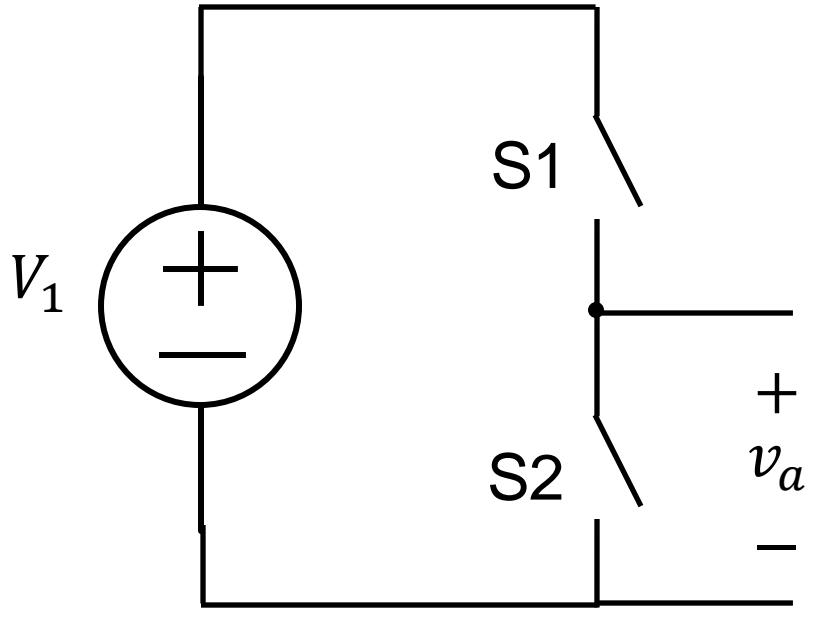
Half-Bridge Switching Cell



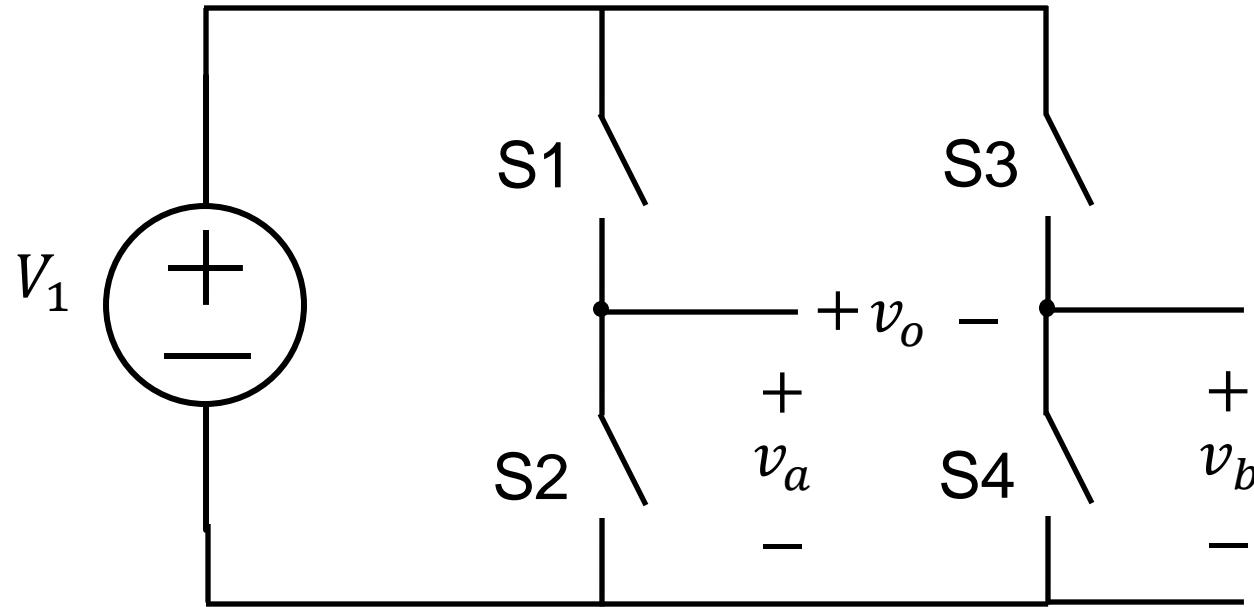
$$v_x = g_1 \cdot V_1$$



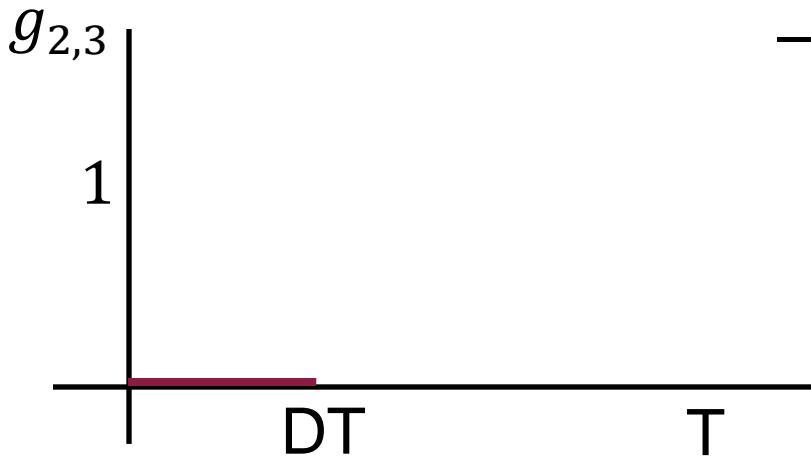
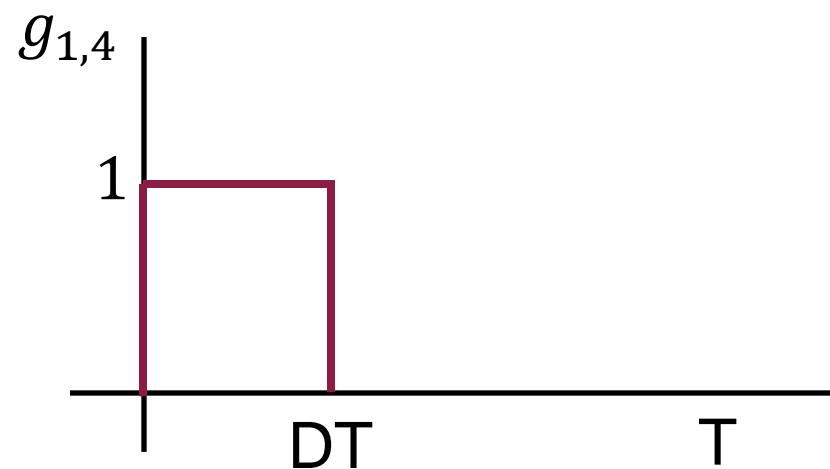
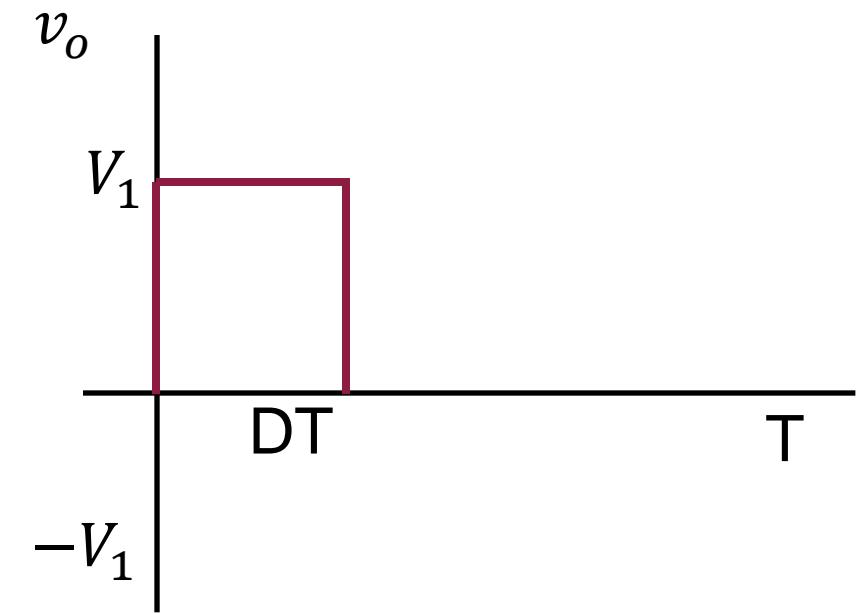
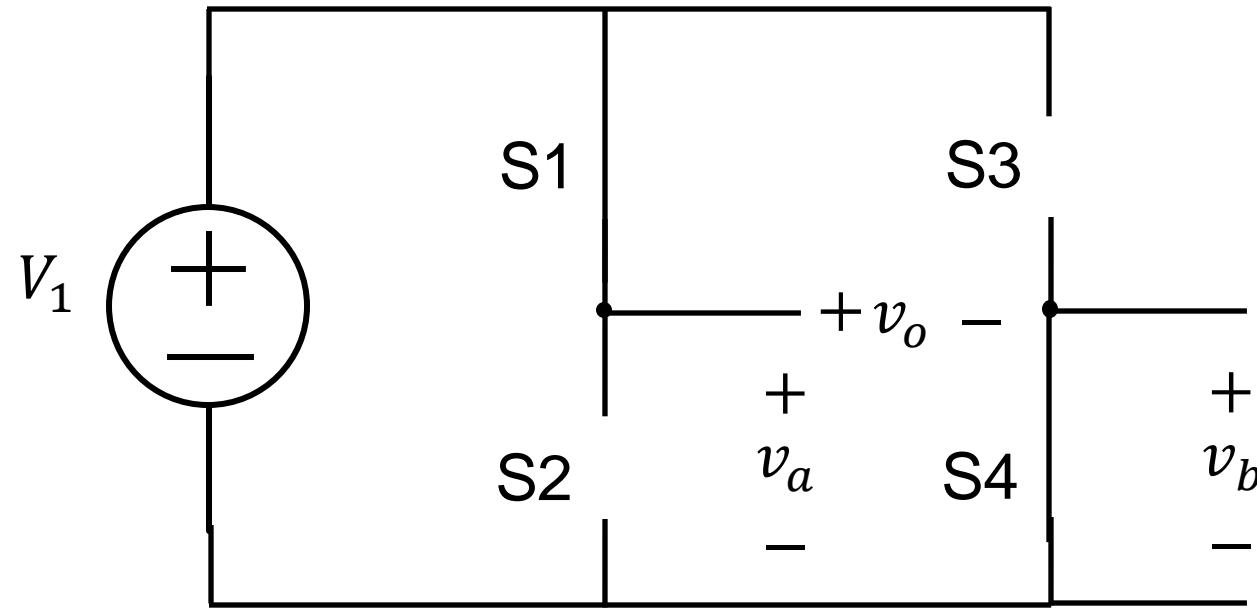
Half-Bridge Harmonics



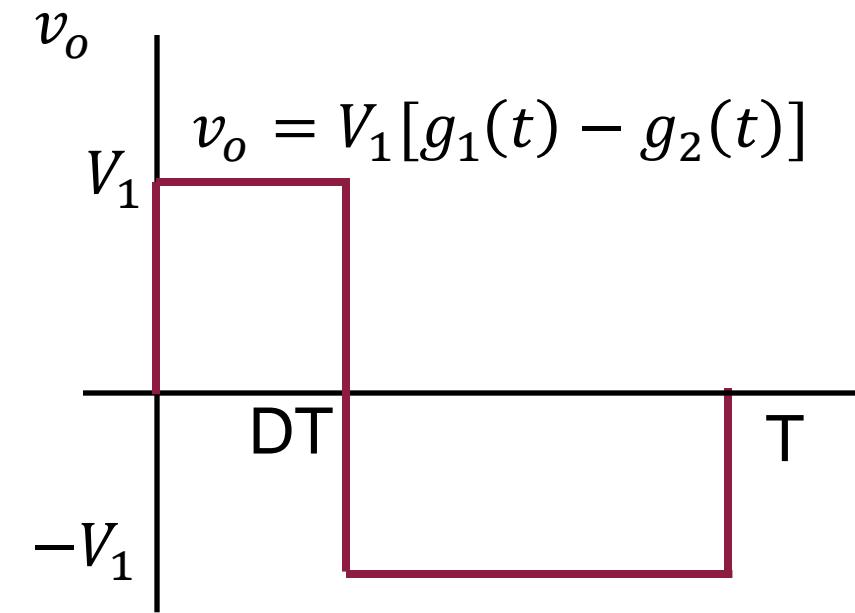
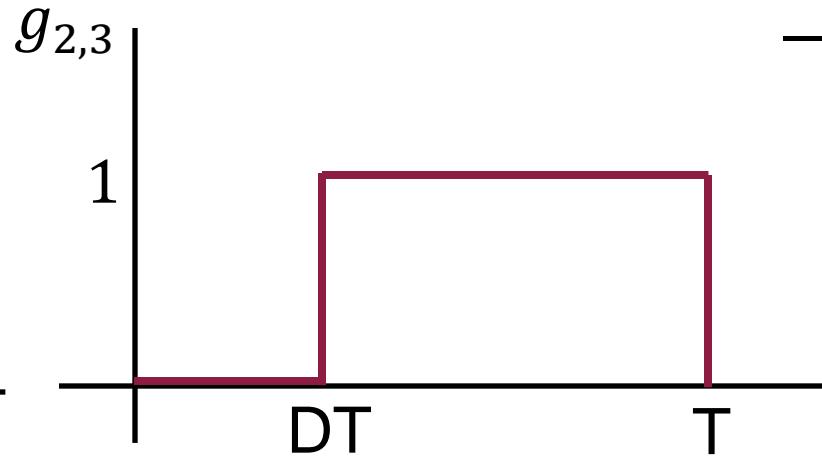
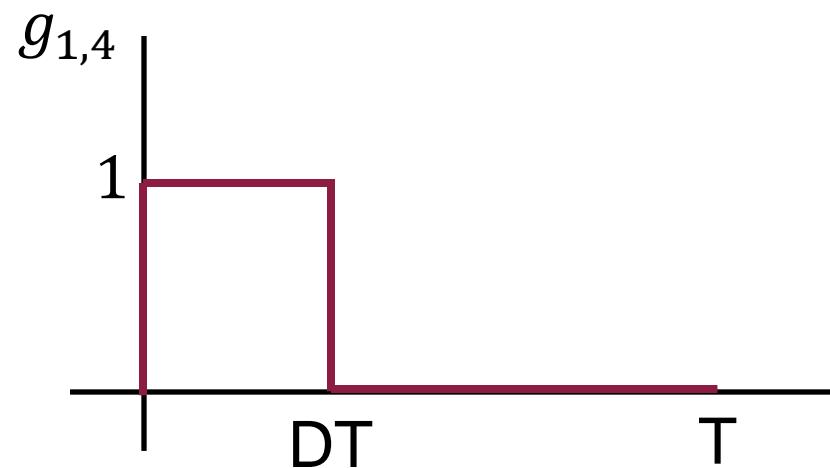
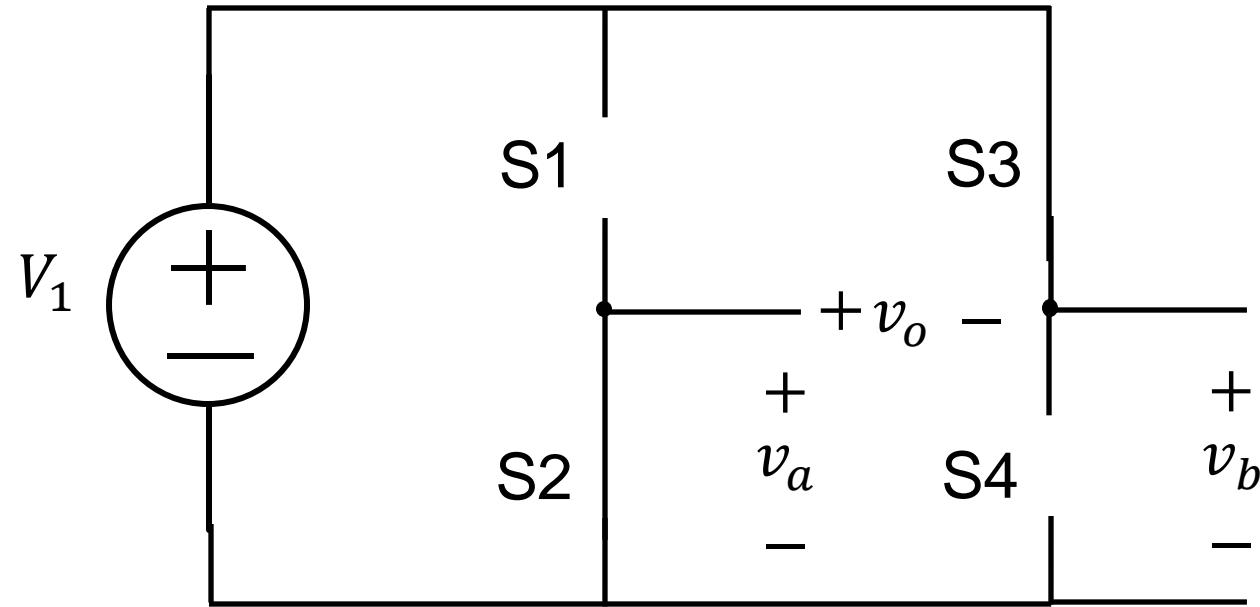
More Common: Full-Bridge Inverter



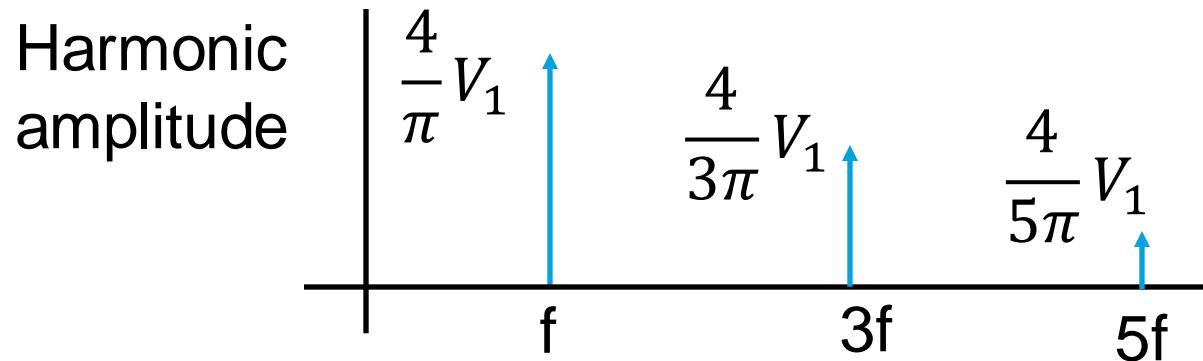
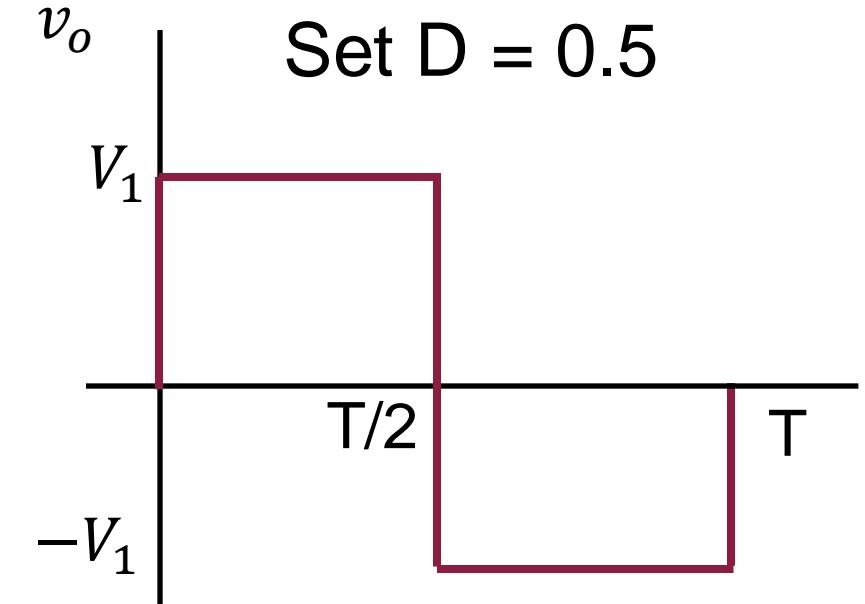
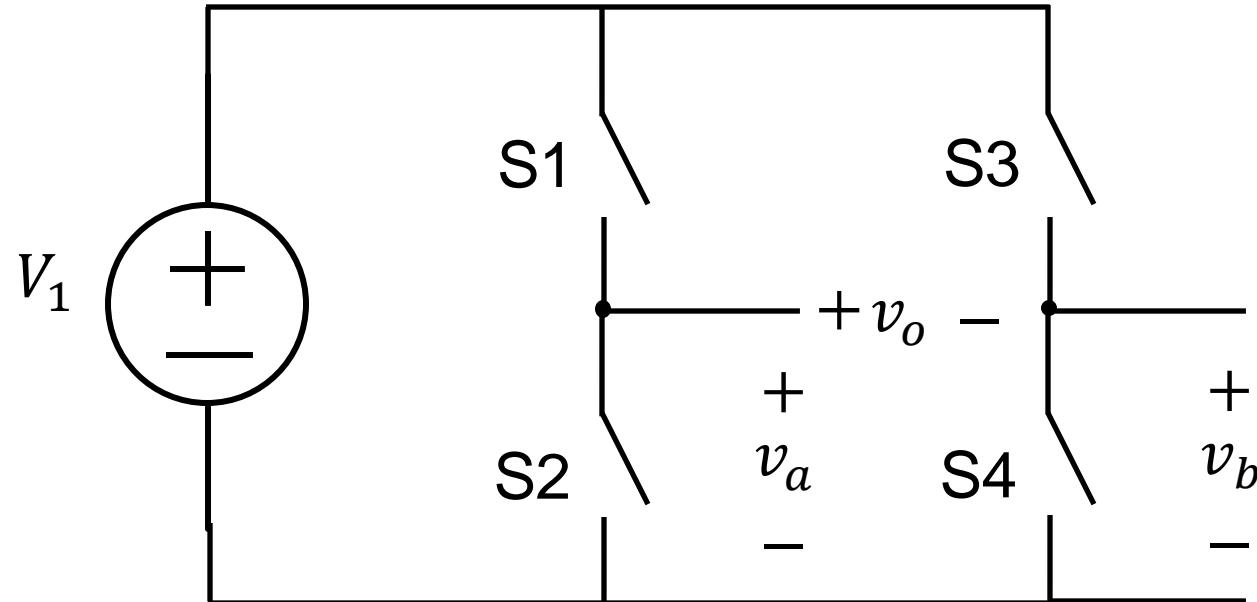
State 1: Positive Output Voltage



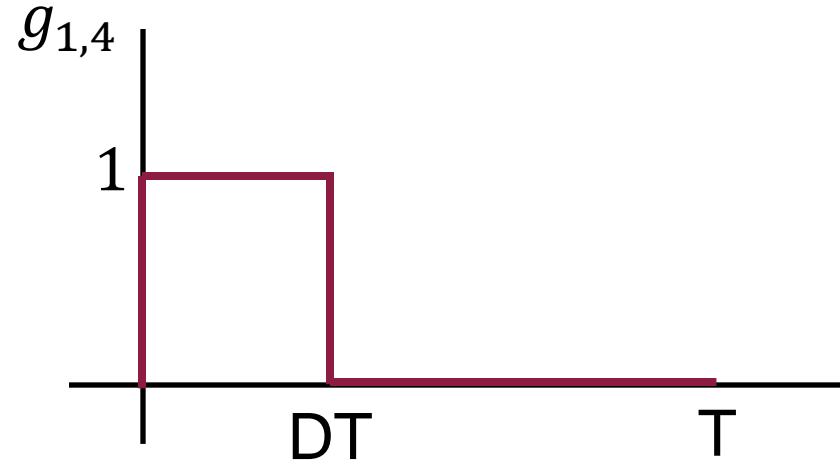
State 2: Negative Output Voltage



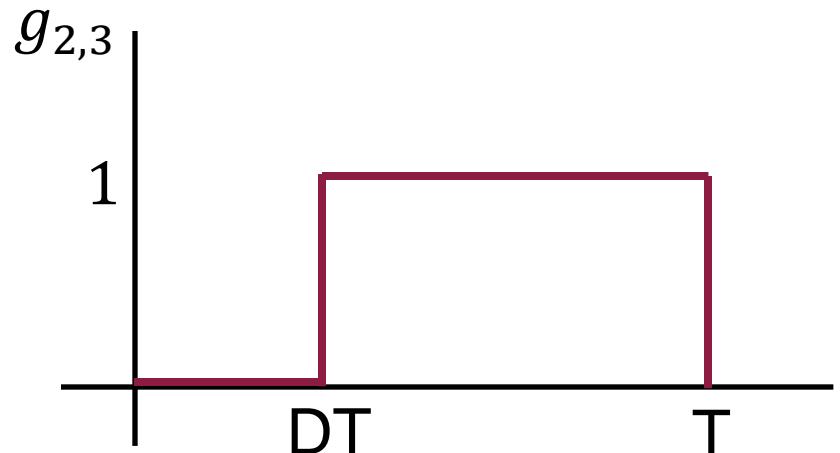
Simplest Operation: Square Wave



Interesting Duty Cycle Relationship



$$v_a = D + H.F. harmonics$$



$$v_b = 1 - D + H.F. harmonics$$

$$v_o = V_{dc}[2D - 1 + H.F. Harmonics]$$

Make “D” Vary Sinusoidally, Slowly

$$v_o = V_{dc}[(2D - 1) + H.F. Harmonics]$$

Set $D(t) = \frac{1}{2} + \frac{m_a}{2} \cos(2\pi f_o t + \phi)$

Choose $f_o \ll f_s$

Make “D” Vary Sinusoidally, Slowly

$$v_o = V_{dc}[(2D - 1) + H.F. Harmonics]$$

Set $D(t) = \frac{1}{2} + \frac{m_a}{2} \sin(2\pi f_o t + \phi)$

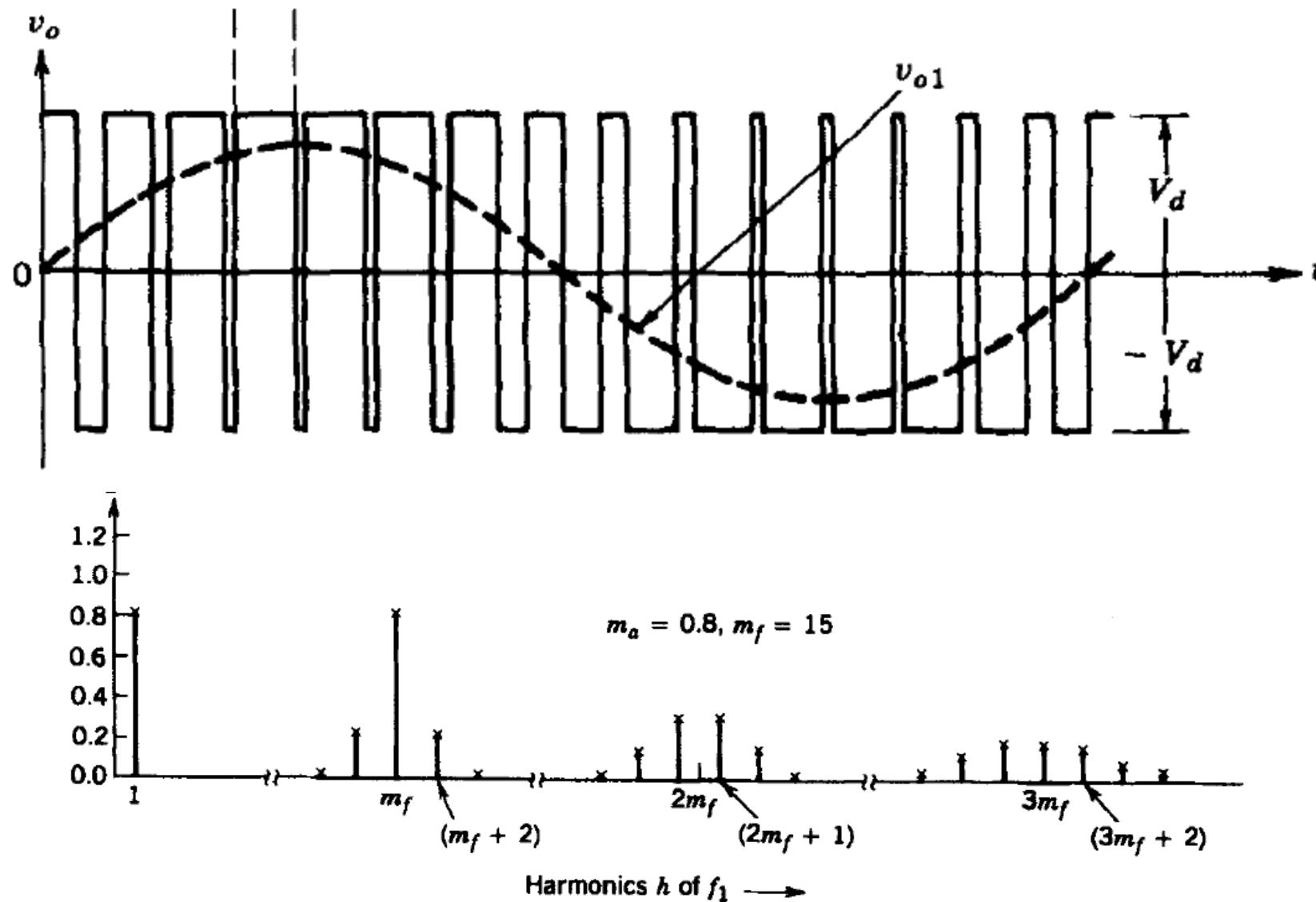
$$m_A \in [0,1]$$

Choose $f_o \ll f_s$

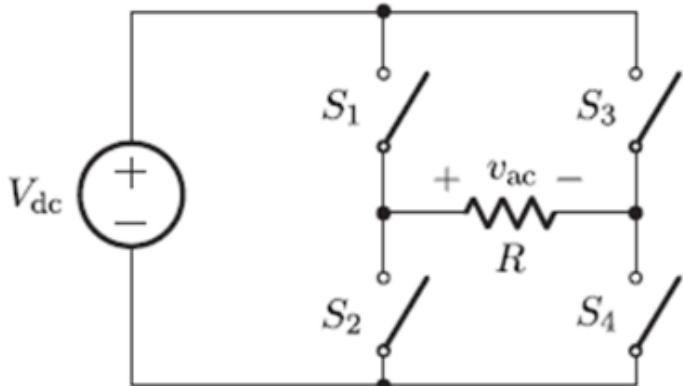
$$v_o = V_o m_a \sin(2\pi f_o t + \phi) + H.F. harmonics$$

Low frequency sinusoid

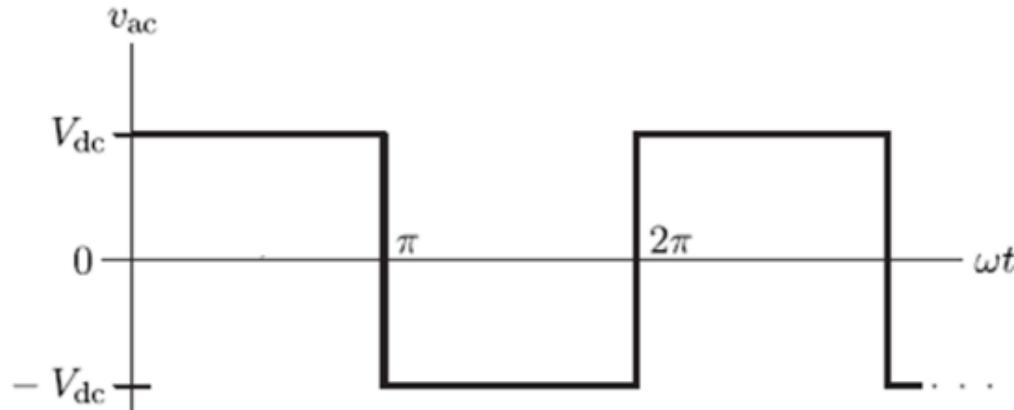
SPWM Waveform and Harmonics



Simpler Inverter Control

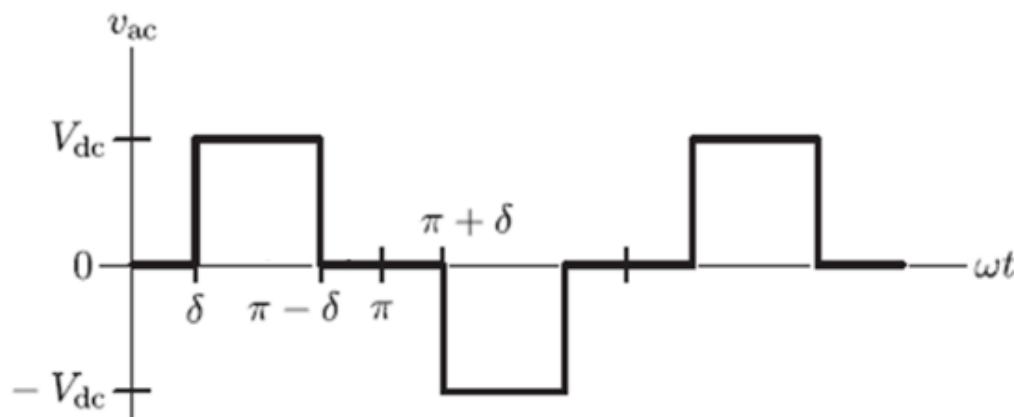


Full-bridge inverter



Square wave modulation

$$\frac{4V_{dc}}{\pi} \sin(\omega t)$$



“Voltage cancellation” modulation

$$\frac{4V_{dc}}{\pi} \cos \delta \sin(\omega t)$$

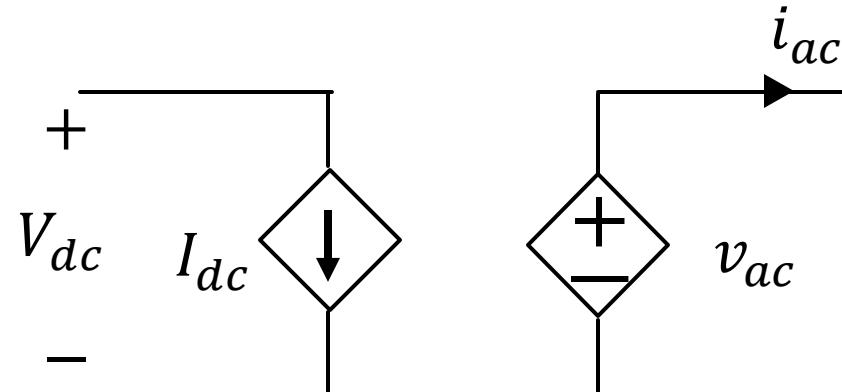
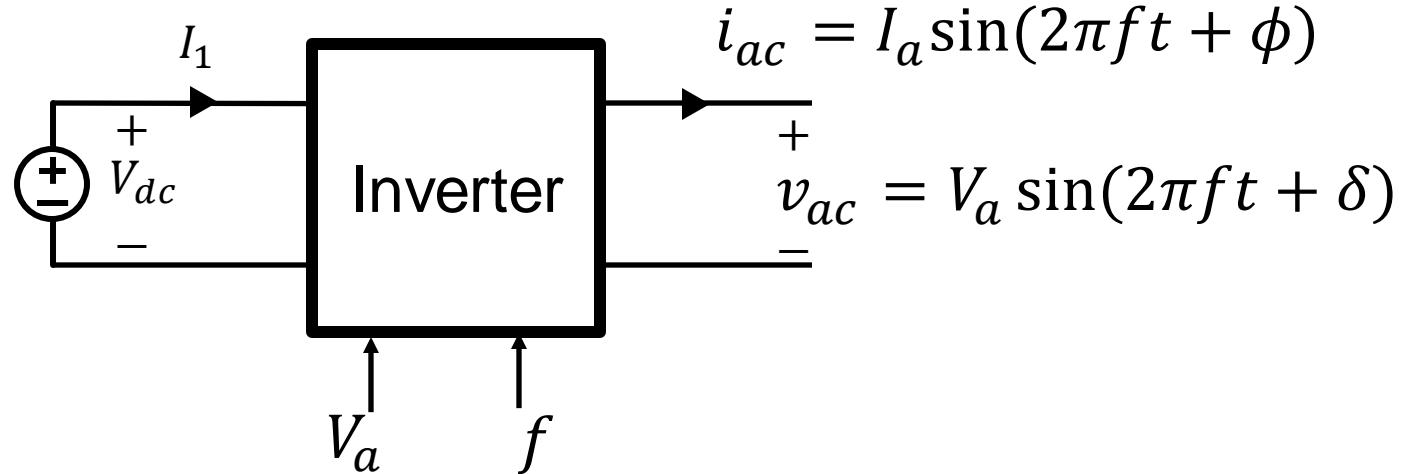
$\delta = 30^\circ$ eliminates all
“triple-n” harmonics

Averaged SPWM Inverter

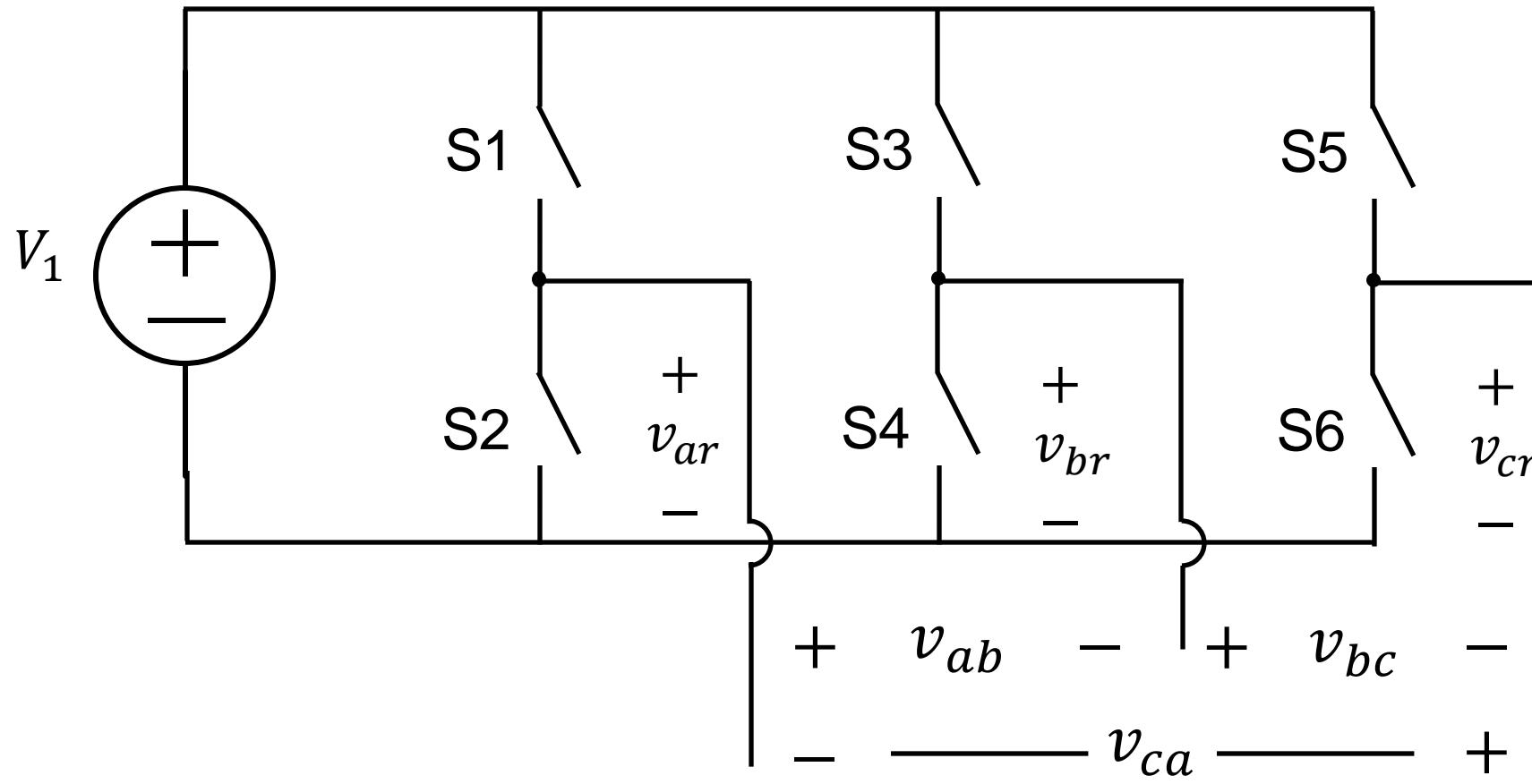
Power equivalent model

$$P_{in} = P_{out}$$

$$I_1 V_{dc} = \frac{V_a I_a}{2} \cos(\delta - \phi)$$



Three-Phase PWM Inverter



SPWM Operation

- Operate each half-bridge 120 degrees out-of-phase

S1:

$$D_1(t) = \frac{1}{2} + \frac{m_a}{2} \sin(2\pi ft)$$

S3:

$$D_3(t) = \frac{1}{2} + \frac{m_a}{2} \sin(2\pi ft + 120^\circ)$$

S5:

$$D_5(t) = \frac{1}{2} + \frac{m_a}{2} \sin(2\pi ft + 240^\circ)$$

SPWM Voltages

$$v_{ar} = \frac{V_{dc}}{2} + \frac{V_{dc}m_a}{2} \sin(2\pi ft) + H.F. harmonics$$

$$v_{br} = \frac{V_{dc}}{2} + \frac{V_{dc}m_a}{2} \sin(2\pi ft + 120^\circ) + H.F. harmonics$$

$$v_{cr} = \frac{V_{dc}}{2} + \frac{V_{dc}m_a}{2} \sin(2\pi ft + 240^\circ) + H.F. harmonics$$

Filtered SPWM Voltages

$$v_{ar} = \frac{V_{dc}}{2} + \frac{V_{dc}m_a}{2} \sin(2\pi ft) + H.F. \cancel{\text{harmonics}}$$

$$v_{br} = \frac{V_{dc}}{2} + \frac{V_{dc}m_a}{2} \sin(2\pi ft + 120^\circ) + H.F. \cancel{\text{harmonics}}$$

$$v_{cr} = \frac{V_{dc}}{2} + \frac{V_{dc}m_a}{2} \sin(2\pi ft + 240^\circ) + H.F. \cancel{\text{harmonics}}$$

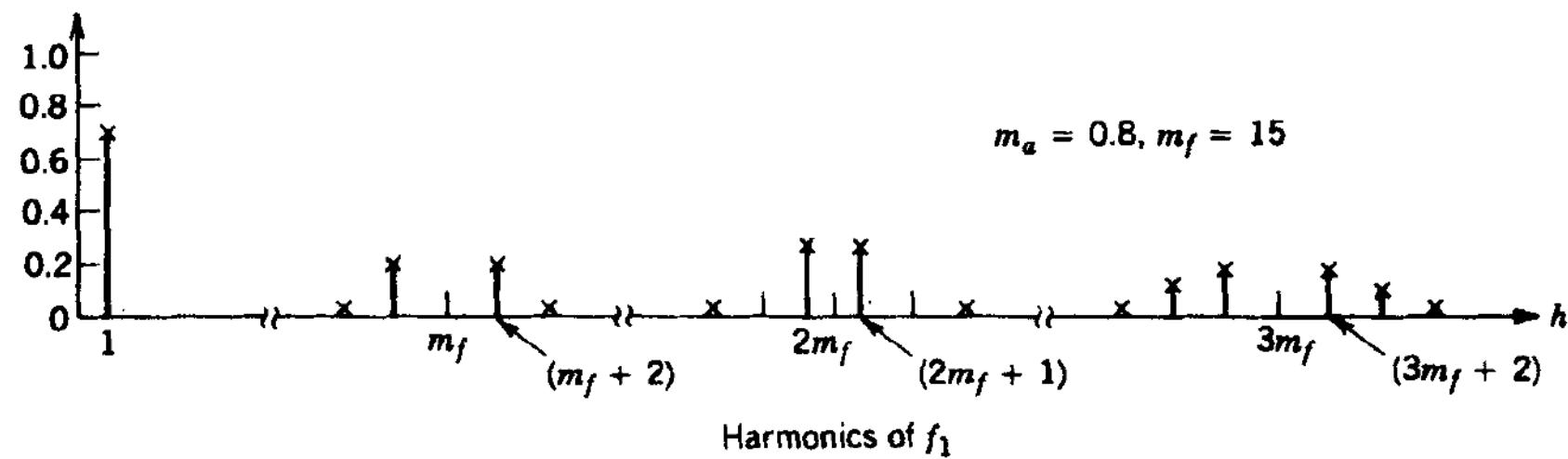
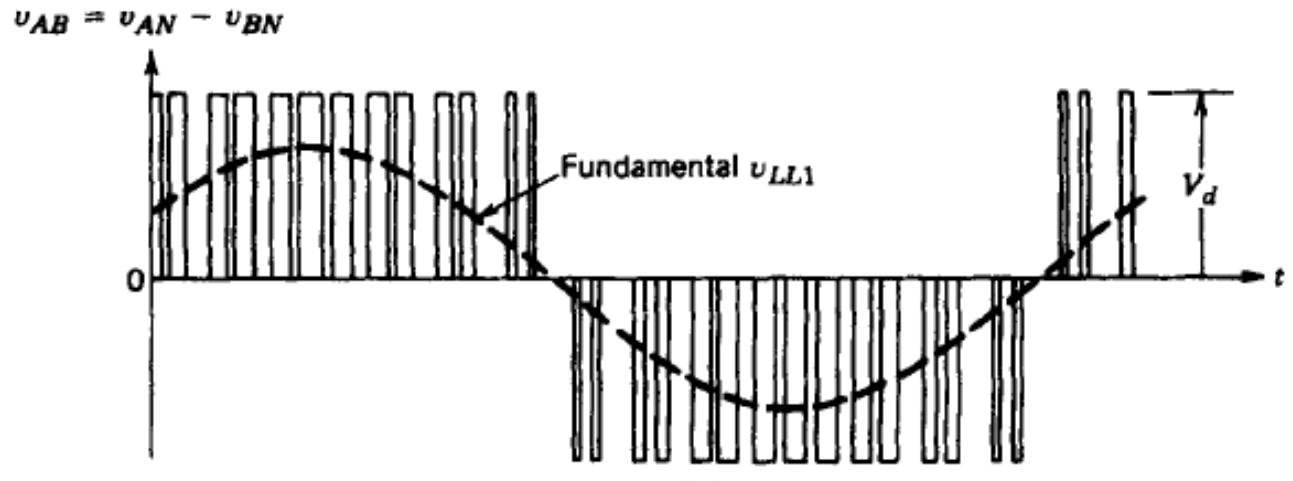
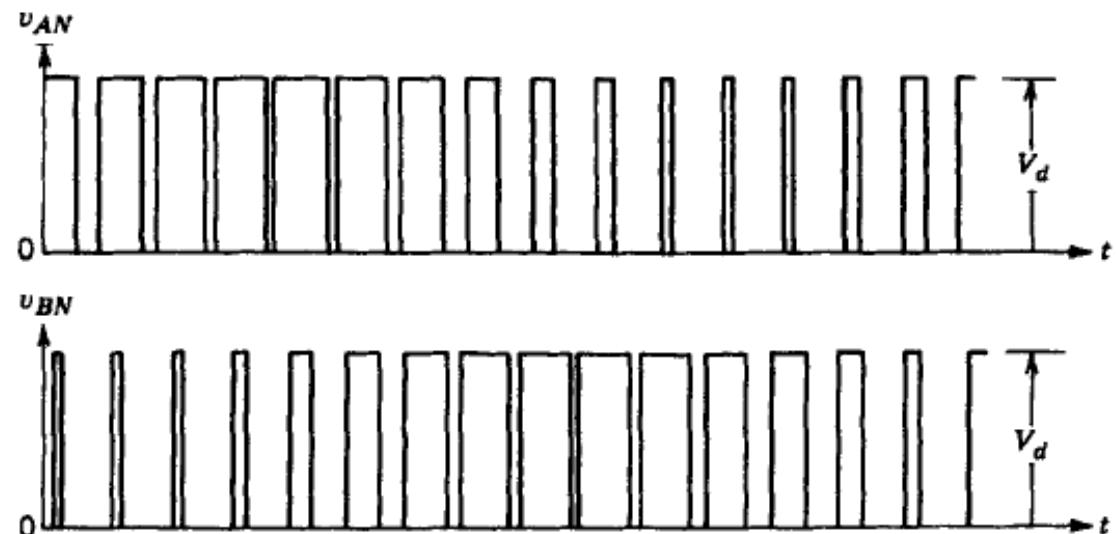
Filtered line-line voltages

$$v_{ab} = \frac{\sqrt{3}V_{dc}m_a}{2} \sin(2\pi ft + 30^\circ)$$

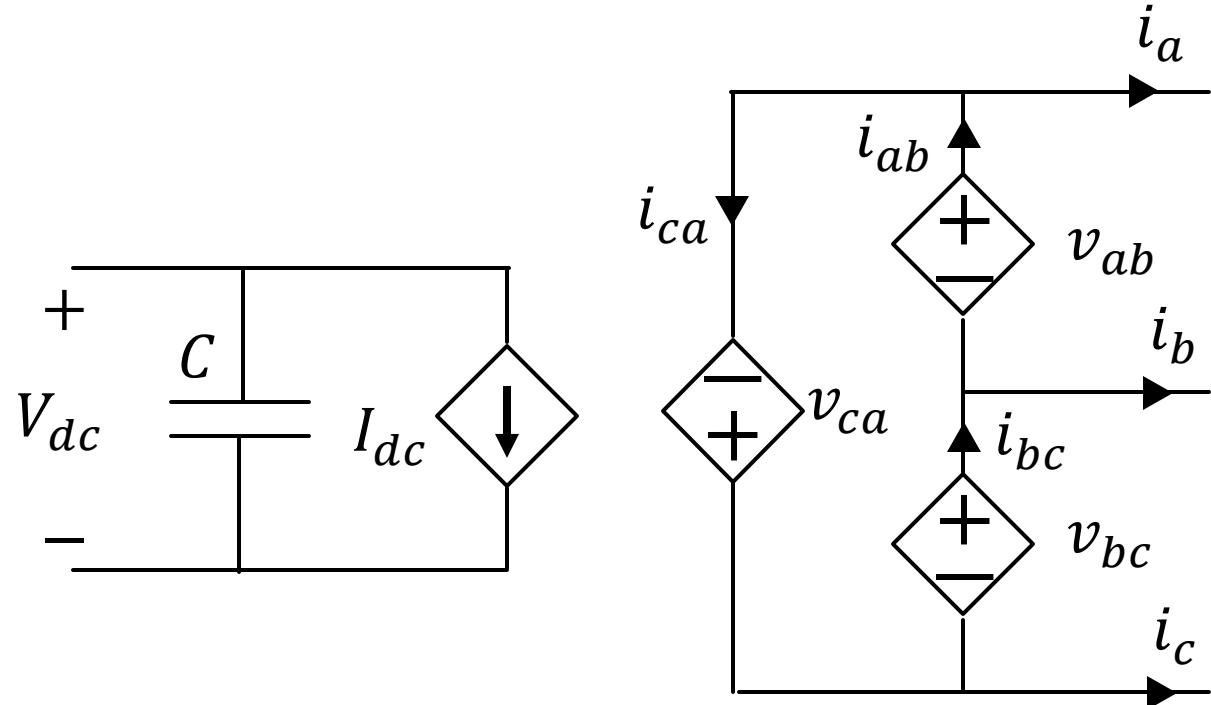
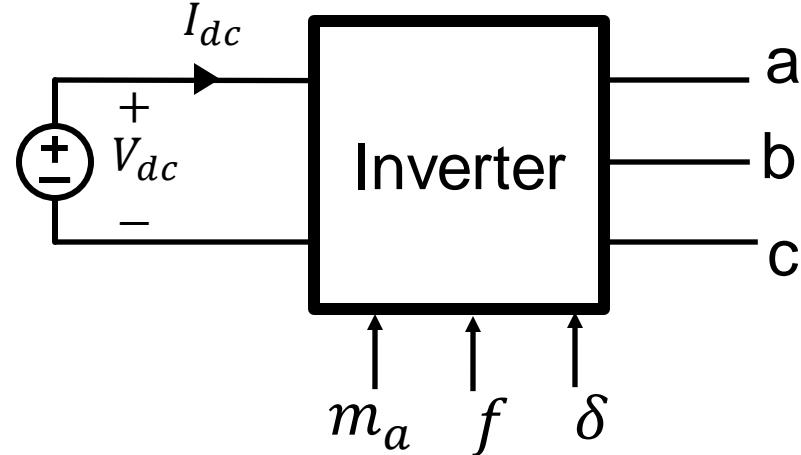
$$v_{bc} = \frac{\sqrt{3}V_{dc}m_a}{2} \sin(2\pi ft - 90^\circ)$$

$$v_{ca} = \frac{\sqrt{3}V_{dc}m_a}{2} \sin(2\pi ft - 210^\circ)$$

Waveforms and Harmonics



Averaged SPWM Three-Phase Inverter



Enforce power balance

$$P_{in} = P_{out}$$

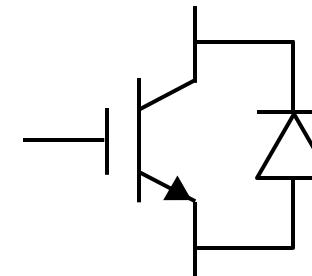
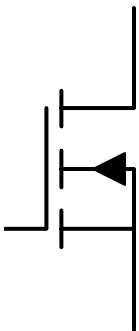
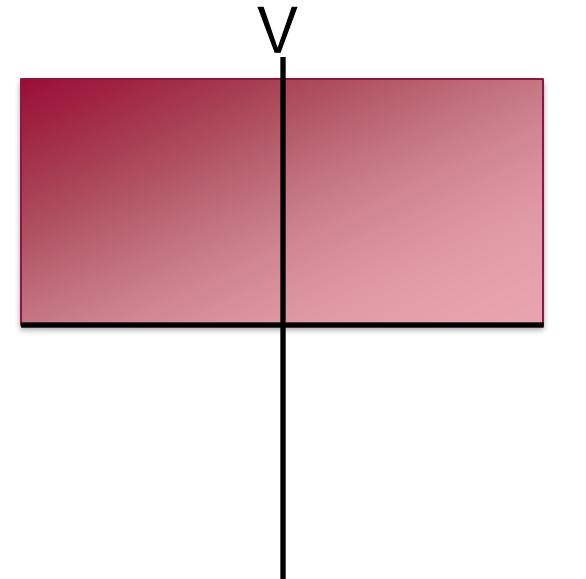
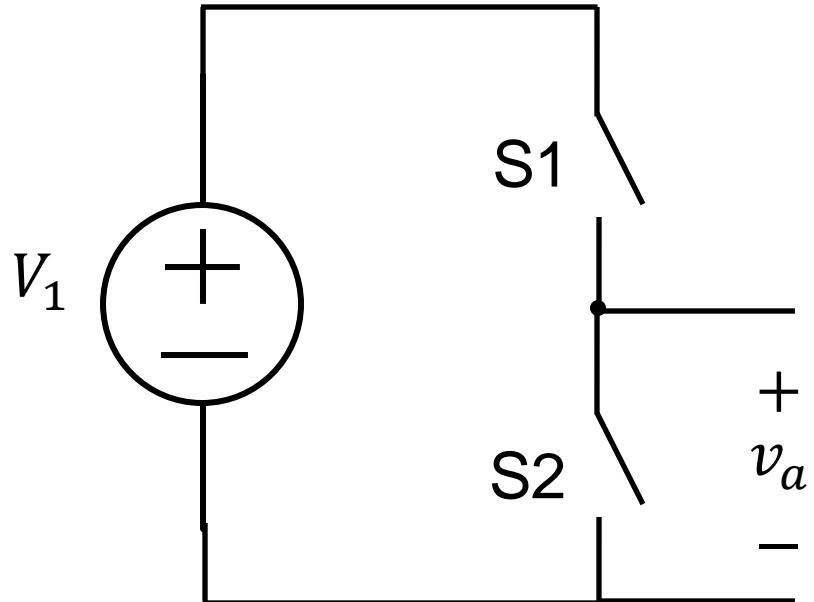
$$I_{dc}V_{dc} = P_{ac}$$

$$v_{ab} = \frac{\sqrt{3}V_{dc}m_a}{2} \sin(2\pi ft + 30^\circ + \delta)$$

$$v_{bc} = \frac{\sqrt{3}V_{dc}m_a}{2} \sin(2\pi ft - 90^\circ + \delta)$$

$$v_{ca} = \frac{\sqrt{3}V_{dc}m_a}{2} \sin(2\pi ft - 210^\circ + \delta)$$

Switches: IGBTs or MOSFETs



Conclusion

- The half-bridge is a key inverter component
- A single-phase full-bridge converter comprises two half-bridges
- Three-phase inverter comprises three half-bridges
- Averaged models allow us to more simply analyze inverter at the system-level
- Higher power inverters switch at lower frequencies (e.g. 100MW, 5kHz vs. 100W, 1MHz owing to switch limitations)