

# **Market Participation of Energy Storage and DER Aggregators: Energy Arbitrage, Retail Market Design, and Electricity Price Forecasting**

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# Acknowledgements

## ▶▶ PSERC Support

- **M-41 [Ongoing]:** The Stacked Value of Battery Energy Storage Systems (BESSs)
- **M-42 [Starting Soon]:** Modeling and Coordinating DERs in Power Systems and Markets

## ▶▶ ASU Students



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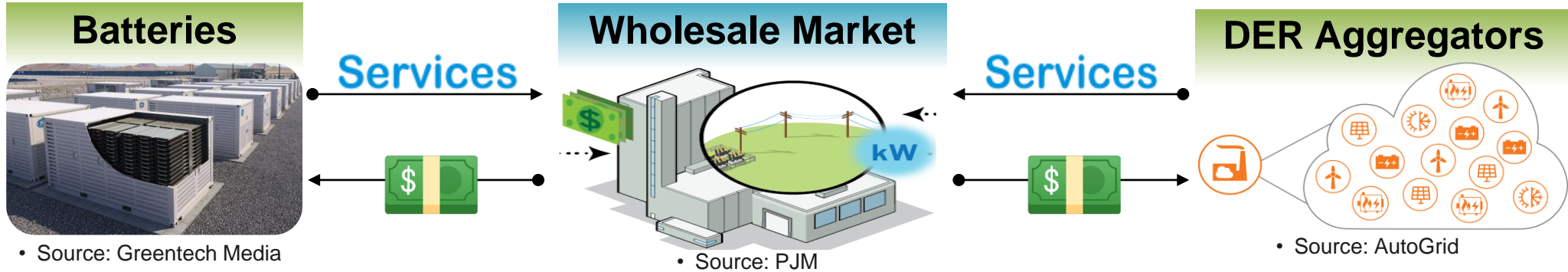
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Market Design + DER Aggregators

# Challenges & Opportunities



## ➡ Market Operation

- Energy arbitrage behavior of batteries?
- Batteries' impact on market operation?
- Coordinate T&D, DER aggregators, and DERs?

## ➡ Market Participation

- Market bidding/offering strategies?
- Forecast Electricity price?
- Offer multiple services?

# Proposed Solutions

1

## *Market + Batteries:*

**Optimal Battery Participation in Energy & Ancillary Services Markets**

2

## *Market + DER Aggregators:*

**A DSO Design for Wholesale & Retail Markets with DER Aggregators**

3

## *Market Participation:*

**Machine Learning for System-Wide Electricity Price Forecasting**

# Proposed Solutions

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Machine Learning for System-Wide Electricity Price Forecasting

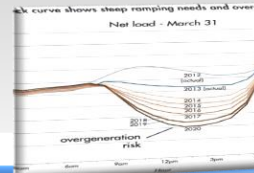
# Background & Motivation

❖ Understand the role of **utility-scale batteries** in daily system operations and economics



## Sustainability

- CO<sub>2</sub> Reduction
- Renewables



## Policy

- FERC Order 841
- BESS → Markets



## Technology

- BESS: fast ramping, multiple services

# Background & Motivation

## ►► The Role of Utility-Scale Batteries in System Operations & Economics

- The impact of utility-scale batteries on daily market operations
- Utility-scale batteries' capability of multiple services provision (energy arbitrage, spinning reserve, frequency regulation services, etc.)
- Operating patterns of merchant batteries in energy, reserve, and pay-as-performance regulation markets
- Interaction between battery owner's profit maximization strategies and system operator's joint operating cost minimization activities (via the market clearing process)



## ►► Bi-Level Optimization: Battery Owner & System Operator

# Problem Formulation: Bi-Level Optimization Framework

## Upper-Level Problem – BESS Profit Maximization

$$\max \sum_{t=1}^{\text{Time}} \left\{ Rev_t^{RT-E} + Rev_t^{RT-Rs} + Rev_t^{RT-Rg,C} + Rev_t^{RT-Rg,M} \right\} \Delta t$$

s. t. BESS output power limits

BESS state of charge (SOC) limits

BESS's Quantity  
and Price Bids

Real-Time Market Clearing  
Prices and Power Dispatched

## Lower Level Problem – ISO Joint Market Clearing

$$\min \sum_{t=1}^{\text{Time}} \left( \sum_g \left[ Cost_t^{GE} + Cost_t^{GRs} + Cost_t^{GRg,C} + Cost_t^{GRg,M} \right] + \left[ Cost_t^{BE} + Cost_t^{BRs} + Cost_t^{BRg,C} + Cost_t^{BRg,M} \right] \right) \Delta t$$

s. t. Operational limits of conventional generators

Operational limits of battery energy storage

Pay-as-performance regulation market constraints

System-wide reserve and regulation requirements

Power balance at each bus

- **Upper-level Problem:** Battery owner's profit maximization from real-time energy, reserve, and pay-as-performance regulation markets

- **Lower-level Problem:** System operator's joint market clearing process for real-time energy, reserve, and pay-as-performance regulation markets



# The Upper-Level Problem

$$\max \sum_{t \in T} \sum_{i \in B} \left[ \pi_{i,t}^E (P_{i,t}^{B,S} - P_{i,t}^{B,D}) + \pi_t^{Rs} P_{i,t}^{B,Rs} + \pi_t^{RgC} P_{i,t}^{B,RgC} + \pi_t^{RgM} P_{i,t}^{B,RgM} \right] \Delta t$$

- **Upper-Level Objective:** Battery owner's profit maximization from real-time energy, reserve, and pay-as-performance regulation markets

Subject to:

$$0 \leq Q_{i,t}^{E,S} \leq u_i P_i^{Rate}$$

$$0 \leq Q_{i,t}^{E,D} \leq (1 - u_i) P_i^{Rate}$$

$$0 \leq Q_{i,t}^{Rs} \leq P_i^{Rate}$$

$$0 \leq Q_{i,t}^{RgC} \leq P_i^{Rate}$$

$$-P_i^{Rate} + P_{i,t}^{B,RgC} \leq P_{i,t}^{B,D} - P_{i,t}^{B,S} - P_{i,t}^{B,Rs} \leq P_i^{Rate} - P_{i,t}^{B,RgC}$$

$$SOC_{i,t} = SOC_i^{Init} + \sum_{k=1}^t (P_{i,k}^{B,S} - P_{i,k}^{B,D}) \Delta t$$

$$SOC_i^{Min} + (P_{i,t}^{B,Rs} + P_{i,t}^{B,RgC}) \Delta t \leq SOC_{i,t} \leq SOC_i^{Max} - P_{i,t}^{B,RgC} \Delta t$$

- **Constraints-1:** Battery output power limits

- **Constraints-2:** Battery state of charge (SOC) limits

# The Lower-Level Problem

$$\max \sum_{t \in T} \left( \sum_{j \in G} \left[ \alpha_{j,t}^{E,S} P_{j,t}^{G,S} + \alpha_{j,t}^{Rs} P_{j,t}^{G,Rs} + \alpha_{j,t}^{RgC} P_{j,t}^{G,RgC} + \alpha_{j,t}^{RgM} P_{j,t}^{G,RgM} \right] + \sum_{i \in B} \left[ \beta_{i,t}^{E,S} P_{i,t}^{B,S} - \beta_{i,t}^{E,D} P_{i,t}^{B,D} + \beta_{i,t}^{Rs} P_{i,t}^{B,Rs} + \beta_{i,t}^{RgC} P_{i,t}^{B,RgC} + \beta_{i,t}^{RgM} P_{i,t}^{B,RgM} \right] \right) \Delta t$$

Subject to:

$$\begin{aligned} 0 &\leq P_{i,t}^{B,S} \leq Q_{i,t}^{E,S} \\ 0 &\leq P_{i,t}^{B,D} \leq Q_{i,t}^{E,D} \\ 0 &\leq P_{i,t}^{B,Rs} \leq Q_{i,t}^{Rs} \\ 0 &\leq P_{i,t}^{B,RgC} \leq Q_{i,t}^{RgC} \end{aligned}$$

$$\begin{aligned} P_j^{Min} + P_{j,t}^{G,RgC} &\leq P_{j,t}^{G,S} \leq P_j^{Max} - P_{j,t}^{G,Rs} - P_{j,t}^{G,RgC} \\ 0 &\leq P_{j,t}^{G,Rs} \leq P_j^{Rs,ramp} \\ 0 &\leq P_{j,t}^{G,RgC} \leq P_j^{Rg,ramp} \end{aligned}$$

- **Lower-Level Objective:** System operator's joint market clearing process for real-time energy, reserve, and pay-as-performance regulation markets

- **Constraints-1:** Operating limits of batteries

- **Constraints-2:** Operating limits of generators

# The Lower-Level Problem

$$\max \sum_{t \in T} \left( \sum_{j \in G} \left[ \alpha_{j,t}^{E,S} P_{j,t}^{G,S} + \alpha_{j,t}^{Rs} P_{j,t}^{G,Rs} + \alpha_{j,t}^{RgC} P_{j,t}^{G,RgC} + \alpha_{j,t}^{RgM} P_{j,t}^{G,RgM} \right] + \sum_{i \in B} \left[ \beta_{i,t}^{E,S} P_{i,t}^{B,S} - \beta_{i,t}^{E,D} P_{i,t}^{B,D} + \beta_{i,t}^{Rs} P_{i,t}^{B,Rs} + \beta_{i,t}^{RgC} P_{i,t}^{B,RgC} + \beta_{i,t}^{RgM} P_{i,t}^{B,RgM} \right] \right) \Delta t$$

Subject to:

$$P_{j,t}^{G,RgC} \leq P_{j,t}^{G,RgM} \leq m_j P_{j,t}^{G,RgC}$$

$$P_{i,t}^{B,RgC} \leq P_{i,t}^{B,RgM} \leq m_i P_{i,t}^{B,RgC}$$

$$\sum_{i \in B} P_{i,t}^{B,Rs} + \sum_{j \in G} P_{j,t}^{G,Rs} \geq R_t^{Rs}$$

$$\sum_{i \in B} P_{i,t}^{B,RgC} + \sum_{j \in G} P_{j,t}^{G,RgC} \geq R_t^{RgC}$$

$$\sum_{i \in B} P_{i,t}^{B,RgM} + \sum_{j \in G} P_{j,t}^{G,RgM} \geq R_t^{RgM}$$

$$\sum_{i \in B} (P_{i,t}^{B,S} - P_{i,t}^{B,D}) + \sum_{j \in G} P_{j,t}^{G,S} = P_t^{Load}$$

- **Lower-Level Objective:** System operator's joint market clearing process for real-time energy, reserve, and pay-as-performance regulation markets

- **Constraints-3:** Operating constraints of pay-as-performance regulation markets

- **Constraints-4:** System-wide reserve and regulation requirements

- **Constraints-5:** System power balance

# Solution Procedure

## ► Convert Bi-Level Problem to Single-Level Problem

- Lower-level problem: linear and convex
- Solve lower-level problem via solving the KKT equations of the lower-level problem
- Write KKT conditions of the Lower-level problem as constraints for the upper-level problem

### Single-Level Problem after Conversion

$$\max \sum_{t \in T} \sum_{i \in B} \left[ \pi_{i,t}^E (P_{i,t}^{B,S} - P_{i,t}^{B,D}) + \pi_t^{Rs} P_{i,t}^{B,Rs} + \pi_t^{RgC} P_{i,t}^{B,RgC} + \pi_t^{RgM} P_{i,t}^{B,RgM} \right] \Delta t$$

*s. t.* Battery power output limits

Battery state of charge (SOC) limits

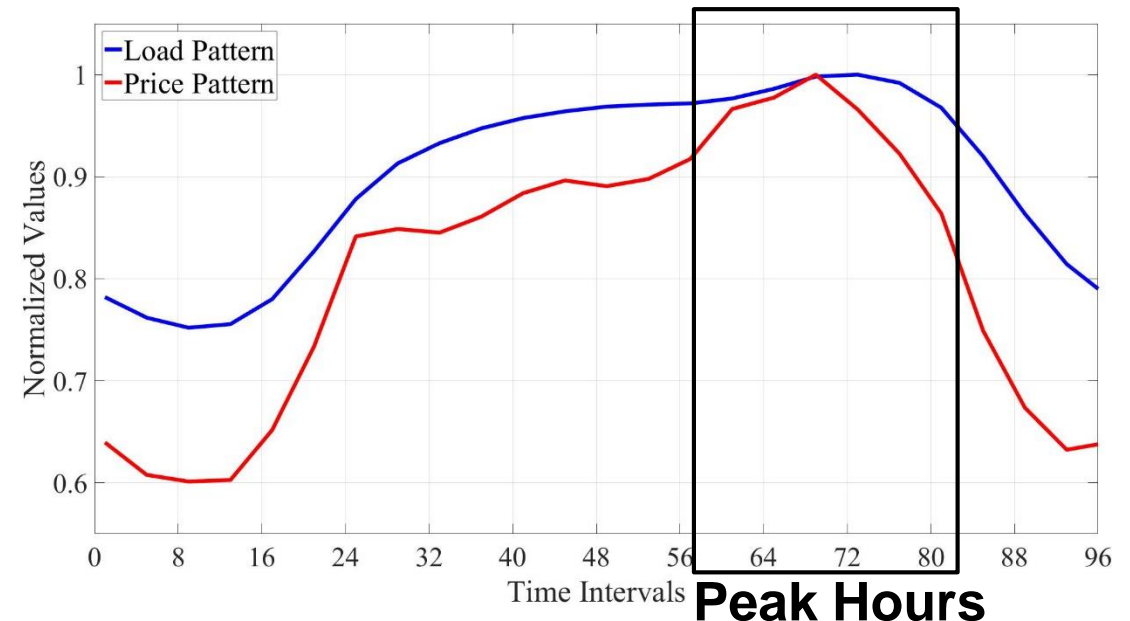
} Original Constraints of  
Upper-Level Problem

**KKT conditions of the lower-level problem**

# Case Study: Test System

- **Modified PJM 5-bus test system (Market clearing interval = 15 min; Simulation time = 24 hours)**
- BESS Capacity: 400<sup>MWh</sup> ; BESS Output Power limit: 40<sup>MW</sup>
- System's Load: 1000<sup>MW</sup> mapped on 2018 PJM load pattern
- System's Spinning Reserve Requirements: 10% of load in each interval
- System's Regulation Capacity Requirements: 4% of load in each interval
- System's Regulation Mileage Requirements: 1.75 times regulation capacity requirements

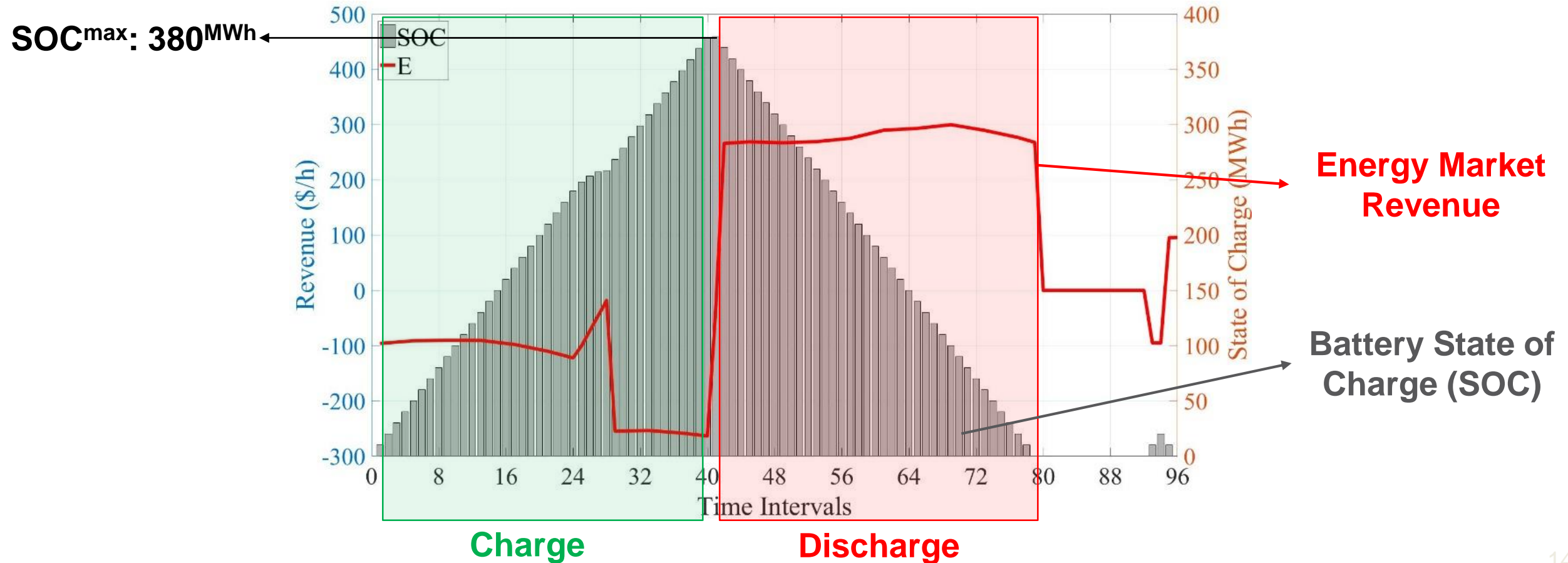
Generator No.	Base Price Bid (\$/MWh)	$p_{\max}$ (MW)	$p_{Rg,ramp}$ (MW)	$p_{Rs,ramp}$ (MW)
G1	10	400	80	40
G2	14	300	60	30
G3	15	210	42	21
G4	30	350	70	35
G5	40	270	54	27



# Case Study Results

## ► [Case 1] Modeling Energy Market Only

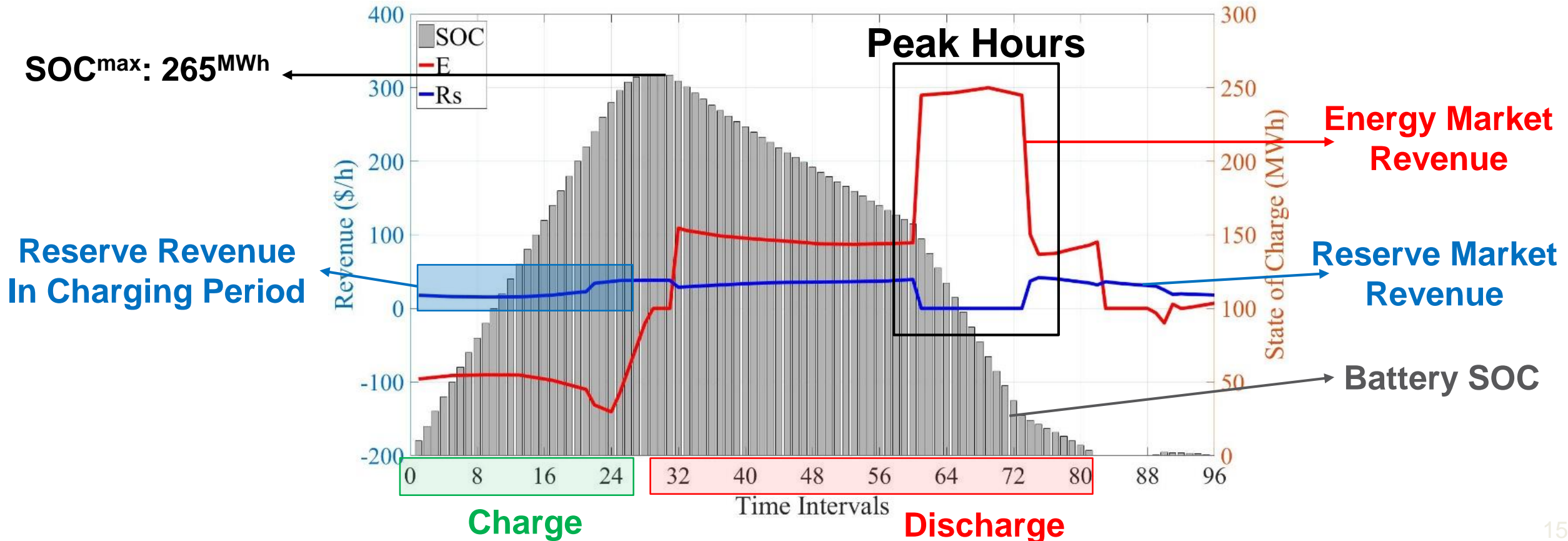
- Energy arbitrage between different market clearing intervals



# Case Study Results

## ►► [Case 2] Modeling Energy & Reserve Markets

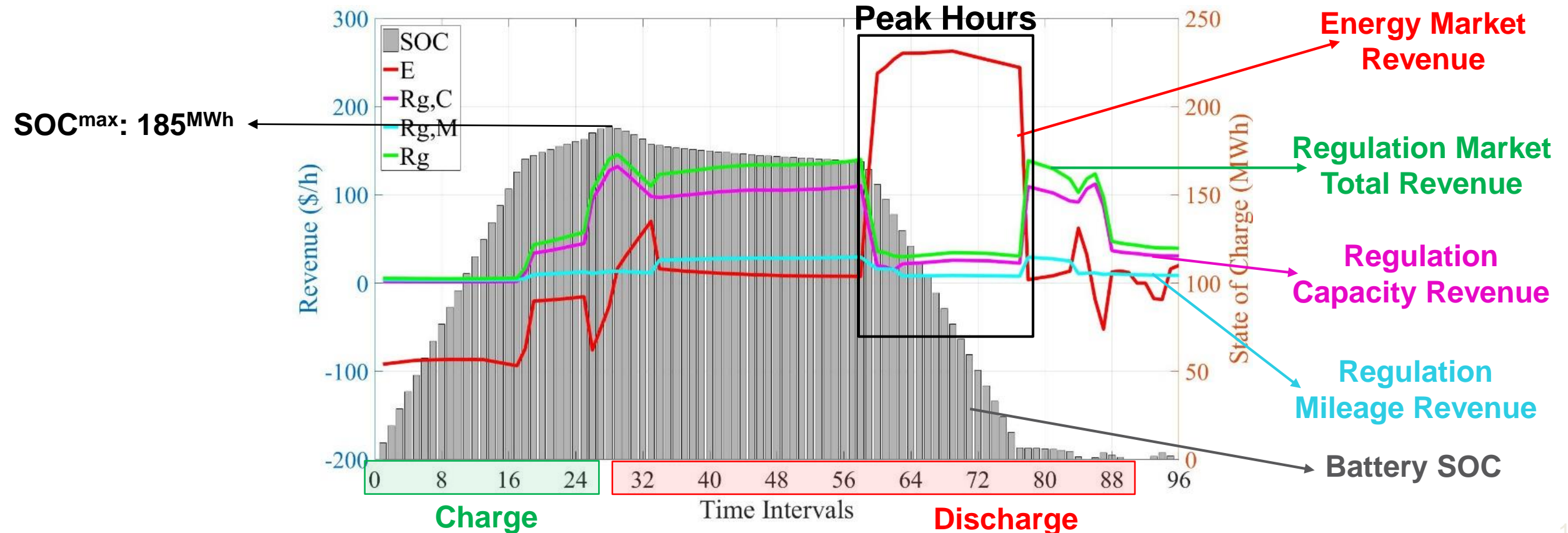
- Energy arbitrage between different market clearing intervals & between different markets
- Energy arbitrage between different markets at the same market clearing interval (during charging period)
- Lower state of charge (SOC) compared to Case 1 (with energy market only)



# Case Study Results

## ► [Case 3] Modeling Energy & Regulation Markets

- Energy arbitrage between different market clearing intervals & between different markets
- Less revenue from the energy market

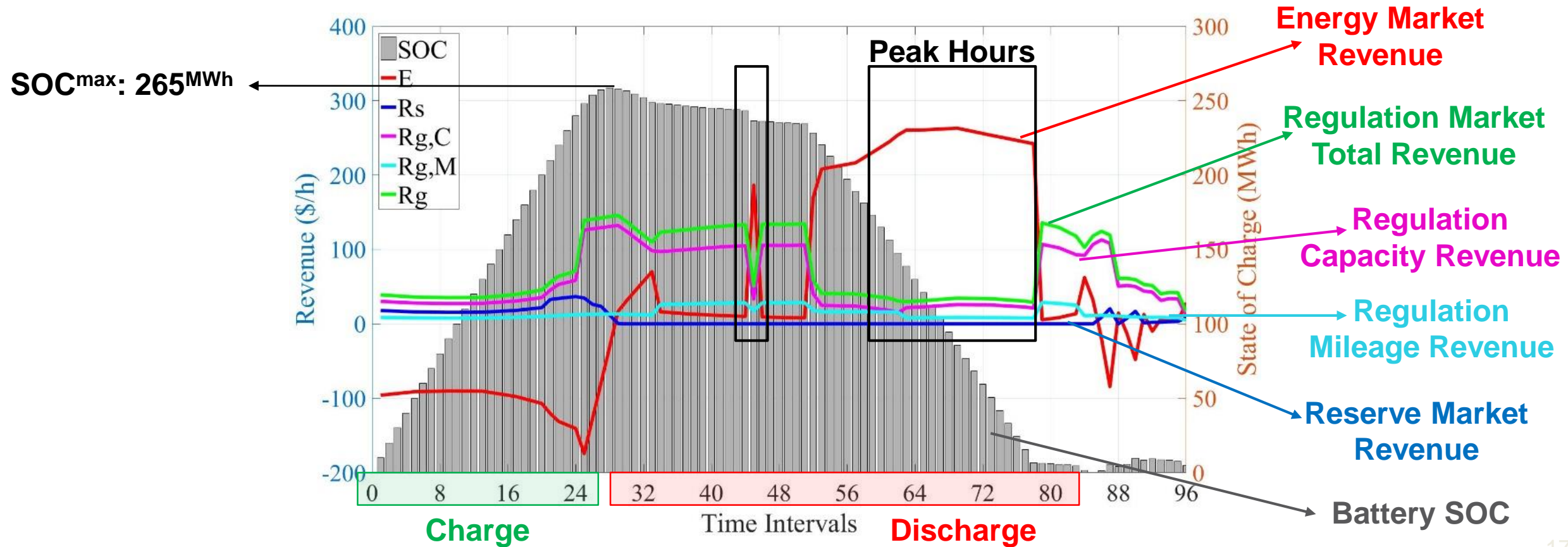




# Case Study Results

## ►► [Case 4] Modeling Energy, Reserve, & Regulation Markets

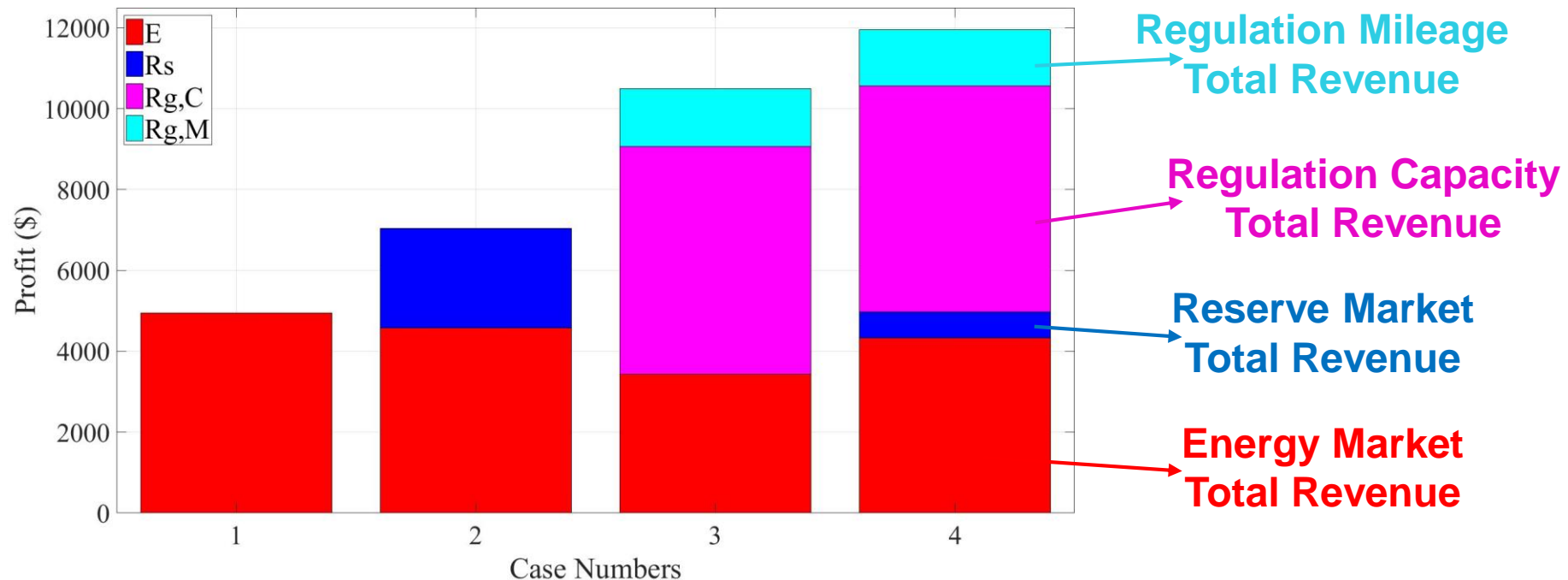
- Energy arbitrage between different market clearing intervals & between different markets
- Battery collects the least revenue from reserve market
- Significant difference in battery revenue patterns and market outcomes



# Case Study Results

## ►► [Cases 1~4] Comparison of Battery Total Revenue

- Regulation market is the most profitable
- Gain more profit by participating in more markets
- Participating in reserve increases the revenue from energy market (Cases 3~4)



# Part I: Conclusions & Future Directions

## ➡ Conclusions

- **A bi-level optimization framework:**
  - ✓ Operating and revenue patterns of merchant batteries in energy, reserve, and regulation markets
  - ✓ Interactions between battery owner's profit maximization strategies and system operator's joint market clearing process

## ➡ Future Directions

- **Incorporate more operating details in the bi-level optimization framework:**
  - ✓ AGC signal deployment
  - ✓ Battery degradation cost
  - ✓ Transmission system model
  - ✓ Battery charge/discharge efficiency, etc.

# Proposed Solutions

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# Background & Motivation

## ➡ Impact of DER Aggregators on T&D Operations

- **DER aggregators:** control distribution-level DERs/loads + participate in transmission-level markets
- **Distribution operations:** cannot monitor DER aggregators' controls over DERs/loads → **security risks**
- **Wholesale markets:** cannot observe DER locations/availabilities in distribution grids → **market uncertainties**



## ➡ Need an **Entity** to Coordinate DER Aggregators in T&D Operations

- **This entity can:**
  - ✓ Observe DER locations/availabilities in distribution grids
  - ✓ Monitor DER aggregators' controls over distribution-level DERs/loads
  - ✓ Coordinate DER aggregators' offers to wholesale markets

# Background & Motivation

►► Need an **Entity** to Coordinate DER Aggregators in T&D Operations



►► Distribution System Operator (**DSO**) Framework

- Operate the retail market + distribution system
- Coordinate DER aggregators' participation in day-ahead wholesale energy + pay-as-performance regulation markets and retail energy markets
- Collect offers from DER aggregators to operate the retail market, and coordinate these offers to construct an aggregated offer/bid for participating in the day-ahead wholesale market
- Consider distribution network security while coordinating DER aggregators' wholesale market participation
- Consider various types of aggregators (for demand response resources, energy storage, EV charging stations, and dispatchable DGs)

# Proposed DSO Framework

## DSO Problem Formulation

$$\min \sum_{t \in T} [\text{Total DSO Operating Cost}] \longleftrightarrow \text{Maximize total social welfare in the distribution grid}$$

- s. t.* Operating constraints for demand response aggregators (DRAGs)  
Operating constraints for energy storage aggregators (ESAGs)  
Operating constraints for EV charging stations (EVCSs)  
Operating constraints for dispatchable DG aggregators (DDGAGs)  
**Linearized distribution power flow equations**

# DSO Framework: The Objective Function

$$\begin{aligned}
 \text{Min } \sum_{t \in T} & \left[ -P_t^{\text{sub}} \pi_t^e - r_t^{\text{sub}, \text{up}} \pi_t^{\text{cap}, \text{up}} - r_t^{\text{sub}, \text{dn}} \pi_t^{\text{cap}, \text{dn}} \right. \\
 & \left. - r_t^{\text{sub}, \text{up}} S_t^{\text{up}} \mu_t^{\text{up}} \pi_t^{\text{mil}, \text{up}} - r_t^{\text{sub}, \text{dn}} S_t^{\text{dn}} \mu_t^{\text{dn}} \pi_t^{\text{mil}, \text{dn}} \right] \\
 & + \sum_{k \in \{K_2, K_4\}} P_{t,k} \pi_{t,k}^e - \sum_{k_3 \in K_3} P_{t,k_3} \pi_{t,k_3}^e \\
 & + \sum_{k \in K} \left[ r_{t,k}^{\text{up}} \pi_{t,k}^{\text{cap}, \text{up}} + r_{t,k}^{\text{dn}} \pi_{t,k}^{\text{cap}, \text{dn}} + r_{t,k}^{\text{up}} S_t^{\text{up}} \mu_t^{\text{up}} \pi_{t,k}^{\text{mil}, \text{up}} \right. \\
 & \left. + r_{t,k}^{\text{dn}} S_t^{\text{dn}} \mu_t^{\text{dn}} \pi_{t,k}^{\text{mil}, \text{dn}} \right] - \sum_{k_1 \in K_1} \sum_{a \in A} P_{a,t,k_1} \pi_{a,t,k_1}^e \Big]
 \end{aligned}$$

} **DSO Operating Cost for Participating in Wholesale Energy, Regulation Capacity & Regulation Mileage Markets**

} **DSO Operating Cost for Operating Retail Energy Markets with Various DER Aggregators**

## DSO Problem Formulation

$$\min \sum_{t \in T} [\text{Total DSO Operating Cost}]$$

↔ **Maximize total social welfare in the distribution grid**



# DSO Framework: The Constraints

## Operating Constraints for Demand Response Aggregators (DRAGs)

$$\sum_{a \in A} P_{a,t,k_1} - r_{t,k_1}^{cap,dn} \geq 0; \quad \forall t \in T, \forall k_1 \in K_1$$

$$P_{t,k_2} = E_{t-1,k_2} - E_{t,k_2} + (1/\eta_{k_2}^{di}) r_{t,k_2}^{cap,up} \mu_t^{up} - (\eta_{k_2}^{ch}) r_{t,k_2}^{cap,dn} \mu_t^{dn}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$P_{t,k_2} = (1/\eta_{k_2}^{di}) P_{t,k_2}^{di} - (\eta_{k_2}^{ch}) P_{t,k_2}^{ch}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$r_{t,k_2}^{cap,up} = r_{t,k_2}^{cap,up,di} + r_{t,k_2}^{cap,dn,ch}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$r_{t,k_2}^{cap,dn} = r_{t,k_2}^{cap,dn,di} + r_{t,k_2}^{cap,up,ch}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$E_{k_2}^{min} \leq E_{t,k_2} \leq E_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$0 \leq P_{t,k_2}^{di} \leq b_{t,k_2} DR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$0 \leq r_{t,k_2}^{cap,up,di} \leq b_{t,k_2} DR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$0 \leq r_{t,k_2}^{cap,dn,di} \leq b_{t,k_2} DR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$0 \leq P_{t,k_2}^{ch} \leq (1 - b_{t,k_2}) CR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$0 \leq r_{t,k_2}^{cap,up,ch} \leq (1 - b_{t,k_2}) CR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$0 \leq r_{t,k_2}^{cap,dn,ch} \leq (1 - b_{t,k_2}) CR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2$$

$$r_{t,k_2}^{cap,dn,di} \leq P_{t,k_2}^{di} \leq DR_{k_2}^{max} - r_{t,k_2}^{cap,up,di}; \\ \forall t \in T, \forall k_2 \in K_2$$

$$r_{t,k_2}^{cap,dn,ch} \leq P_{t,k_2}^{ch} \leq CR_{k_2}^{max} - r_{t,k_2}^{cap,up,ch}; \\ \forall t \in T, \forall k_2 \in K_2$$

- Limitations for DRAG's offers to energy, regulation capacity-up and capacity-down markets
- Real power offered at each demand block is limited within its permitted range
- The regulation capacity-up and capacity-down offers are lower than their maximum permitted values.

# DSO Framework: The Constraints

## ► Operating Constraints for Energy Storage Aggregators (ESAGs)

$$\begin{aligned} P_{t,k_2} &= E_{t-1,k_2} - E_{t,k_2} + (1/\eta_{k_2}^{di}) r_{t,k_2}^{cap,up} \mu_t^{up} \\ &\quad - (\eta_{k_2}^{ch}) r_{t,k_2}^{cap,dn} \mu_t^{dn}; \quad \forall t \in T, \forall k_2 \in K_2 \\ P_{t,k_2} &= (1/\eta_{k_2}^{di}) P_{t,k_2}^{di} - (\eta_{k_2}^{ch}) P_{t,k_2}^{ch}; \quad \forall t \in T, \forall k_2 \in K_2 \\ r_{t,k_2}^{cap,up} &= r_{t,k_2}^{cap,up,di} + r_{t,k_2}^{cap,dn,ch}; \quad \forall t \in T, \forall k_2 \in K_2 \\ r_{t,k_2}^{cap,dn} &= r_{t,k_2}^{cap,dn,di} + r_{t,k_2}^{cap,up,ch}; \quad \forall t \in T, \forall k_2 \in K_2 \\ E_{k_2}^{min} &\leq E_{t,k_2} \leq E_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ 0 &\leq P_{t,k_2}^{di} \leq b_{t,k_2} DR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ 0 &\leq r_{t,k_2}^{cap,up,di} \leq b_{t,k_2} DR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ 0 &\leq r_{t,k_2}^{cap,dn,di} \leq b_{t,k_2} DR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ 0 &\leq P_{t,k_2}^{ch} \leq (1 - b_{t,k_2}) CR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ 0 &\leq r_{t,k_2}^{cap,up,ch} \leq (1 - b_{t,k_2}) CR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ 0 &\leq r_{t,k_2}^{cap,dn,ch} \leq (1 - b_{t,k_2}) CR_{k_2}^{max}; \quad \forall t \in T, \forall k_2 \in K_2 \\ r_{t,k_2}^{cap,dn,di} &\leq P_{t,k_2}^{di} \leq DR_{k_2}^{max} - r_{t,k_2}^{cap,up,di}; \\ &\quad \forall t \in T, \forall k_2 \in K_2 \\ r_{t,k_2}^{cap,dn,ch} &\leq P_{t,k_2}^{ch} \leq CR_{k_2}^{max} - r_{t,k_2}^{cap,up,ch}; \\ &\quad \forall t \in T, \forall k_2 \in K_2 \end{aligned}$$

- Defining ESAG's power injection
- Decomposing offers to the energy, regulation capacity-up and capacity-down markets into charging and discharging terms
- Limitation for the charge level
- Ensure that ESAG's offers to the energy, regulation capacity-up and capacity-down markets are in their permitted ranges.
- Limitation for ESAG's offers to the energy, regulation capacity-up and capacity-down markets with respect to the charging and discharging rates.

# DSO Framework: The Constraints

## Operating Constraints for EV Charging Stations (EVCSs)

$$\begin{aligned} 0 &\leq P_{t,k_3} \leq ER_{k_3}^{max} b_{k_3}; \quad \forall t \in T', \forall k_3 \in K_3 \\ 0 &\leq r_{t,k_3}^{cap,up} \leq ERR_{k_3}^{max} b_{k_3}; \quad \forall t \in T', \forall k_3 \in K_3 \\ 0 &\leq r_{t,k_3}^{cap,dn} \leq ERR_{k_3}^{max} b_{k_3}; \quad \forall t \in T', \forall k_3 \in K_3 \\ P_{t,k_3} + r_{t,k_3}^{cap,up} &\leq ER_{k_3}^{max}; \quad \forall t \in T', \forall k_3 \in K_3 \\ P_{t,k_3} - r_{t,k_3}^{cap,dn} &\geq 0; \quad \forall t \in T', \forall k_3 \in K_3 \\ 0.9CL_{k_3}^{max} b_{k_3} &\leq E_{k_3}^{int} b_{k_3} + \sum_{t \in T'} [P_{t,k_3} + r_{t,k_3}^{cap,up} \mu_t^{up} \\ &\quad - r_{t,k_3}^{cap,dn} \mu_t^{dn}] \gamma_{k_3}^{ch} \leq CL_{k_3}^{max} b_{k_3}; \quad \forall k_3 \in K_3 \end{aligned}$$

- Limitation for EVCS's offers to the energy, regulation capacity-up and capacity-down markets.
- Ensuring that EVs are fully charged

## Operating Constraints for Dispatchable DG Aggregators (DDGAGs)

$$\begin{aligned} P_{t,k_4} + r_{t,k_4}^{cap,up} &\leq P_{k_4}^{max}; \quad \forall t \in T, \forall k_4 \in K_4 \\ P_{t,k_4} - r_{t,k_4}^{cap,dn} &\geq P_{k_4}^{min}; \quad \forall t \in T, \forall k_4 \in K_4 \\ 0 &\leq r_{t,k_4}^{cap,up} \leq RU_{k_4}; \quad \forall t \in T, \forall k_4 \in K_4 \\ 0 &\leq r_{t,k_4}^{cap,dn} \leq RD_{k_4}; \quad \forall t \in T, \forall k_4 \in K_4 \end{aligned}$$

- Limitation DDAG's offers to the energy, regulation capacity-up and capacity-down markets.
- Ensure the regulation capacity-up/capacity-down offers are lower than maximum ramp-up/ramp-down rates.

# DSO Framework: The Constraints

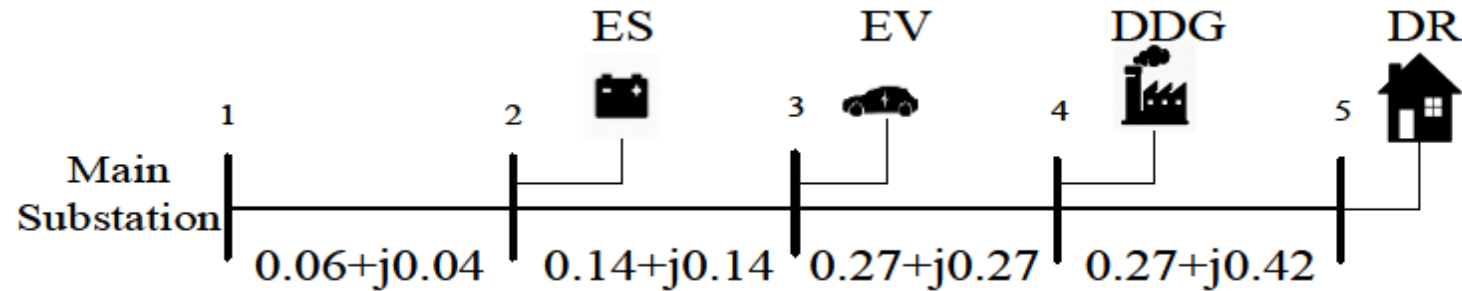
## ▶▶ Linearized Distribution Power Flow Equations [1]

$$\begin{aligned}
 & \sum_{k_1 \in K_1} \sum_{a \in A} H_{n,k_1} P_{a,t,k_1} + \sum_{k_3 \in K_3} H_{n,k_3} P_{t,k_3} + P_{t,n}^D \\
 & - \sum_{k_2 \in K_2} H_{n,k_2} P_{t,k_2} - \sum_{k_4 \in K_4} H_{n,k_4} P_{t,k_4} \\
 & + H_n^{sub} P_t^{sub} + \sum_{j \in J} Pl_{j,t} A_{j,n} = 0; \quad \forall t \in T, \forall n \in N \\
 & \sum_{k_1 \in K_1} \sum_{a \in A} H_{n,k_1} P_{a,t,k_1} \tan \phi_{k_1} + Q_{t,n}^D \\
 & - \sum_{k_4 \in K_4} H_{n,k_4} P_{t,k_4} \tan \phi_{k_4} \\
 & + H_n^{sub} Q_t^{sub} + \sum_{j \in J} Ql_{j,t} A_{j,n} = 0; \quad \forall t \in T, \forall n \in N \\
 & V_{m,t} = V_{n,t} - (r_j Pl_{j,t} + x_j Ql_{j,t}); \quad \forall t \in T, \forall m \in N, \\
 & \quad \forall n \in N, C(m,n) = 1, A(j,n) = 1 \\
 & V^{min} \leq V_{n,t} \leq V^{max}; \quad \forall t \in T, \forall n \in N \\
 & - Pl^{max} \leq Pl_{j,t} \leq Pl^{max}; \quad \forall t \in T, \forall j \in J \\
 & - Ql^{max} \leq Ql_{j,t} \leq Ql^{max}; \quad \forall t \in T, \forall j \in J \\
 & r_t^{sub,up} = \sum_{k_2 \in K_2} r_{t,k_2}^{cap,up} + \sum_{k_4 \in K_4} r_{t,k_4}^{cap,up} \\
 & \quad + \sum_{k_1 \in K_1} r_{t,k_1}^{cap,dn} + \sum_{k_3 \in K_3} r_{t,k_3}^{cap,dn}; \quad \forall t \in T \\
 & r_t^{sub,dn} = \sum_{k_2 \in K_2} r_{t,k_2}^{cap,dn} + \sum_{k_4 \in K_4} r_{t,k_4}^{cap,dn} \\
 & \quad + \sum_{k_1 \in K_1} r_{t,k_1}^{cap,up} + \sum_{k_3 \in K_3} r_{t,k_3}^{cap,up}; \quad \forall t \in T
 \end{aligned}$$

- Represent the real and reactive power flow
- Represent voltage drop at each line
- Represent real and reactive power limits at each line
- Represent DSO's aggregated offers for participating in the wholesale energy, regulation capacity-up and capacity-down markets.

[1] M. E. Baran and F. F. Wu, "Network reconfiguration in distribution systems for loss reduction and load balancing," IEEE Trans. Power Del., vol. 4, no. 2, pp. 1401–1407, April 1989.

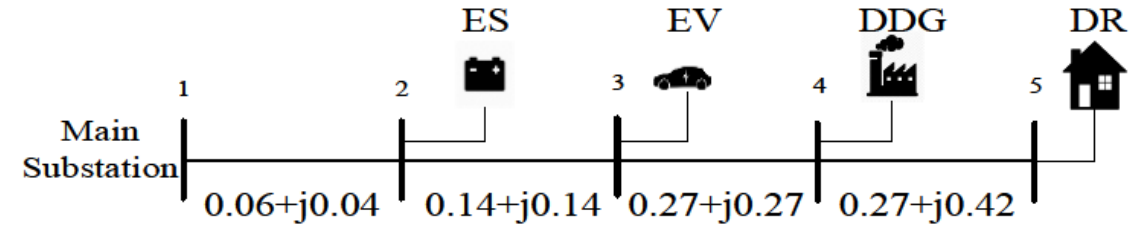
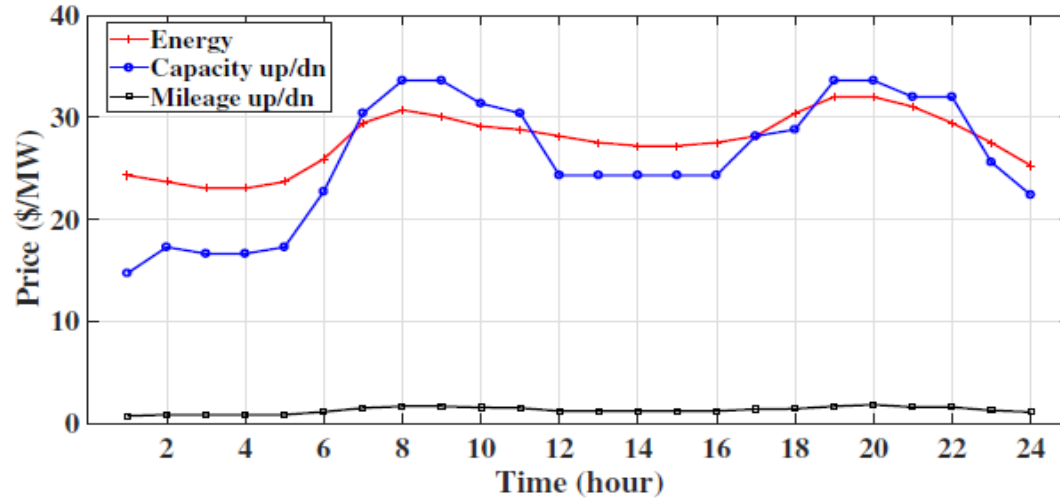
# Case Studies: The Test System



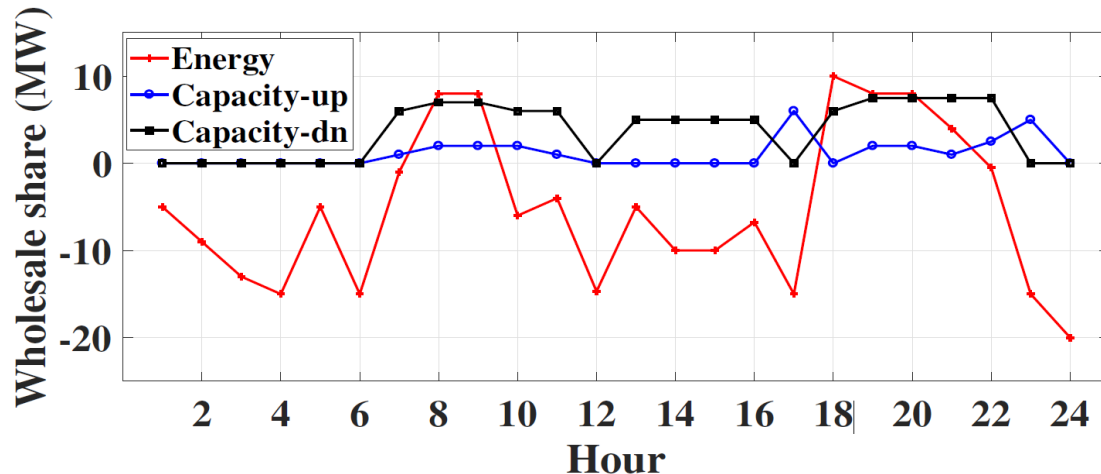
- A distribution test system with 5 nodes and 4 lines
- One demand response aggregator @ Node 5
- One dispatchable DG aggregator @ Node 4
- One EV charging station @ Node 3
- One energy storage aggregator @ Node 2

# Case Studies: DSO's Wholesale Market Participation

## Wholesale Energy and Regulation Markets Prices



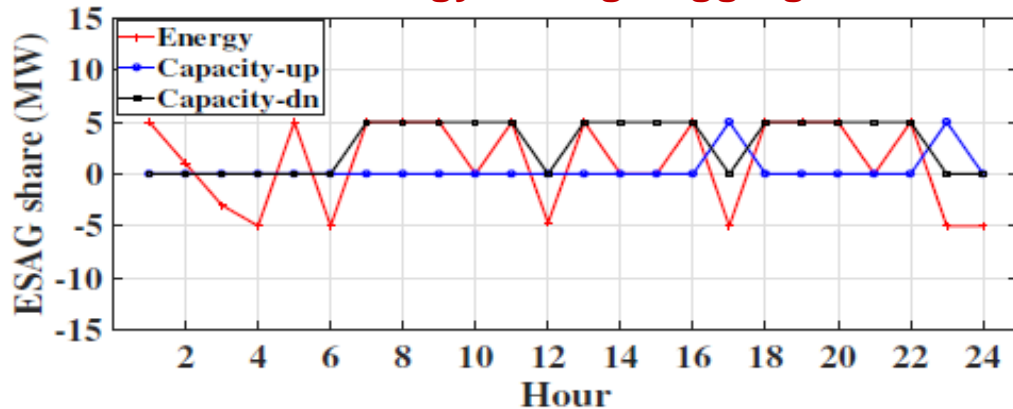
## Trades between DSO and Wholesale Market



- **DSO** sells energy to the wholesale market @ hours 8~9 and 18~21 → wholesale energy prices are high
- **DSO** buys energy from the wholesale market @ other hours

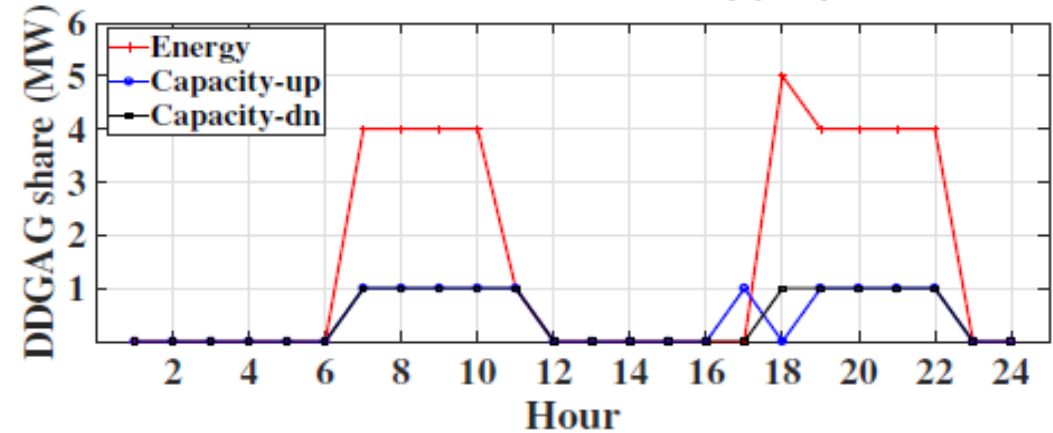
# Case Studies: Aggregators' Market Participation

Hourly Awarded Energy & Regulation Services  
for The **Energy Storage Aggregator**



- **Energy storage aggregator** prefers offering regulation capacity-down service → To increase its charging level
- **Energy storage aggregator** offers regulation capacity-down service at hours 13~16, when the regulation capacity-down price is lower than the energy price in wholesale market

Hourly Awarded Energy & Regulation Services  
for The **Dispatchable DG Aggregator**

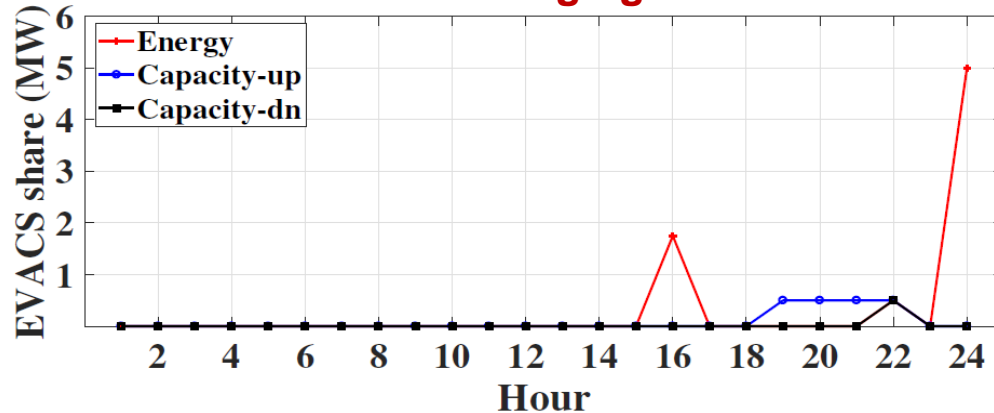


- **Dispatchable DG aggregator** offers energy and regulation capacity services to the wholesale market during peak hours
- **Dispatchable DG aggregator** increases its energy provision (without offering regulation capacity-up services) @ hour 18, when wholesale regulation capacity price is lower than wholesale energy price



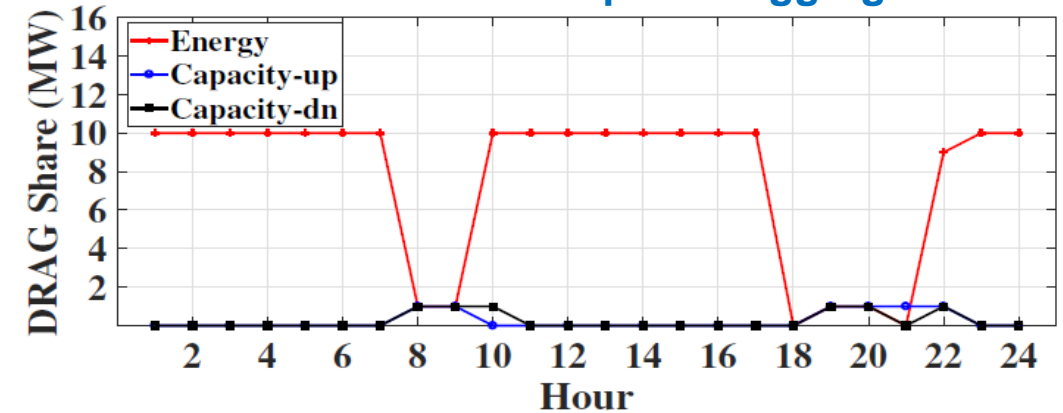
# Case Studies: Retail Market Outcomes

Hourly Awarded Energy & Regulation Services  
for The **EV Charging Station**



- **EV charging station** purchases energy @ hours 16 and 24 → Wholesale energy price is the lowest of the day
- **EV charging station** offers regulation capacity-up service @ hours 19~22 → Regulation capacity-up price is high, and EV charging station can increase EV charge levels by offering this service

Hourly Awarded Energy & Regulation Services  
for The **Demand Response Aggregator**



- **Dispatchable DG aggregator** does not purchase energy from wholesale market at peak hours
- **Dispatchable DG aggregator** purchases energy for providing regulation capacity-down service



# Part II: Conclusions & Future Directions

## ➡ Conclusions

- **A DSO framework:**

- ✓ Operate the retail energy market and participate in the wholesale energy and regulation markets
- ✓ Collect offers from various DER aggregators via the retail market, and coordinate these offers to construct an aggregated offer/bid for participating in the day-ahead wholesale market
- ✓ Consider distribution power flow constraints

## ➡ Future Directions

- **Improve the proposed DSO framework:**

- ✓ Three-phase unbalanced operations
- ✓ Aggregators with mixed types of resources
- ✓ Reactive power incentivization via the retail market, etc.

# Proposed Solutions

1

## *Market + Batteries:*

Optimal Battery Participation in Energy & Ancillary Services Markets

2

## *Market + DER Aggregators:*

A DSO Design for Wholesale & Retail Markets with DER Aggregators

3

## *Market Participation:*

**Machine Learning for System-Wide Electricity Price Forecasting**

# Background & Motivation

## ➡ Electricity Price Forecasting by Market Participants

- Critical for market participants to determine optimal bidding/offering strategies
  - No confidential system model parameters/topology/operating conditions available to market participants
- ➔ Market participants need to forecast LMPs in a purely model-free/data-driven manor



## ➡ Machine Learning for System-Wide Real-Time LMP Forecasting

- Purely model-free, using only public market data
- No confidential system modeling/operating details
- Spatio-temporal correlations among heterogeneous market data
- Inspired by **video prediction techniques**

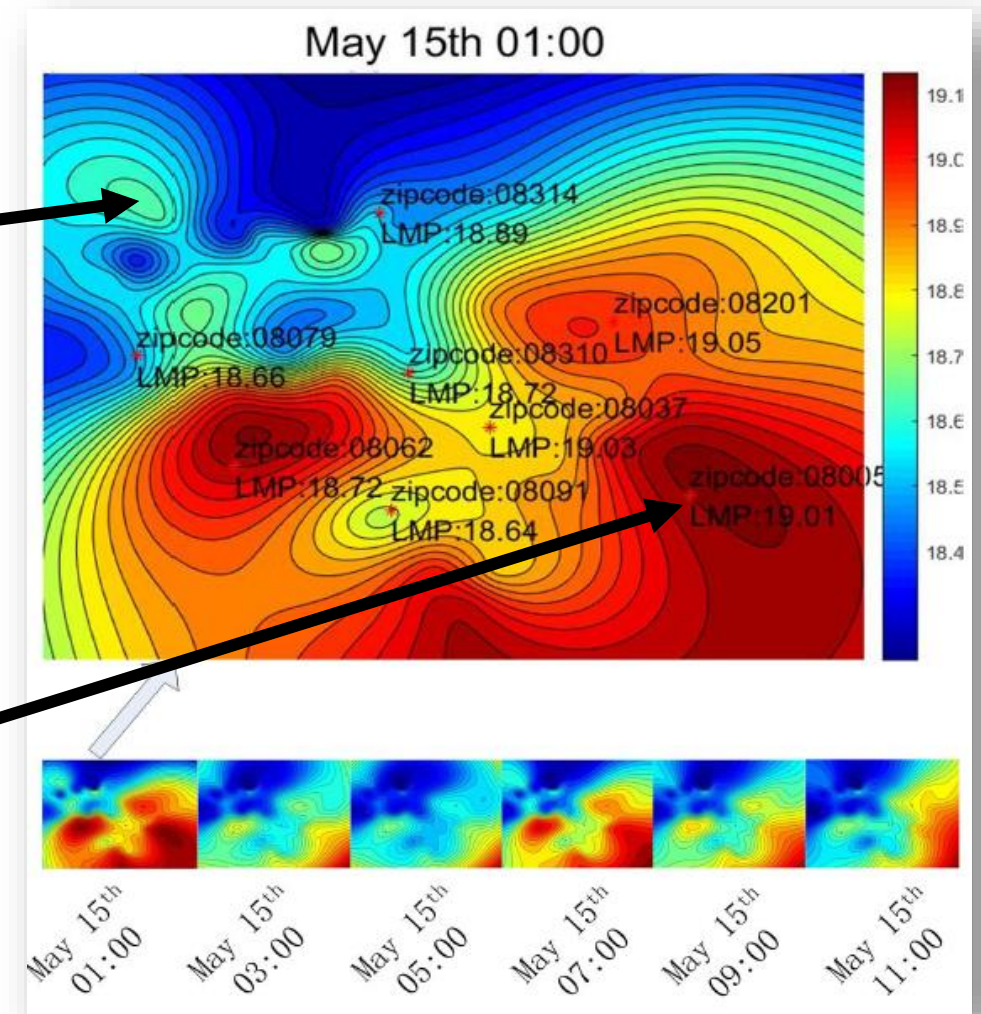
# Market Data Images & Videos (PJM AECO Price Zone)

## Heterogeneous Market Data

- Zipcode = 08014
- Hour = 1 AM, May 15, 2019
- LMP = \$18.77 \$/MWh
- Load = 1.05 MW
- Temperature = 39.59 F
- .....

## Heterogeneous Market Data

- Zipcode = 08005
- Hour = 1 AM, May 15, 2019
- LMP \$19.01 \$/MWh
- Load = 33.42 MW
- Temperature = 41.54 F
- .....

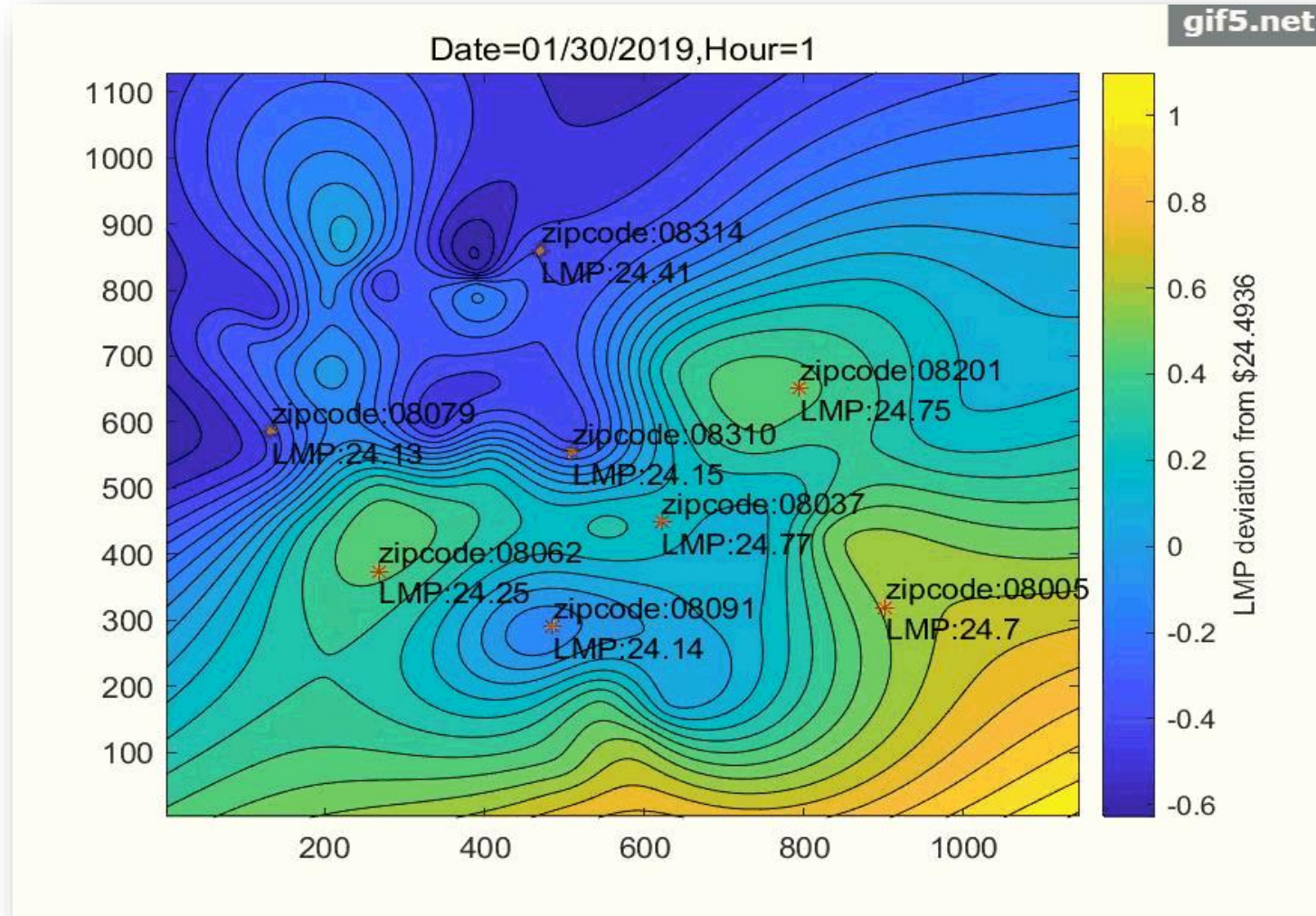


Spatio-Temporal Market Data



Market Data Images & Videos

# Example: Market Data Video (PJM AECO Price Zone)

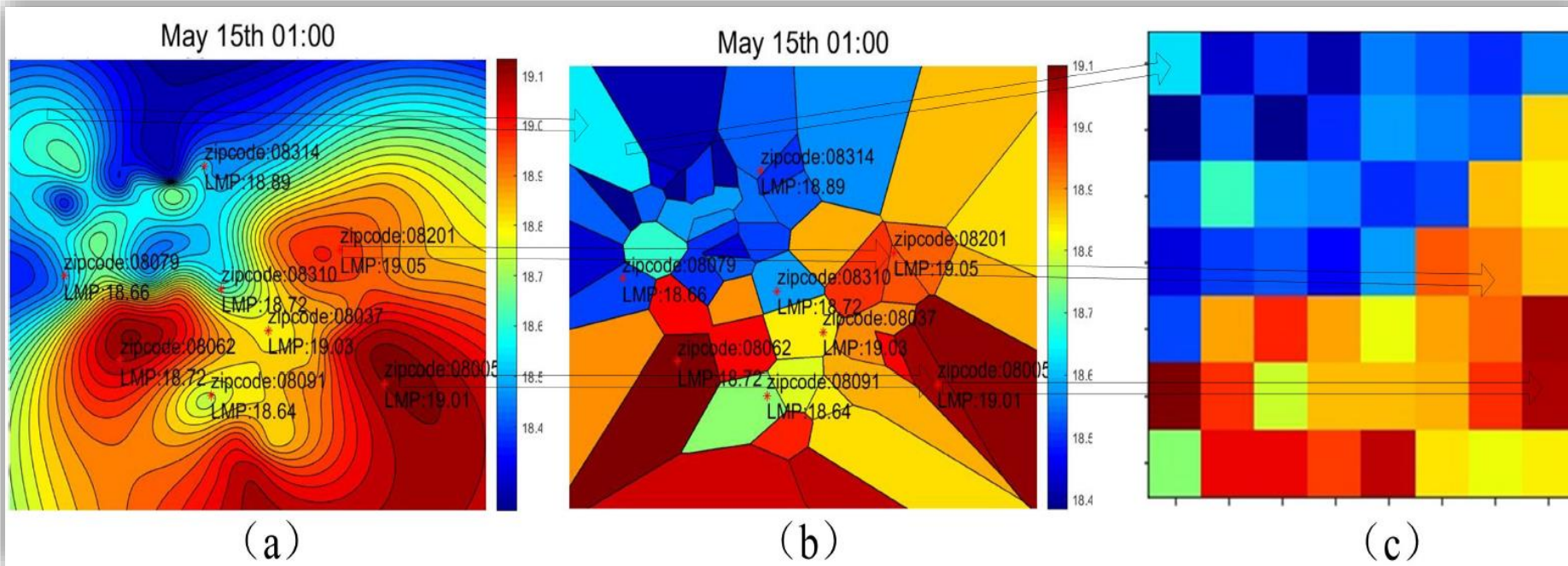


Hourly LMPs @ PJM AECO Price Zone on 1/30/2019



# General Data Structure: Market Data Pixels, Images, & Videos

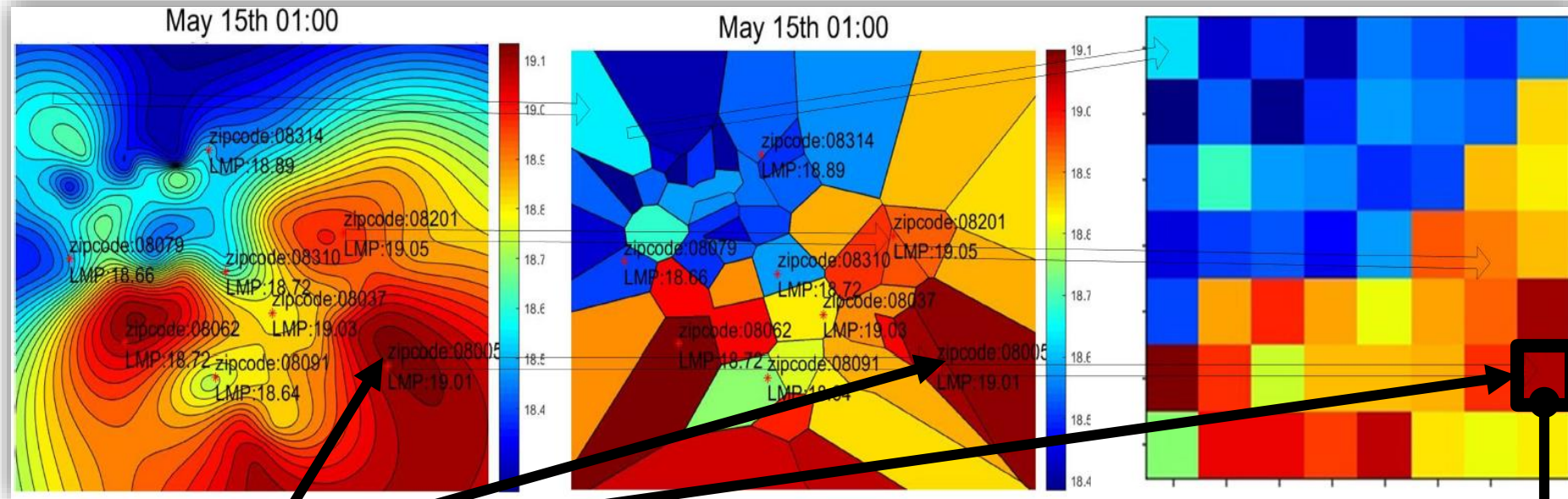
➡ Different interpolation techniques applied to the same market dataset (56 price nodes)



**PJM AECO  
Price Zone**

- [a] Biharmonic spline interpolation ➔ smooth with many different colors
- [b] Nearest neighbor interpolation ➔ less smooth with exactly 56 different colors (1 color/price node)
- [c] Pixel representation ➔ 56 **pixels** with 56 different colors (1 color/price node)

# General Data Structure: Market Data Pixels, Images, & Videos



## Heterogeneous Market Data

- Zipcode = 08005
- Hour = 1 AM, May 15, 2019
- **LMP \$19.01 \$/MWh**
- **Load = 33.42 MW**
- **Temperature = 41.54 F**
- .....

Data

Normalization

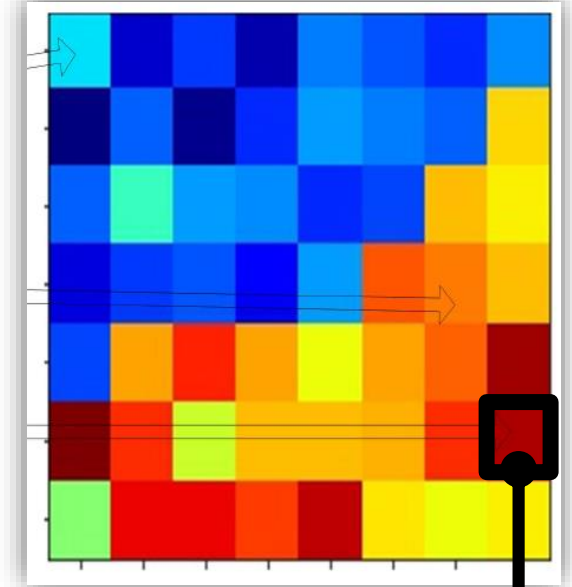
## RGB Color Codes

- Pixel Location = [6,8]
- Hour = 1 AM, May 15, 2019
- **R = Normalized (LMP)**
- **G = Normalized (Load)**
- **B = Normalized (Temperature)**
- **Pixel Color = [R,G,B]**

# General Data Structure: Market Data Pixels, Images, & Videos

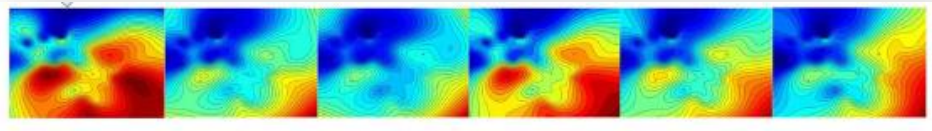
## ➡ Market Data Pixel

- The smallest addressable element of a market data image
- Pixel color is fully determined by the R, G, B color codes
- R, G, B color codes = percentages of red, green, blue colors in a pixel
- Let R, G, B color codes = Normalized heterogeneous market data
- ➔ Color of market data pixel =  $f(\text{Normalized heterogeneous market data})$



## ➡ Market Data Image & Video

- [Market Data Image]: Spatioal variations of market data
- [Market Data Video]: Spatio-temporal variations of market data

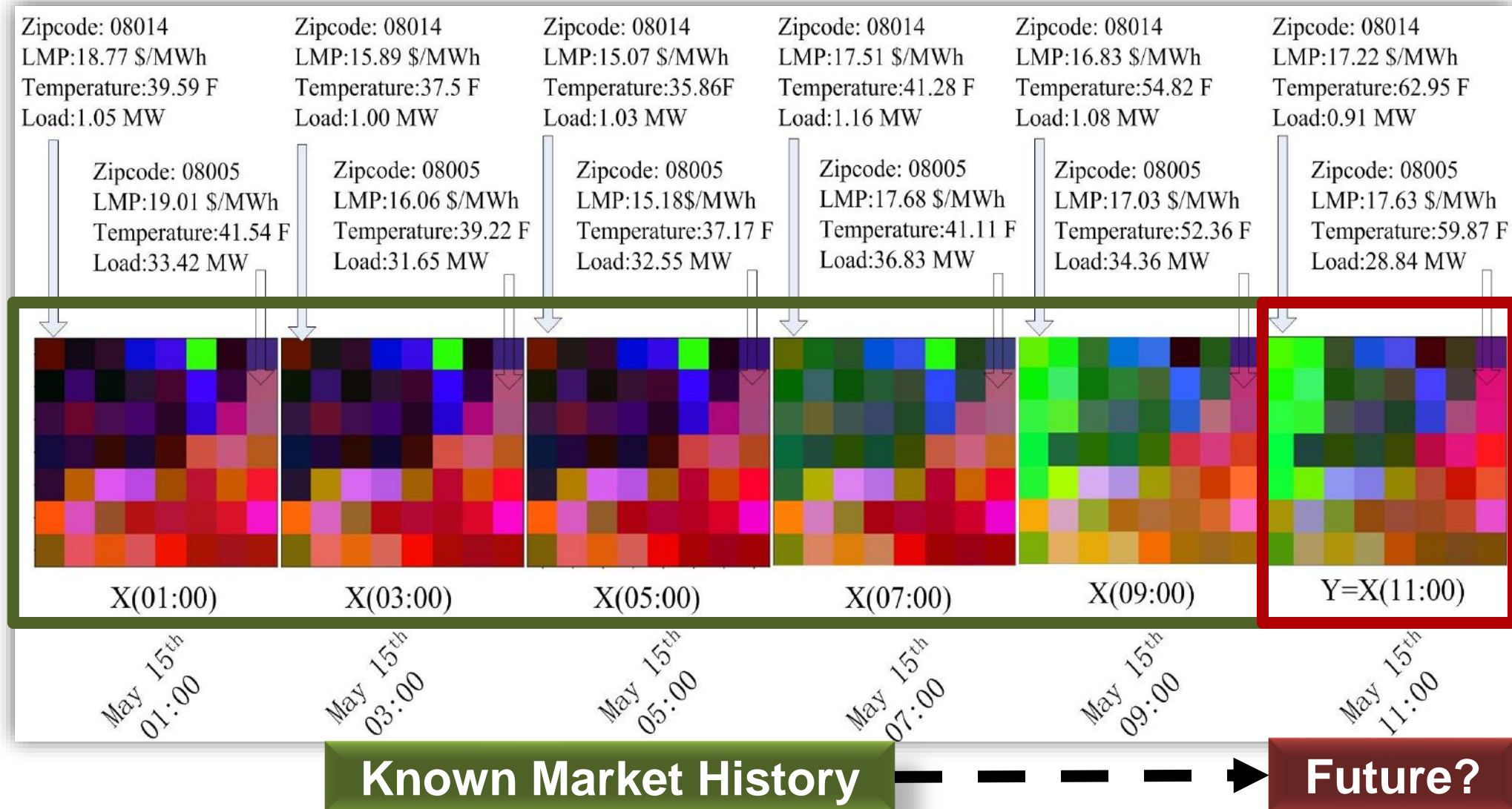


### RGB Color Codes

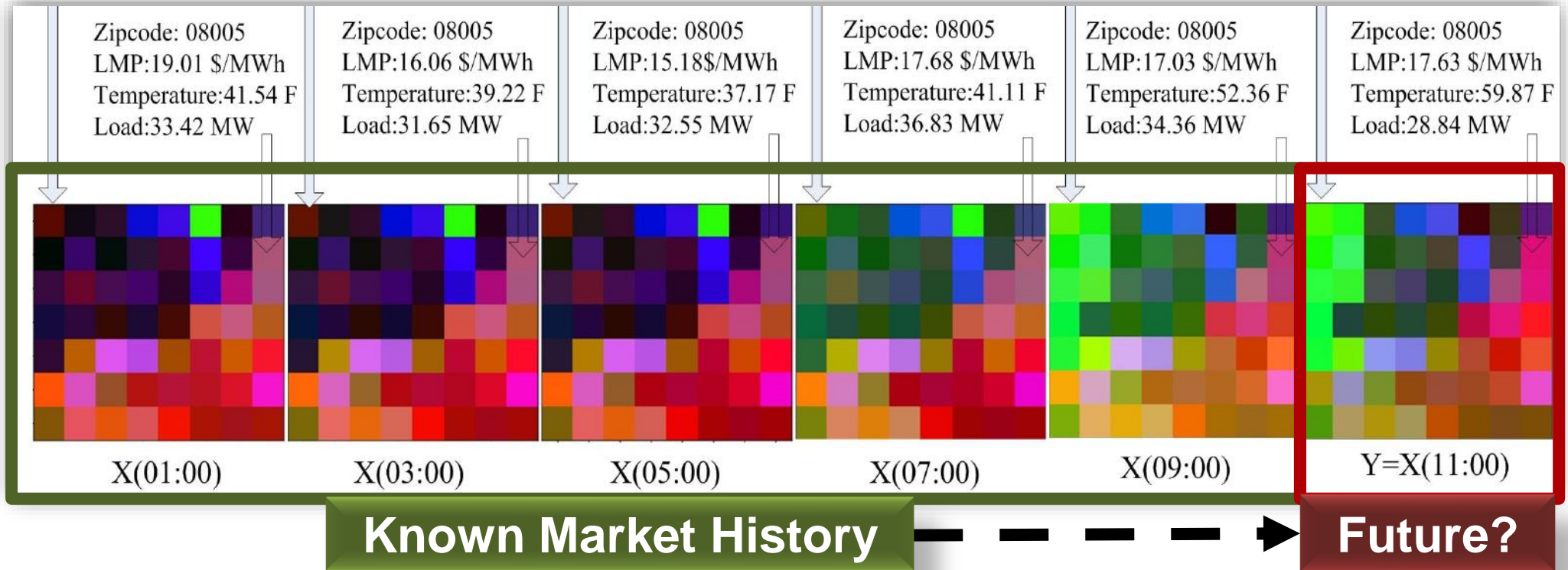
- Pixel Location = [6,8]
- Hour = 1 AM, May 15, 2019
- R = Normalized (LMP)
- G = Normalized (Load)
- B = Normalized (Temperature)
- Pixel Color = [R,G,B]



# Market Data Video: An Example (PJM AECO Price Zone, 56 Price Nodes)



# Market Data Video: An Example (PJM AECO Price Zone, 56 Price Nodes)

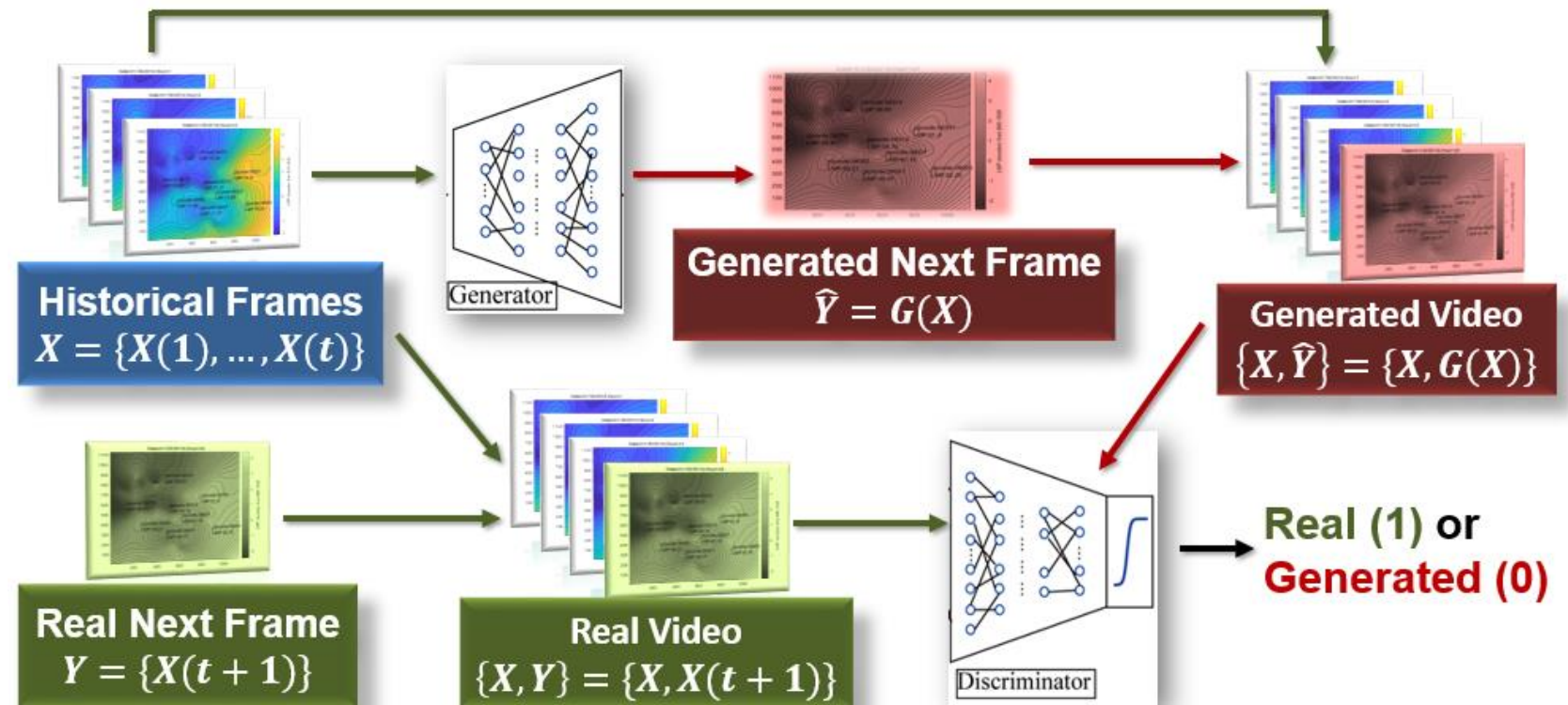


- ❖ Market Data Pixel @ Location  $[i, j]$  @ Time  $t$ :  $x_{i,j}(t) = [\mathbf{x}_{i,j}^R(t), \mathbf{x}_{i,j}^G(t), \mathbf{x}_{i,j}^B(t)] = f(\text{Normalized Market Data})$
- ❖ Market Data Image @ Time  $t$ :  $M \times N$  matrix  $X(t) = [x_{i,j}(t)]$
- ❖ Market Data Video @ Time 1~T :  $X = \{X(1), \dots, X(t), \dots, X(T)\}$

# Deep Video Prediction for System-Wide LMP Forecasting

- ❖ **Problem Formulation:** Given the historical market data video  $X = \{X(1), \dots, X(t)\}$ , generate a future video frame  $Y = \hat{X}(t + 1)$ , s.t. the conditional probability  $p(\hat{X}(t + 1)|X)$  is maximized.
- ❖ **Proposed Solution:** Conditional Generative Adversarial Network (GAN) with multiple loss functions.

- Training Procedure:  
GAN-Based Real-Time  
LMP Forecasting





# Loss Functions: Learning Spatio-Temporal Correlations

►► **Discriminator:** A CNN trained by minimizing the following loss (distance) function:

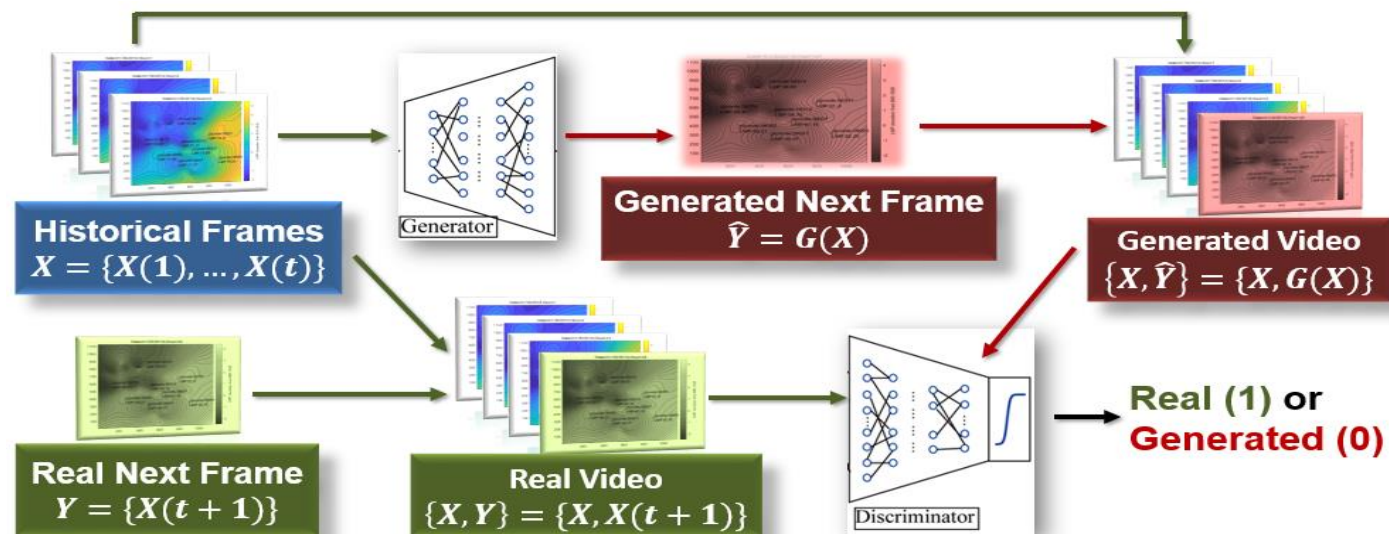
$$\mathcal{L}_{adv}^D(X, Y) = \mathcal{L}_{bce}(D(\{X, Y\}), 1) + \mathcal{L}_{bce}(D(\{X, \hat{Y}\}), 0) \quad (4)$$

where  $\mathcal{L}_{bce}$  is the binary cross-entropy:

$$\mathcal{L}_{bce}(K, S) = - \sum_i [K_i \log(S_i) + (1 - K_i) \log(1 - S_i)] \quad (5)$$

where  $K_i \in [0, 1]$  and  $S_i \in \{0, 1\}$ .

- ❖ **Objective:** Classify input videos  $\{X, Y\}$  as real (1) and  $\{X, \hat{Y}\}$  as generated/fake (0).
- ❖ **Upon Convergence:** Generator produces realistic  $\hat{Y}$ , s.t. Discriminator cannot classify  $\hat{Y}$  as generated/fake.



# Loss Functions: Learning Spatio-Temporal Correlations

► **Generator:** A CNN trained by minimizing the following loss (distance) functions:

$$\mathcal{L}^G(X, Y) = \lambda_{adv} \mathcal{L}_{adv}^G(X, Y) + \lambda_{\ell_p} \mathcal{L}_p(X, Y) \\ + \lambda_{gdl} \mathcal{L}_{gdl}(X, Y) + \lambda_{dcl} \mathcal{L}_{dcl}(X, Y)$$

$$\mathcal{L}_p(X, Y) = \ell_p(G(X), Y) = \|G(X) - Y\|_p^p$$

$$\mathcal{L}_{adv}^G(X, Y) = \mathcal{L}_{bce}(D(\{X, G(X)\}), 1)$$

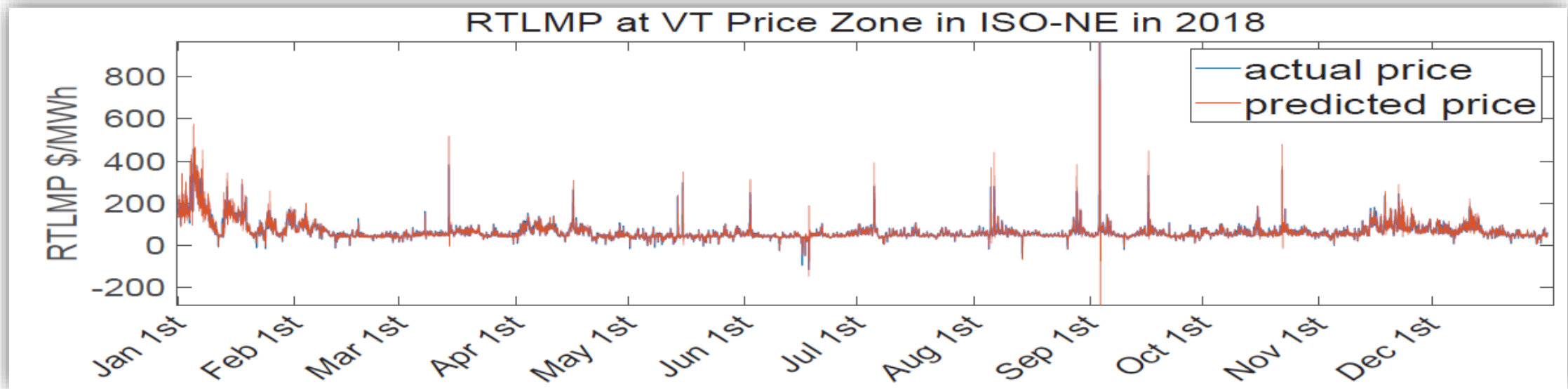
$$\mathcal{L}_{gdl}(X, Y) = \mathcal{L}_{gdl}(\hat{Y}, Y) \\ = \sum_{i,j} ||Y_{i,j} - Y_{i-1,j}| - |\hat{Y}_{i,j} - \hat{Y}_{i-1,j}||^\alpha \\ + ||Y_{i,j-1} - Y_{i,j}| - |\hat{Y}_{i,j-1} - \hat{Y}_{i,j}||^\alpha$$

$$\mathcal{L}_{dcl}(X, Y) = \sum_{i,j} |sgn(\hat{Y}_{i,j} - X_{i,j}(t)) - sgn(Y_{i,j} - X_{i,j}(t))|$$

- ❖ **Objective:** Generate  $\hat{Y} = G(X)$ , s.t. the distance b.t.  $Y$  and  $\hat{Y}$  (quantified by  $\mathcal{L}^G(X, Y)$ ) is minimized.
- ❖  $\mathcal{L}_p(X, Y)$ :  $p$ -norm distance b.t.  $Y$  &  $\hat{Y}$
- ❖  $\mathcal{L}_{adv}^G(X, Y)$ : temporal coherency of generated video  $\{X, \hat{Y}\} = \{X, X(G)\}$
- ❖  $\mathcal{L}_{gdl}(X, Y)$ : spatial correlations among market data at neighboring price nodes.
- ❖  $\mathcal{L}_{dcl}(X, Y)$ : market data changing directions (increment/decrement)

# Case Study 1: ISO New England

- ❖ **Training Data for Case 1:** Hourly zonal real-time LMPs, day-ahead LMPs, and demands in the entire years of 2016 and 2017 @ 9 price zones of ISO-NE
- ❖ **Testing Data for Case 1:** Hourly zonal real-time LMPs in 2018 @ 9 price zones of ISO-NE

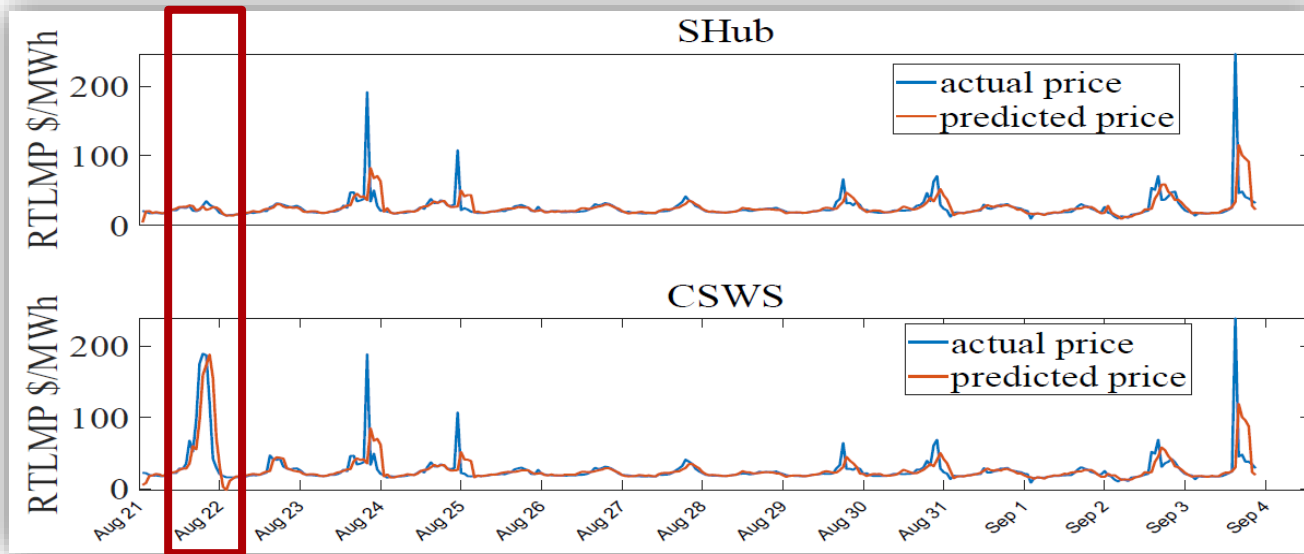


**Real-Time LMP Forecasting Error @ 9 Price Zones of ISO-NE**

Price Zone	VT	HN	ME	WC MA	Sys- tem	NE MA	CT	RI	SE MA
MAPE (%)	11.03	11.25	11.82	10.99	11.06	11.05	11.04	11.01	11.05

# Case Study 2: Southwest Power Pool

- ❖ **Training Data for Case 2:** Hourly zonal real-time LMPs, day-ahead LMPs, demands, and generation resource mix data from 6/1/2016 to 7/30/2017
- ❖ **Testing Data for Case 2:** Hourly zonal real-time LMPs during 7/31/2017-8/13/2017, 8/21/2017-9/3/2017, 9/18/2017-10/1/2017, 10/2/2017-10/15/2017



## Real-Time LMP Forecasting Error @ SHub & NHub Price Zones of SPP

Approach	MAPE (%) for SHub Price Zone	MAPE (%) for NHub Price Zone
ALG+ $\hat{M}^1$	25.4	36.9
Genscape <sup>2</sup>	21.7	28.2
Case 2	17.7	19.1

- 1: Best LMP forecasting result with method proposed in [2]  
2: Baseline LMP forecasting from commercial predictor Genscape [2]

# Part III: Conclusions & Future Directions

## ➡ Conclusions

- **A General Data Structure:** Organizing heterogeneous spatio-temporal electricity market data into market data pixels, images, and videos
- **Real-Time LMP Forecasting:** Formulated as a video prediction problem and solved using conditional GAN with multiple loss functions
- **A General Framework:** Incorporating video/image processing techniques for power system spatio-temporal data analytics

## ➡ Future Directions

- **Improve LMP Forecasting:** electricity price spike forecasting, market (dc OPF) model/parameters recovery, etc.
- **Other Spatio-temporal data analytics:** Apply the general data structure and video/image processing techniques to other power system spatio-temporal data analytics



# Related Publications

**[Market + Batteries]:** R. Khalilisenobari and M. Wu, "Optimal Participation of Price-Maker Battery Energy Storage Systems in Energy, Reserve and Pay as Performance Regulation Markets," *2019 North American Power Symposium (NAPS)*, Wichita, KS, USA, 2019, pp. 1-6.

**[Market + DER Aggregators]:** M. Mousavi and M. Wu, "A DSO Framework for Comprehensive Market Participation of DER Aggregators," *2020 IEEE Power & Energy Society General Meeting*, Montreal, Canada, 2020, Accepted.

**[Price Forecasting]:** Z. Zhang and M. Wu, "Predicting Real-Time Locational Marginal Prices: A GAN-Based Video Prediction Approach," *IEEE Transactions on Power Systems*, Submitted.

# Market Participation of Energy Storage and DER Aggregators: Energy Arbitrage, Retail Market Design, and Electricity Price Forecasting

*Thank You!*



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