



**PSERC Webinar**  
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# **Distribution System Voltage Control under Imperfect Communications**

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# Voltage control

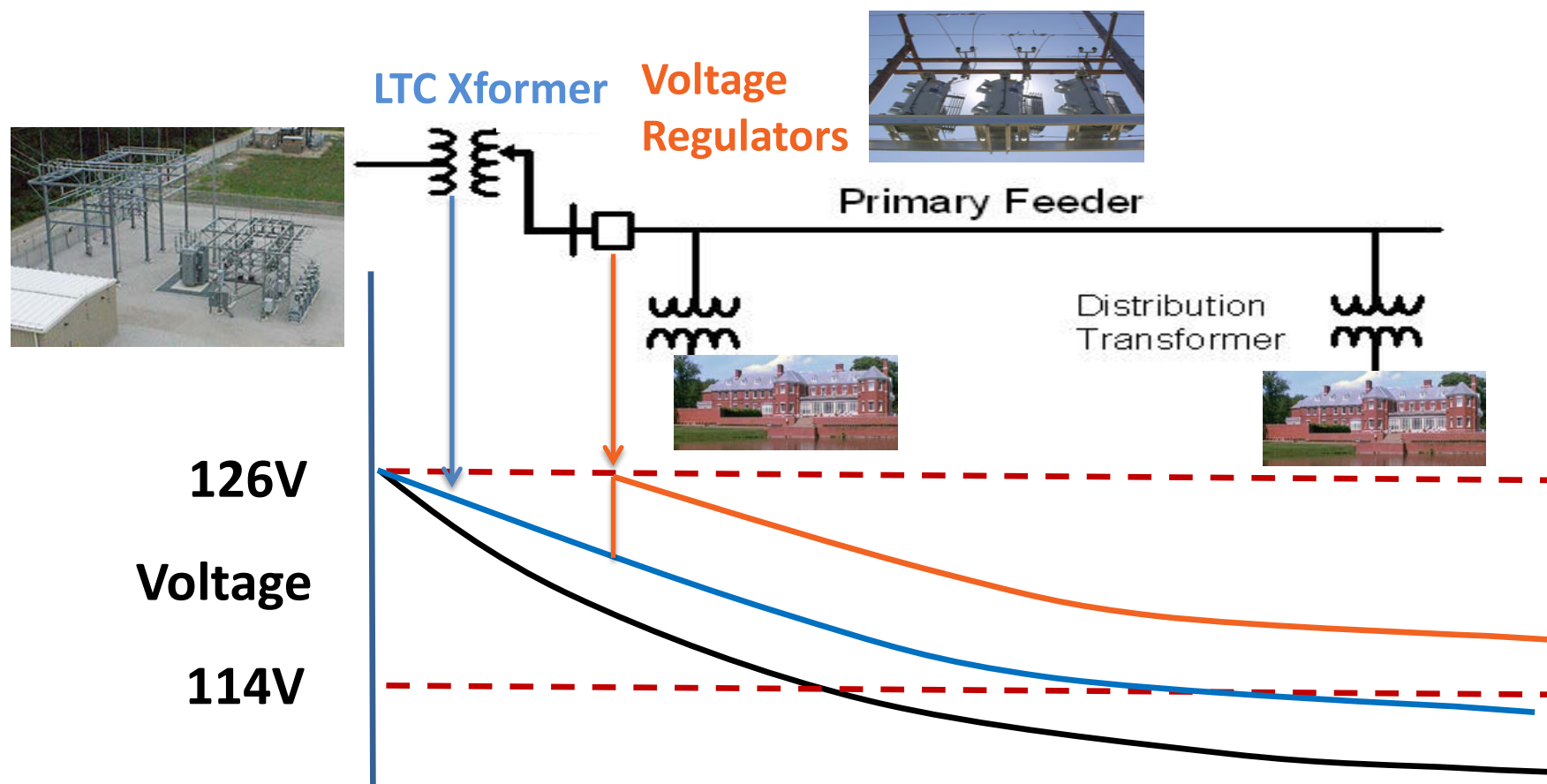
- Ideally, we all want to plug into a constant voltage source at 120V
- Voltage control/stability in bulk transmission grid more closely related to reactive power (VAR) load balance
  - Fast decoupled power flow (FDPF) model
- Real power could also affect voltage fluctuations in distribution systems because of the higher  $r/x$  ratio



Cartoon: W-R-O-N-G  
Voltaggheeee for a vintage  
machine like Myself  
[Source: jantoo.com]

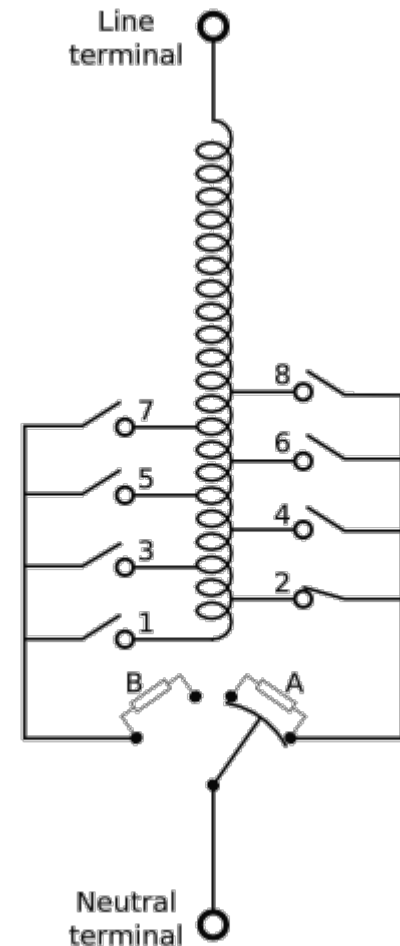
# Voltage control in distribution systems

- Typical control devices: load tap changer (LTC) transformers, voltage regulators, and capacitor banks



# Load tap changer (LTC)

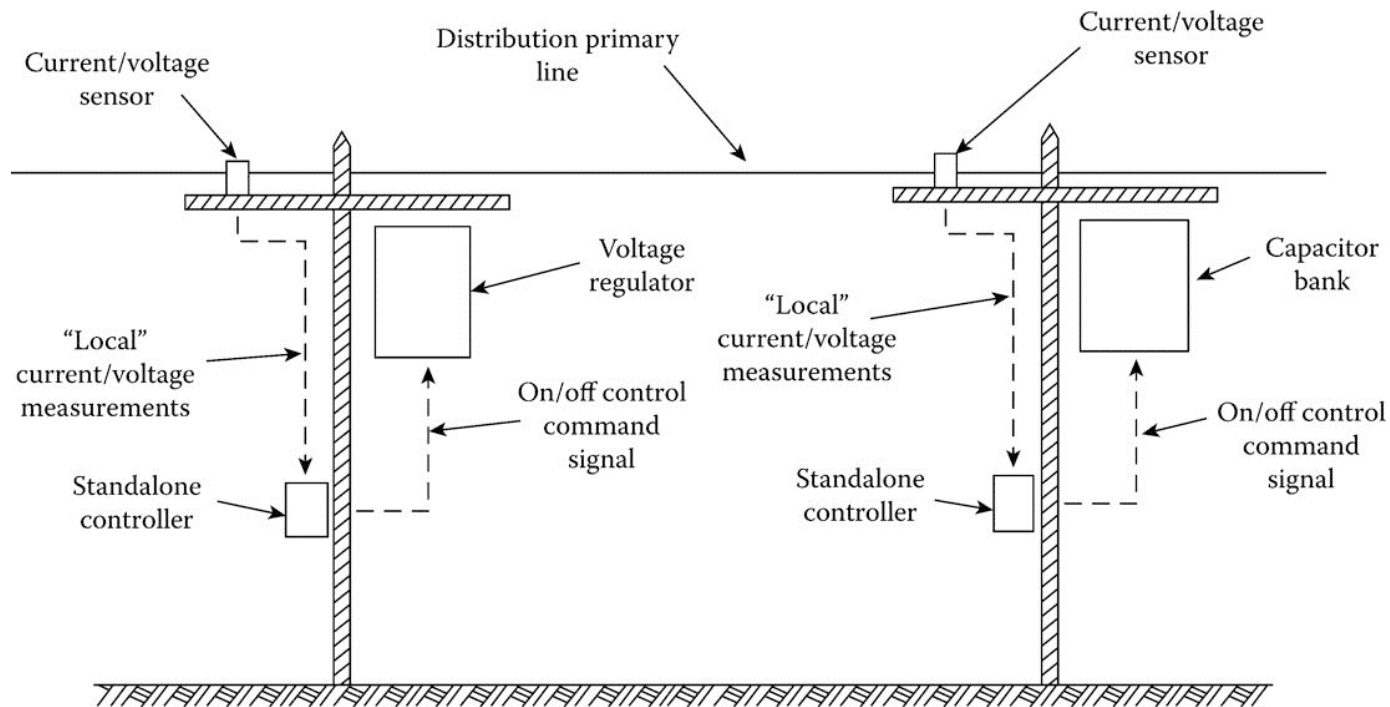
- A selector switch device attached to power transformers
- To maintain a constant low-side or secondary voltage with a variable primary voltage supply
- Or to hold a constant voltage out along the feeders on the low-voltage side for varying load conditions
- Also termed as tap changing under load (TCUL) transformers



"Tap changing switch" by BillC at English Wikipedia

# Voltage regulators and capacitors

- Voltage regulators: induction devices in shunt or series with regulated circuit for the control of its voltage
- Capacitors: perform power factor correction with additional switching and protective elements



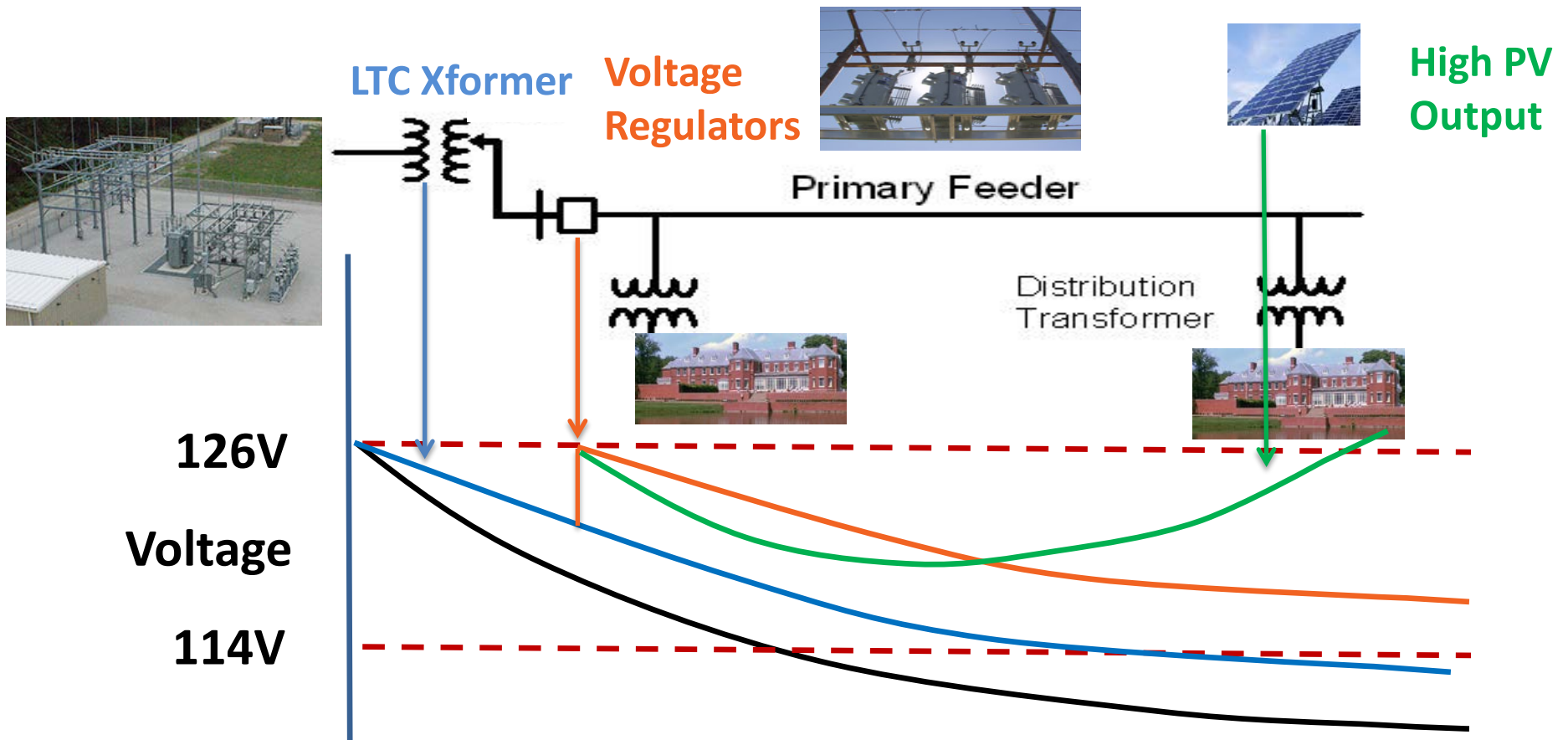
# Volt/Var control (VVC)

- Traditional VVC relies on individual, independent, stand-alone control devices that react to local measurements
- Challenged by rapid changes in distribution loads due to penetration of distributed generations and electric vehicle charging



Source: EPRI Smart Grid Demo

# An example

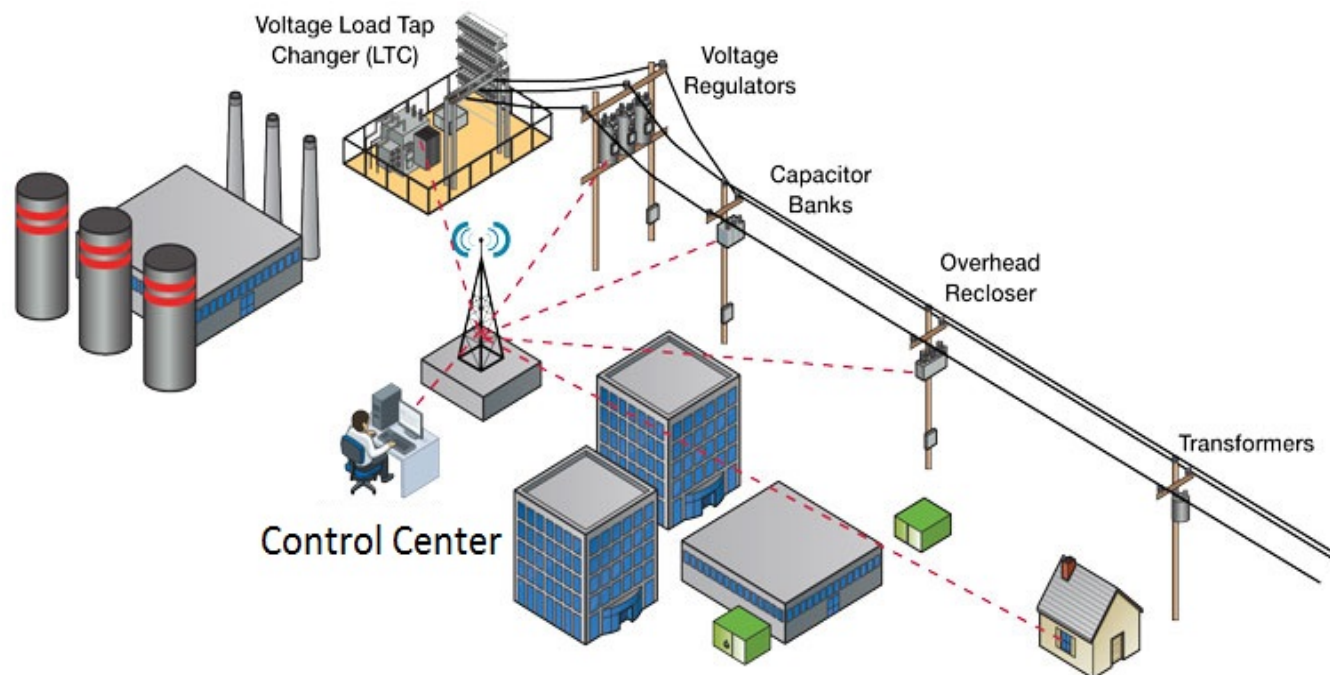


- Real power injection increases local voltage
- Non-decreasing voltage profile due to DG outputs



# Centralized VVC

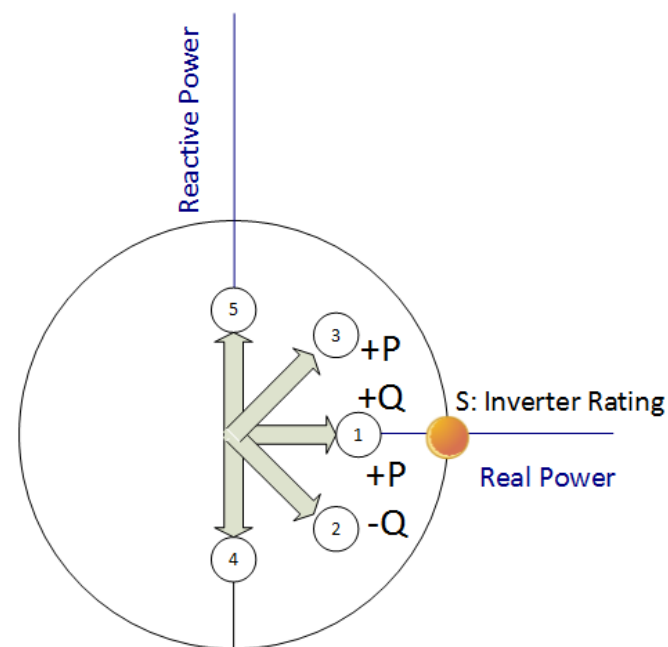
- An integrated approach that computes and executes coordinated control for all devices [Cf. optimal power flow (OPF)]
- Enabled by two-way communications between a centralized controller and remote meters/devices





# Additional VAR sources

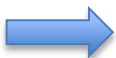
- DGs/battery devices also offer new venues for VAR support
- Synchronous generation: exciter control
- Inverter-connected devices: VAR control  
[Lopes et al '07],[Turitsyn et al '11]
- Most of these VAR sources currently operated under fixed power factor




# Optimal voltage control


- OPF problem formulation [Farivar et al '12] [Zhang et al '15]
- A two-stage approach of slow/fast time-scales [Robbins et al '13]
- (De-)centralized solvers for three-phase systems [Dall'anese-Zhu-Giannakis'13]

minimize *Power losses* + *Load demand* + *VAR costs*

subject to  $\underline{V} \leq V \leq \bar{V}$   Voltage regulation

$\underline{P}_g \leq P_g \leq \bar{P}_g$   DG limit constraints

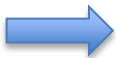
$\underline{Q}_g \leq Q_g \leq \bar{Q}_g$

*Power flow equations*  Convex relaxation

# Optimal transformer tap control

- An OPF approach to optimize three-phase transformer taps
- A virtual-bus based transformer model
- (De-)centralized solvers using convex relaxation

minimize *Power losses* + *operational costs*

subject to  $\underline{V} \leq V \leq \bar{V}$   Voltage regulation

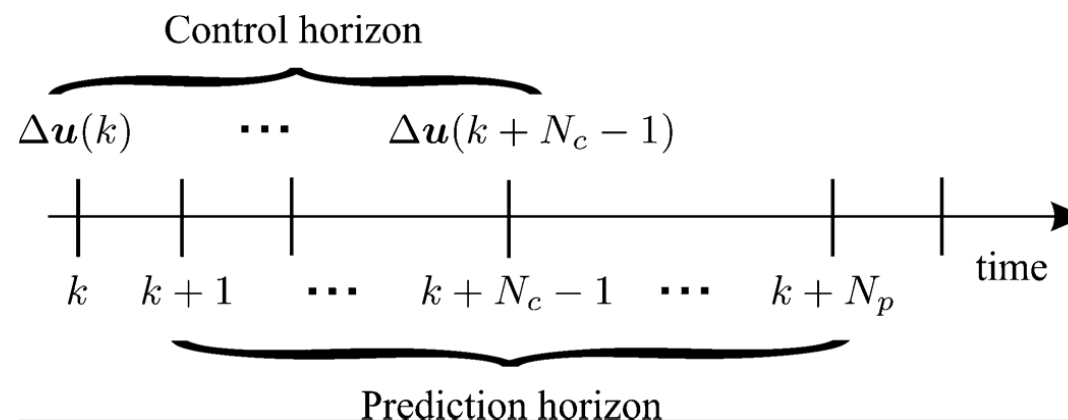
$\underline{a}V_p \leq V_s \leq V_p\bar{a}$   Tap constraints

*Power flow equations*  Convex relaxation

B. A. Robbins, H. Zhu, and A. D. Domínguez-García, "Optimal Setting of the Taps of Voltage Regulation Transformers in Distribution Systems," *IEEE Trans. Power Systems*, 2015.

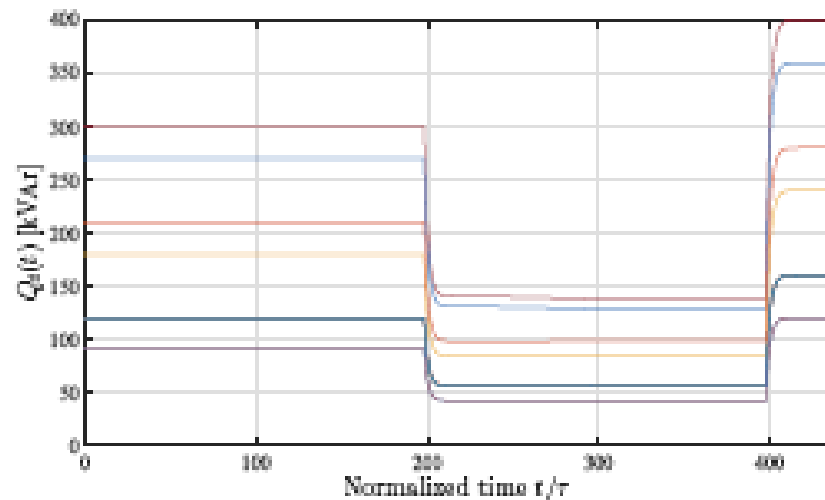
# Alternative approaches

- Adaptive control: sequentially updates the DG VAR output at each bus [Yeh et al '12]
- A model predictive control (MPC) framework [Valverde et al '13], [Wang et al '14]
  - Coordinated management of DG real/reactive power generation and transformer tap positions



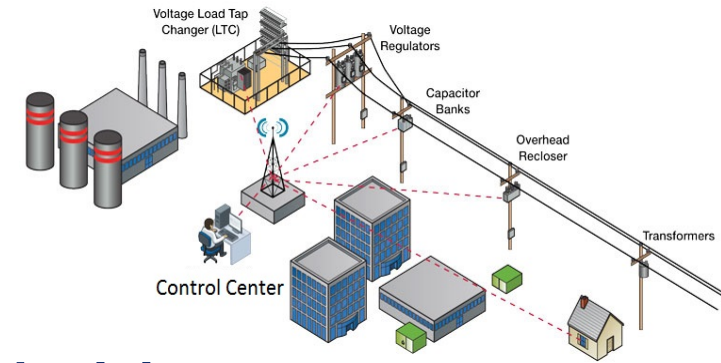
# Stochastic control

- Stochastic-approximation VVC method that deals with system uncertainty and measurement noise [Bazrafshan et al '14], [Kekatos et al '15]
- A dual-subgradient approach that accounts for the dynamics/delay in updating inverter control setpoints [Dall'anese et al '15]



E. Dall'Anese, S. V. Dhople, and G. B. Giannakis, "Photovoltaic Inverter Controller Seeking AC Optimal Power Flow Solutions," *IEEE Trans. on Power Systems*, to appear. [Online] Available at: <http://arxiv.org/abs/1501.00188> 13

# Summary of centralized VVC

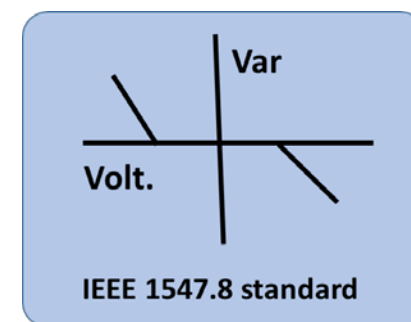


- With all information available, centralized decision-making can improve the overall system operations
- But it requires high-quality high-throughput two-way **communications** to remote devices
- Communication failures/delays can result in **suboptimal** and **instable** control, especially for distribution systems with rapid load variations and intermittent DGs

1. Local VVC at no communication requirements
2. Distributed VVC resilient to communication link failures

# Fast local inverter VAR control

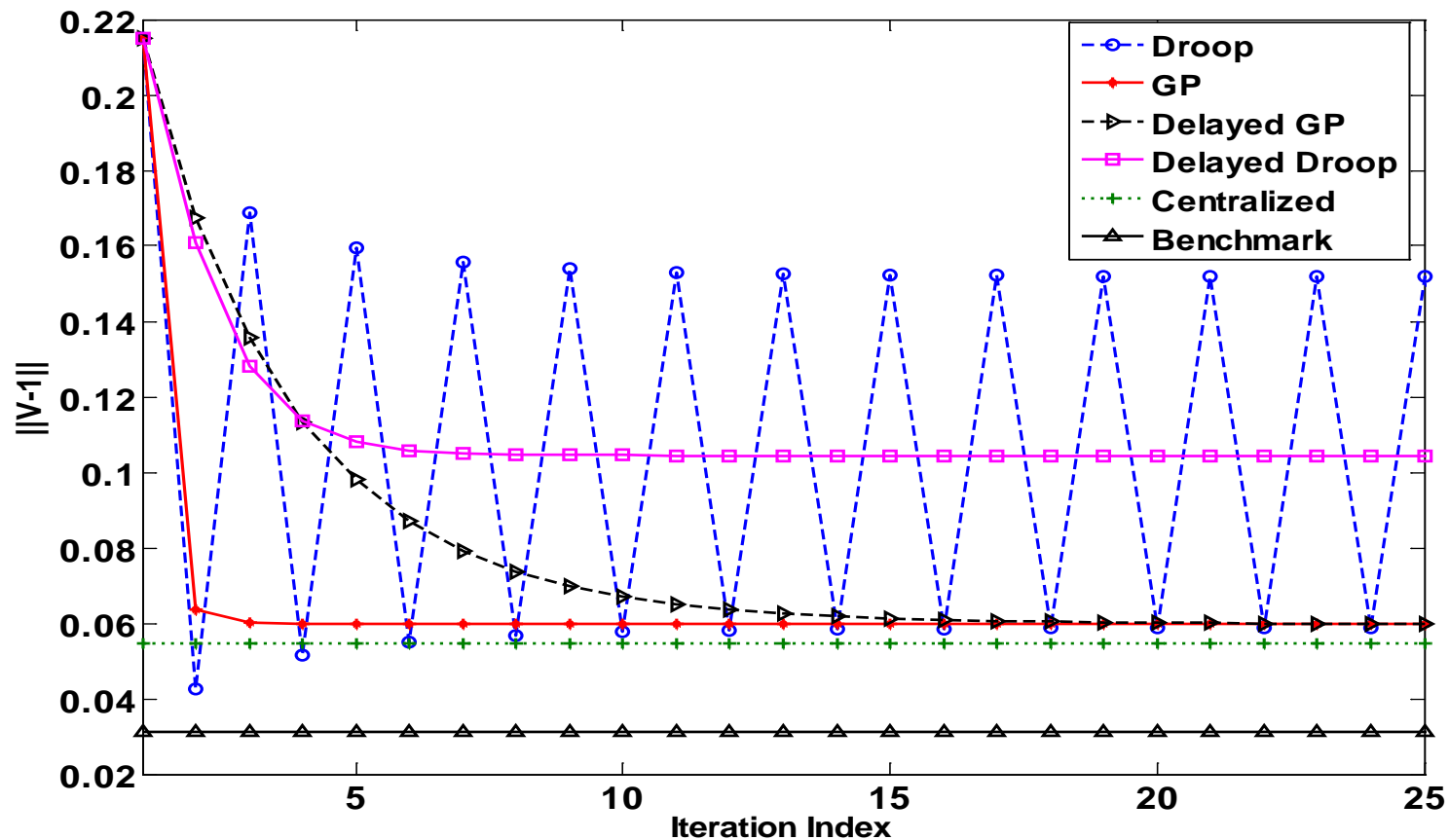
- At no communications, inverters can determine VAR outputs based on local bus voltage magnitudes
  - Can quickly and accurately respond to voltage violations
  
- Droop control (IEEE 1547.8) [Farivar et al '13]
  - Instability arises under high PV penetration [Jahangiri et al '13]
  - Integral control at unlimited inverter VAR [Zhang et al '12], [Li et al '14]



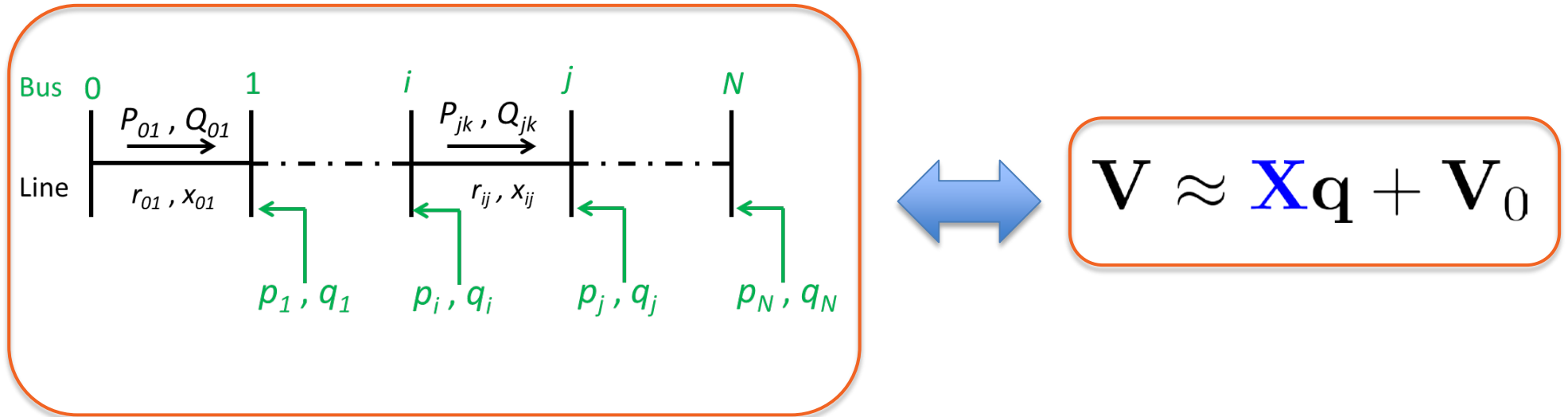


# Unstable droop control

- A radial 16-bus single-phase case with  $r/x$  ratio  $\approx 0.635$
- Bus loading  $\sim (70+j30)$ kVA; abundant VARs ( $\pm 100$ kVar)



# Matrix LinDistFlow model



- $\mathbf{X}^{-1} = \mathbf{B}$  is the power network  $\mathbf{B}$  bus matrix (dc power flow)
- Equivalent to fast decoupled power flow (FDPF) model

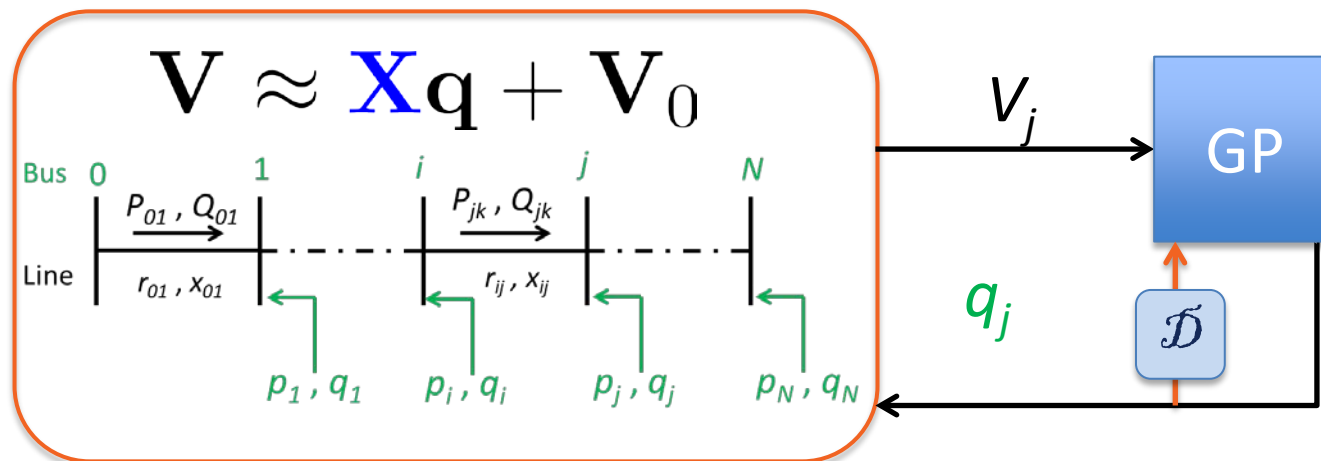
$$\Delta \mathbf{V} \approx \mathbf{X} \Delta \mathbf{q} \longleftrightarrow \Delta \mathbf{q} \approx \mathbf{B} \Delta \mathbf{V}$$

# Gradient-Projection (GP) based VAR control

minimize *Weighted V mismatch* + *VAR costs*  
 $(\mathbf{V} - \mathbf{1})^T \mathbf{B}(\mathbf{V} - \mathbf{1}) + \mathbf{q}^T \mathbf{C} \mathbf{q} \longrightarrow$  Quadratic

subject to  $\underline{q}_j \leq q_j \leq \overline{q}_j$  at every bus  $j$

- Optimal GP iteration  $q_j(t+1) = \mathbb{P}_j [(1 - d_j c_j) q_j(t) - d_j (V_j(t) - 1)]$

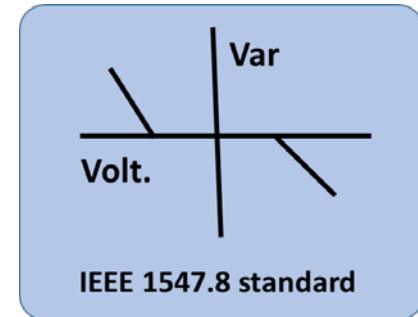


# Features of GP-based local control

- **Droop control: setting**  $d_j = 1/c_j$ 
$$q^g(t+1) = \mathbb{P}_j[-d_j(V_j(t) - 1)]$$
  - $c_j$  has to be large enough to ensure stability [Farivar et al '13]
  - A delayed + droop scheme in [Jahangiri et al '13]
- Requiring **minimal** coordination with control center
  - GP-based control can be stabilized with any arbitrary  $c_j$
- Generalizing **unbalanced** (three-phase) distribution networks

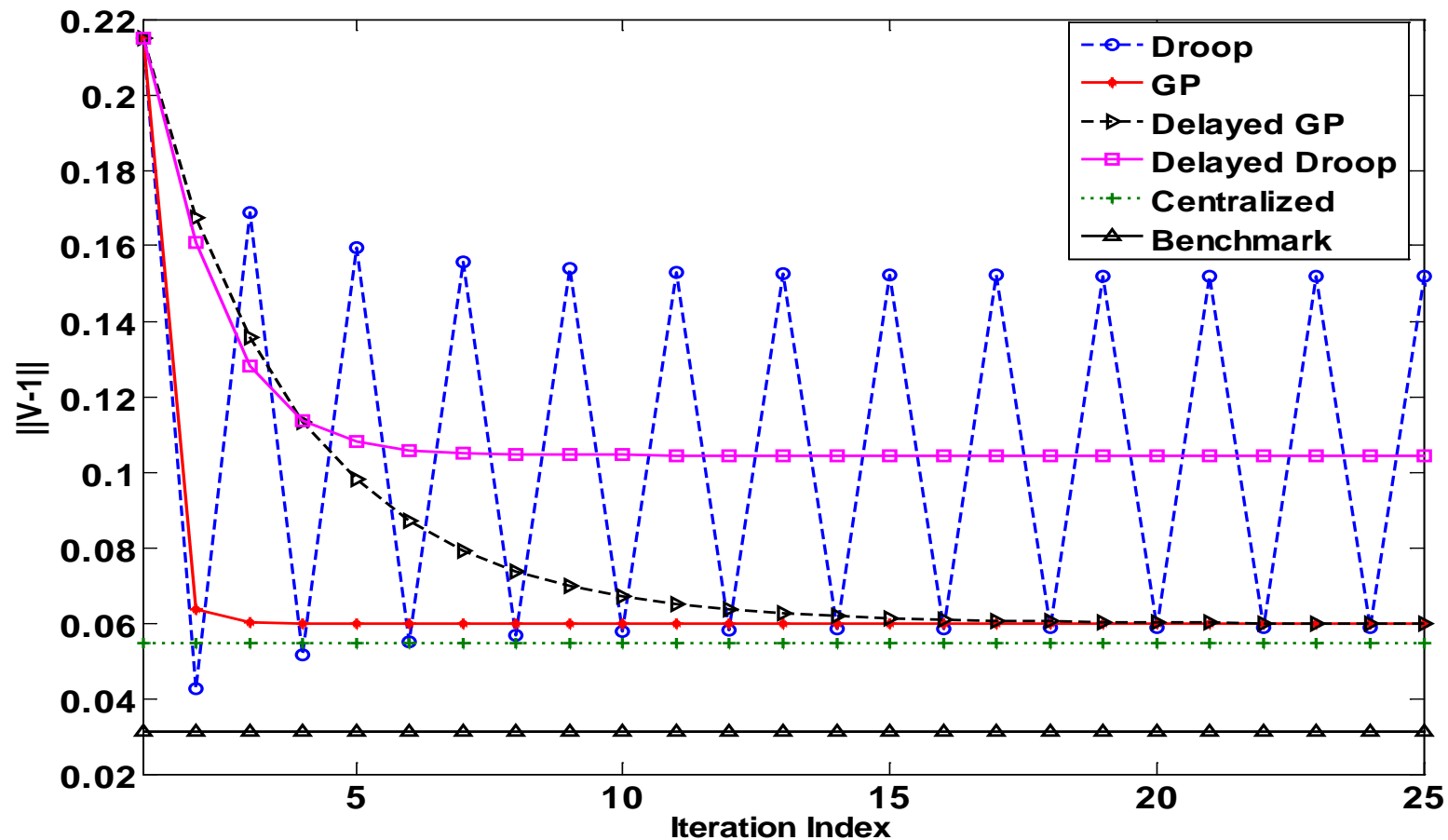
$$\mathbb{B}\Delta v \approx \Delta q$$

- Allowing for **asynchronous** control updates (**plug-and-play**)



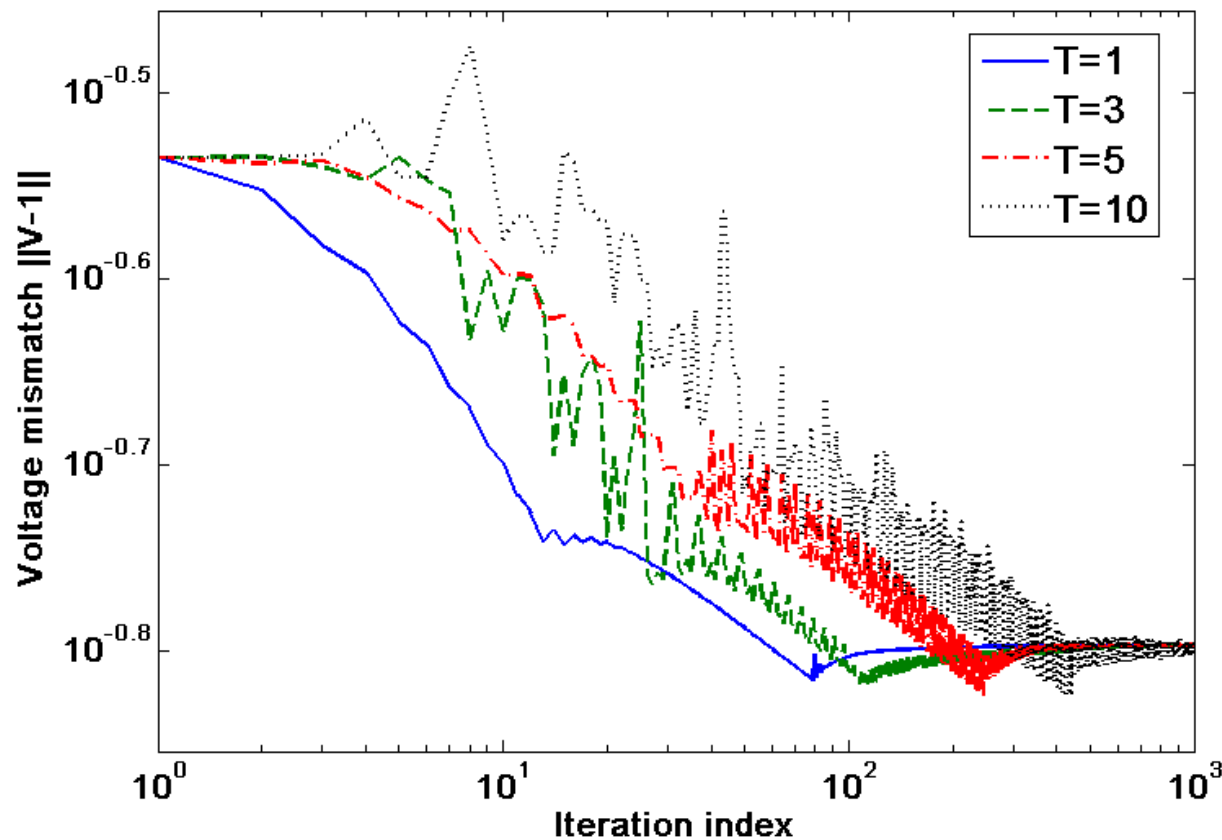
# Static system tests

- A radial 16-bus single-phase case with  $r/x$  ratio  $\approx 0.635$
- Bus loading  $\sim (70+j30)$ kVA; abundant VARs ( $\pm 100$ kVar)
- **NOTE:** voltage obtained by solving ac power flow (not the linearized model)!



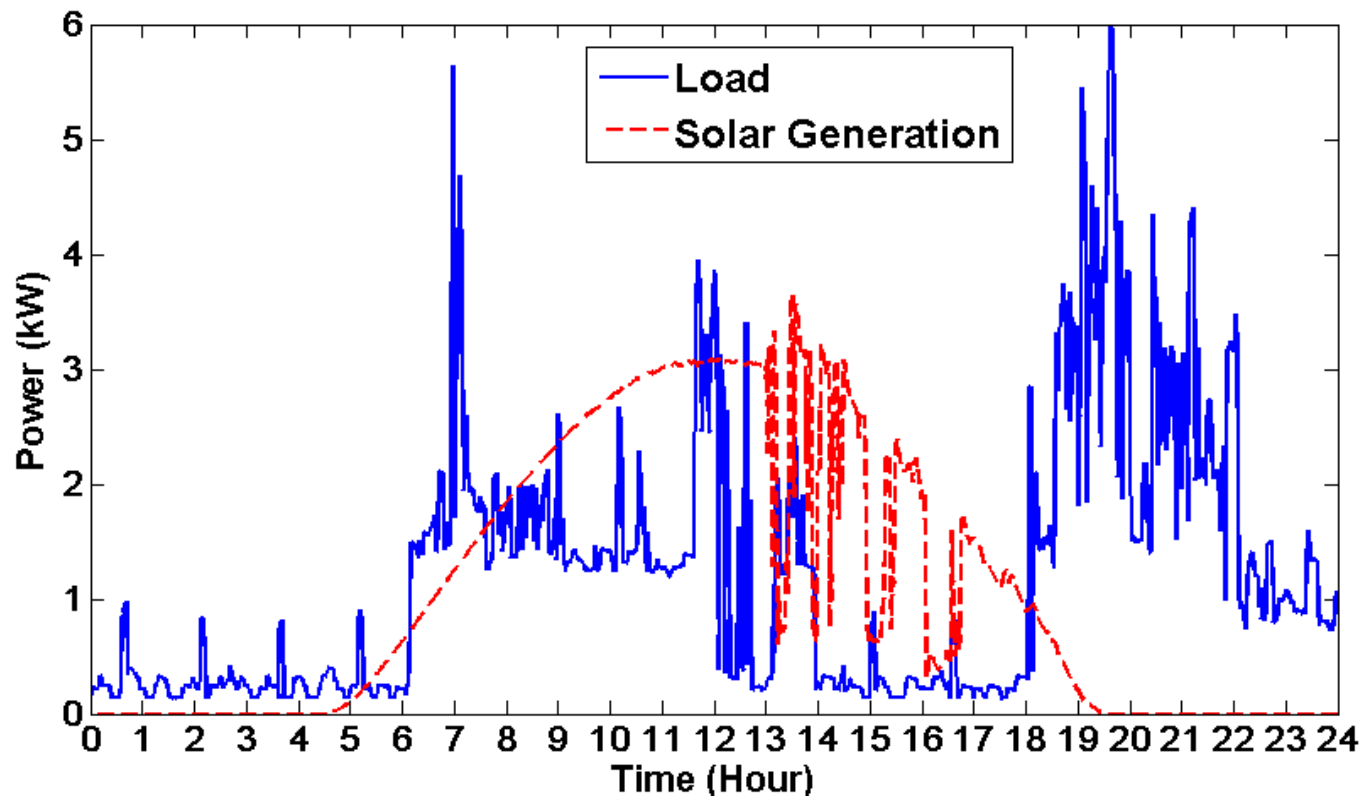
# Asynchronous updates

- Each bus randomly updates every  $t \in [1, T]$  iterations
- Guaranteed to converge; larger  $T$  slows down convergence speed



# Dynamic system tests

- Daily profile of residential load and solar PV output every minute
- Heavy loading during the evening (18:00-22:00)
- High solar variability in the afternoon (12:00-17:00)

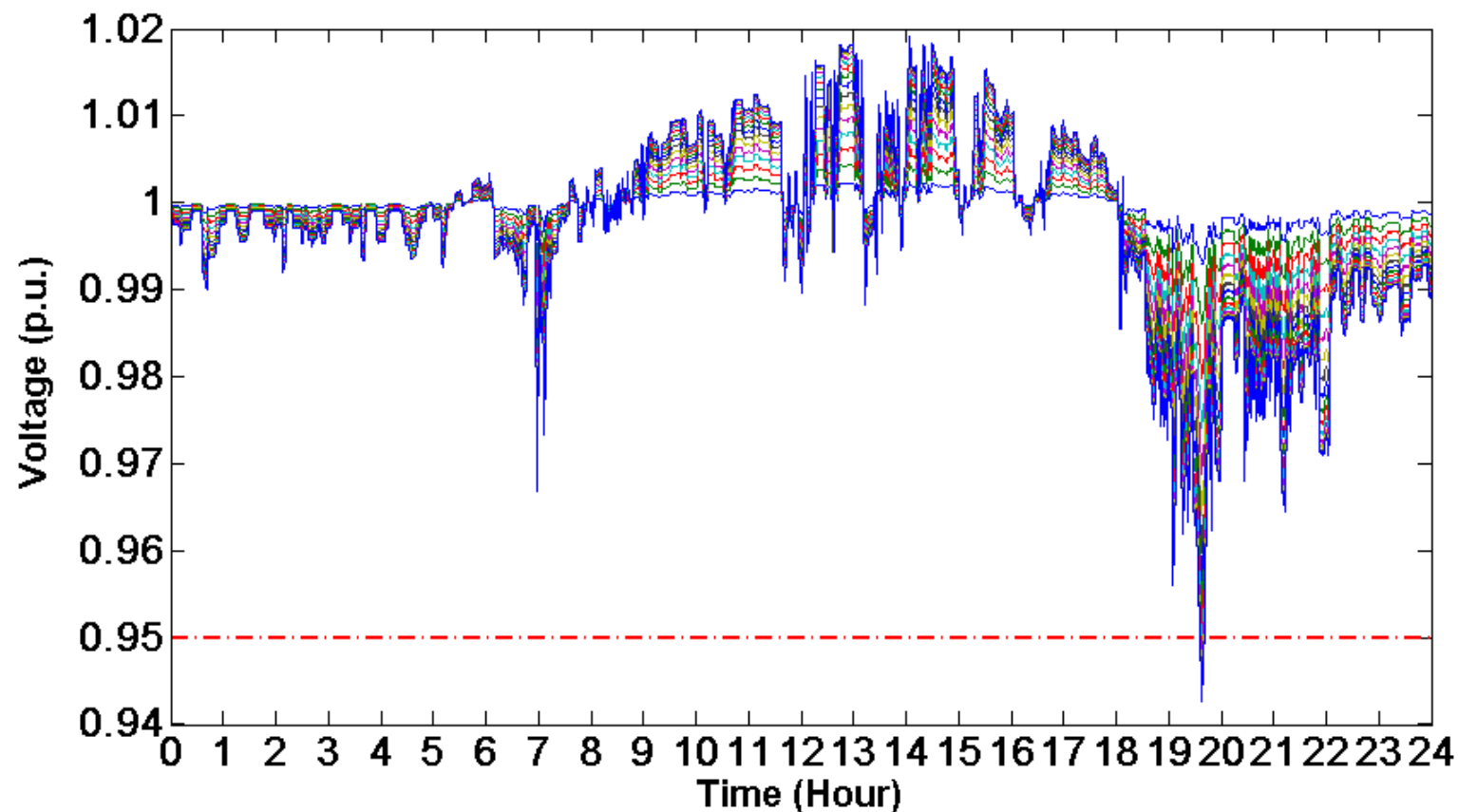


Source: <https://archive.ics.uci.edu/ml/datasets/Individual+household+electric+power+consumption>



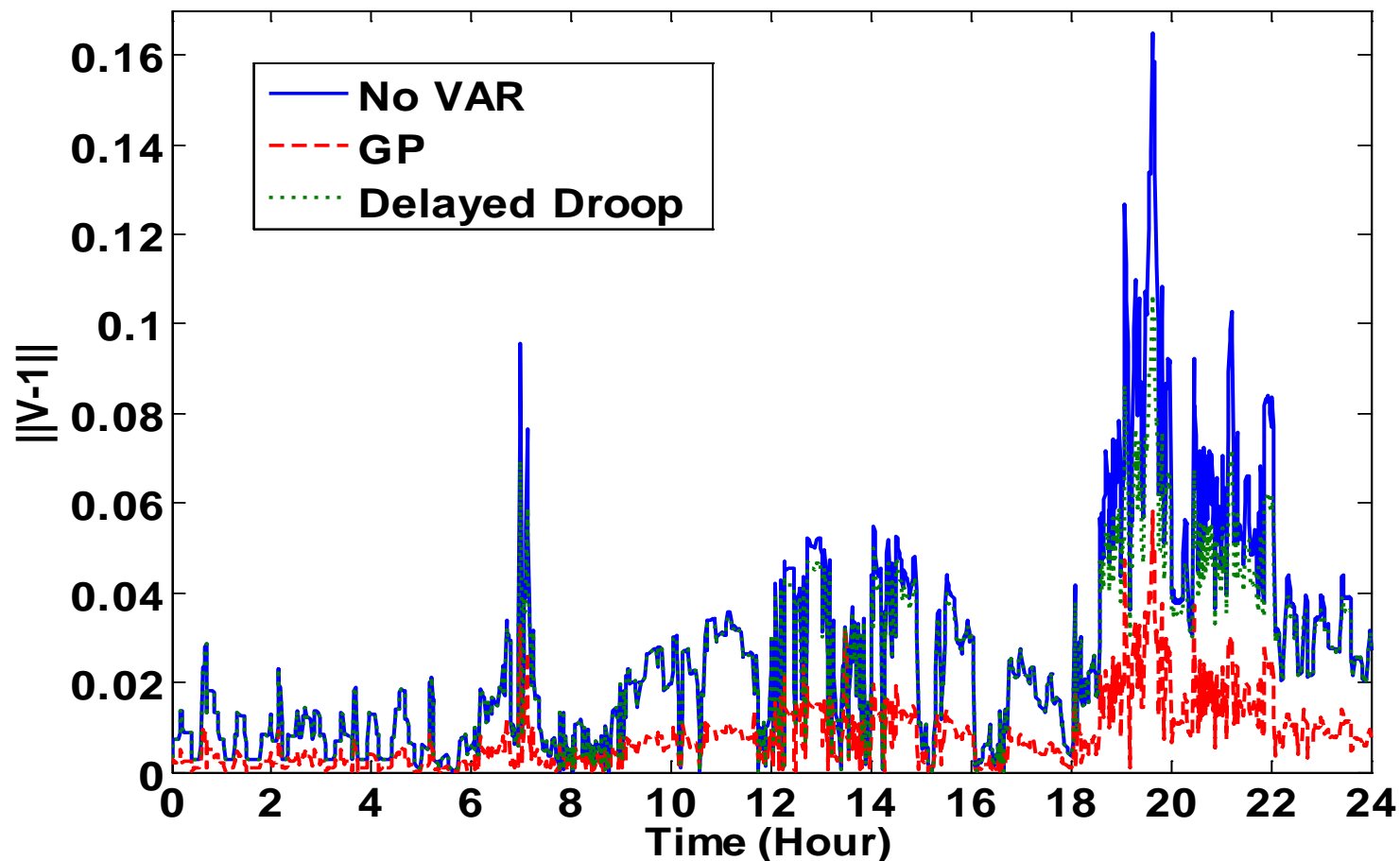
# Daily voltage profile at no inverter VAR

- Over-voltage during noon hours, and low-voltage in the evening
- More severe at the end of feeder



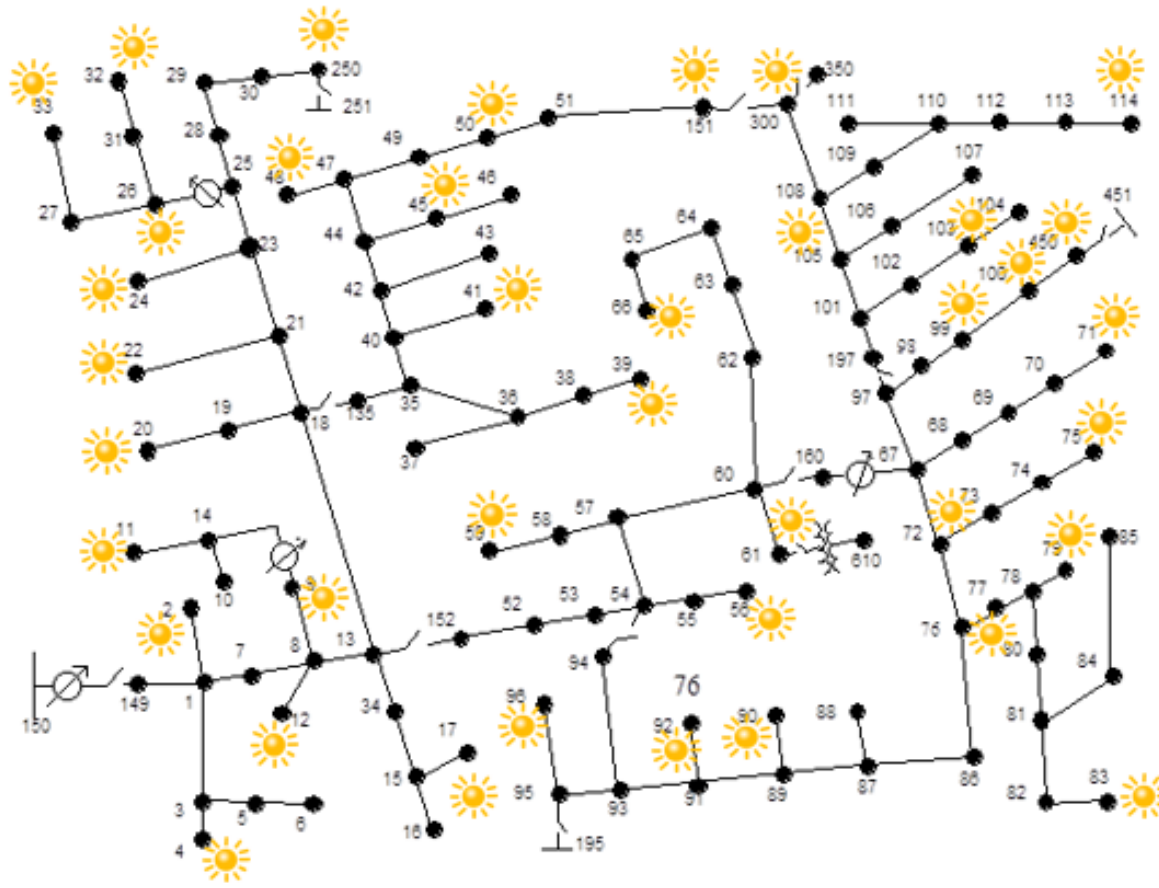
# Dynamic VAR control

- Local VAR control updates every 5 seconds
- Proposed GP-based scheme effectively reduce voltage mismatch



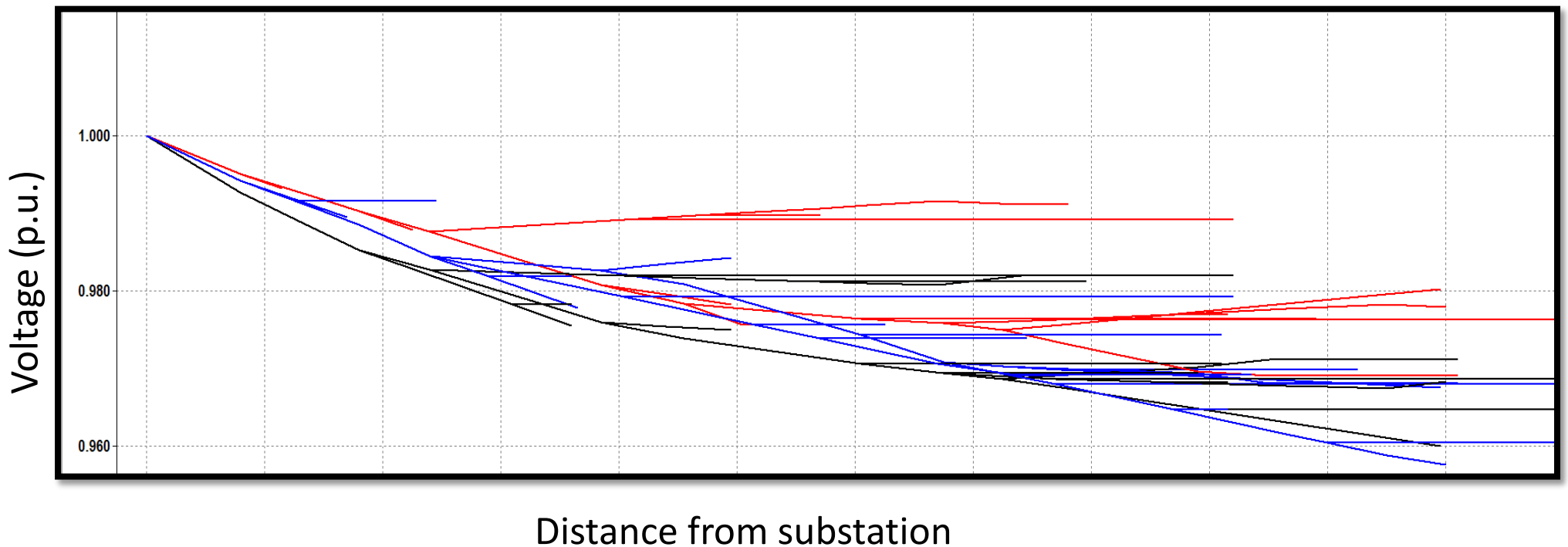
# Three-phase system tests

- Local control can be easily implemented on three-phase systems
- IEEE 123-bus test cases with 30% solar penetration



# Three-phase voltage profile

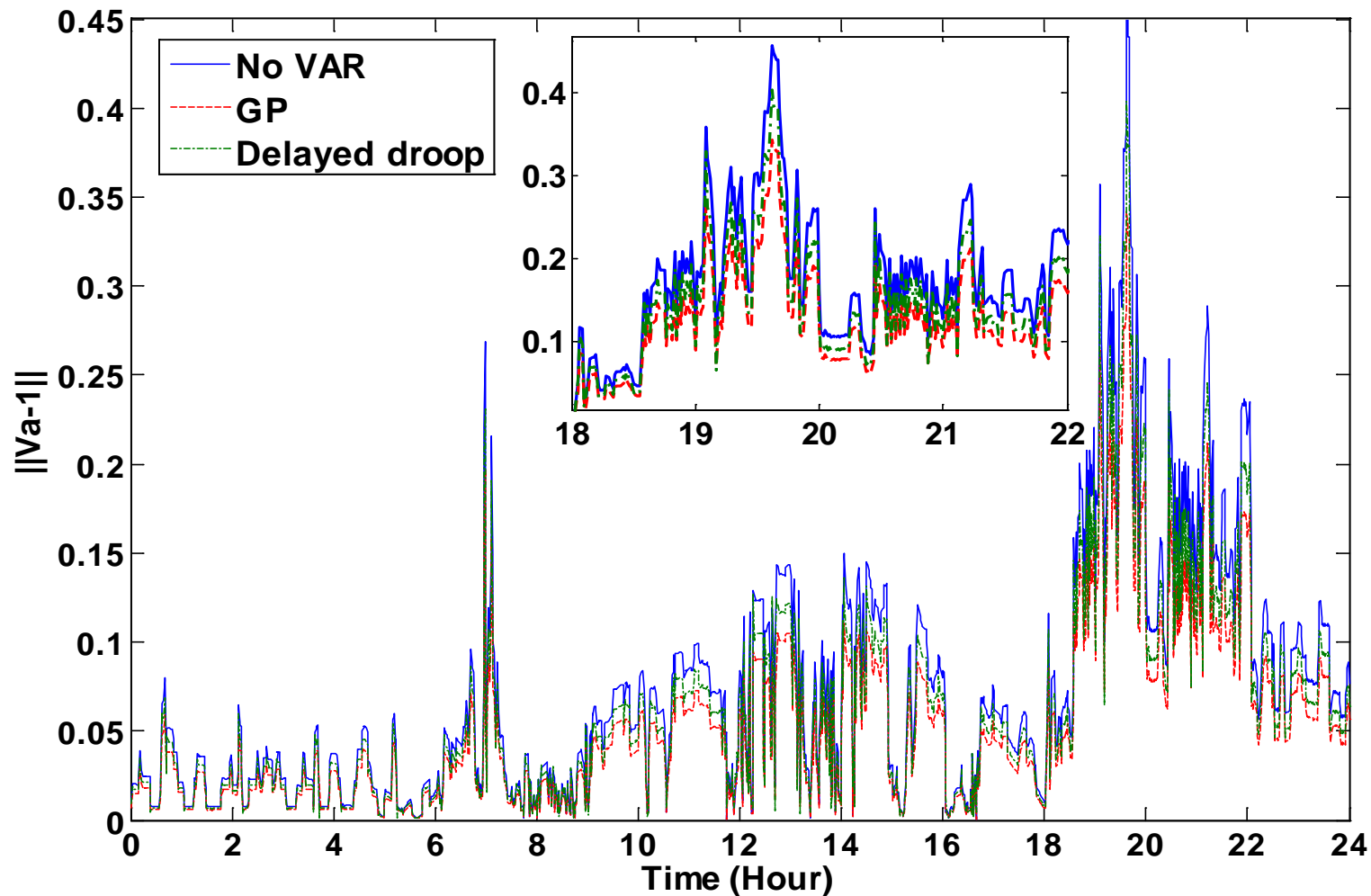
- Actual voltage profile obtained using OpenDSS
  - Phase a: black; Phase b: red; Phase c: blue



# Dynamic voltage mismatch

Need communications to share information globally!

- Local control less effective under low solar penetration level



# Drawbacks of local control

- It minimizes a **weighted** mismatch norm, instead of  $\|\mathbf{V} - \mathbf{1}\|^2$

minimize **Weighted  $V$  mismatch** + **VAR costs**

$$(\mathbf{V} - \mathbf{1})^T \mathbf{B}(\mathbf{V} - \mathbf{1}) + \mathbf{q}^T \mathbf{C} \mathbf{q}$$

subject to  $\underline{q}_j \leq q_j \leq \overline{q}_j$  at every bus  $j$

- Global objective: unweighted voltage mismatch norm**

minimize  **$V$  mismatch** + **VAR costs**

$$\|\mathbf{V} - \mathbf{1}\|^2 + \mathbf{q}^T \mathbf{C} \mathbf{q}$$

subject to  $\underline{q}_j \leq q_j \leq \overline{q}_j$  at every bus  $j$

# Distributed VAR control

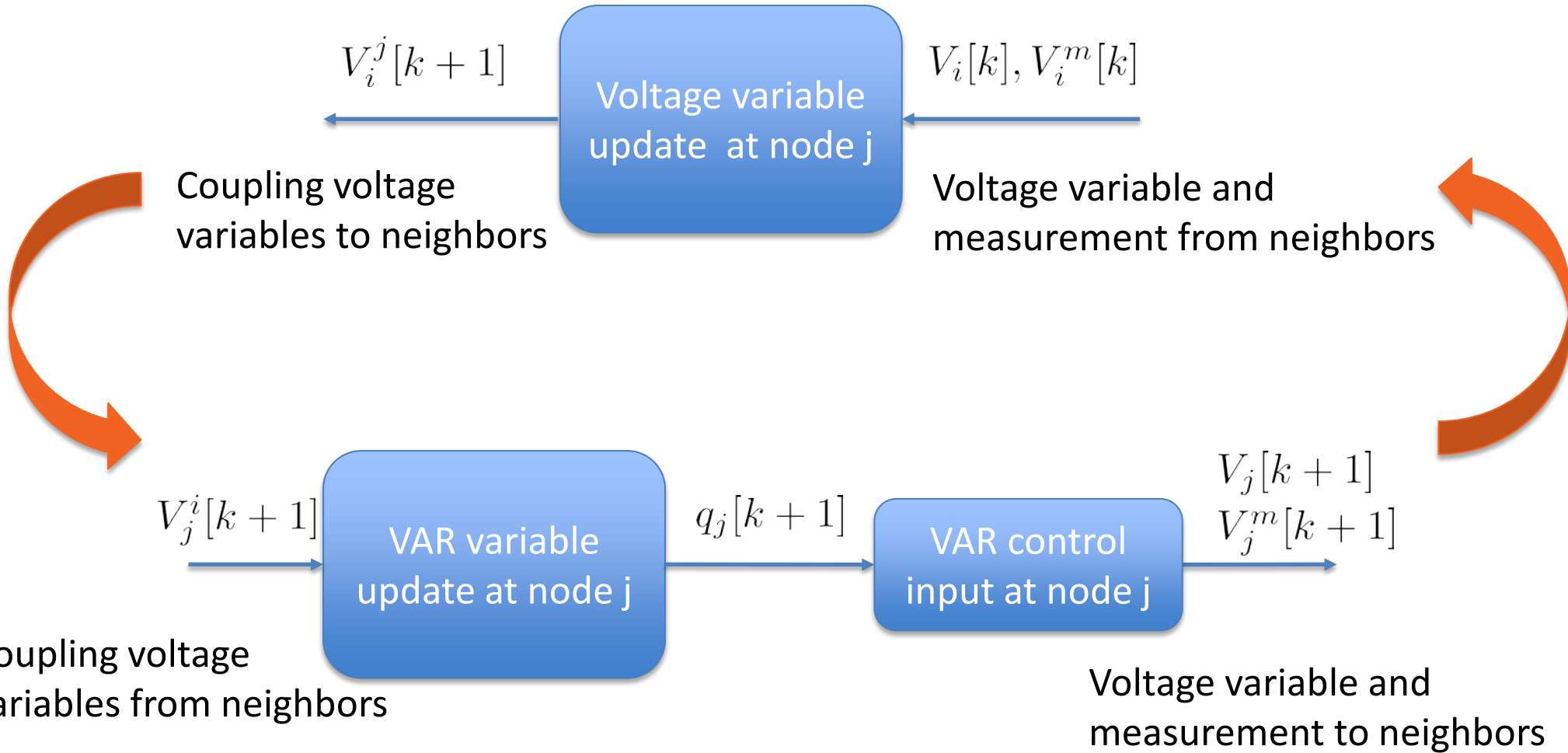
- Key of parallelization lies in the structure of  $\mathbf{B}\Delta\mathbf{V} \approx \Delta\mathbf{q}$
- Power flow constraint at bus  $j$  just involves its neighboring buses

$$\sum_{\forall i \in \mathcal{N}_j} B_{ji}V_i + B_{jj}V_j = q_j + c_j$$

- Distributed solver (ADMM): communications between one-hop neighboring buses
- Also holds for unbalanced three-phase systems  $\mathbf{B}\Delta\mathbf{v} \approx \Delta\mathbf{q}$



# Communication Links



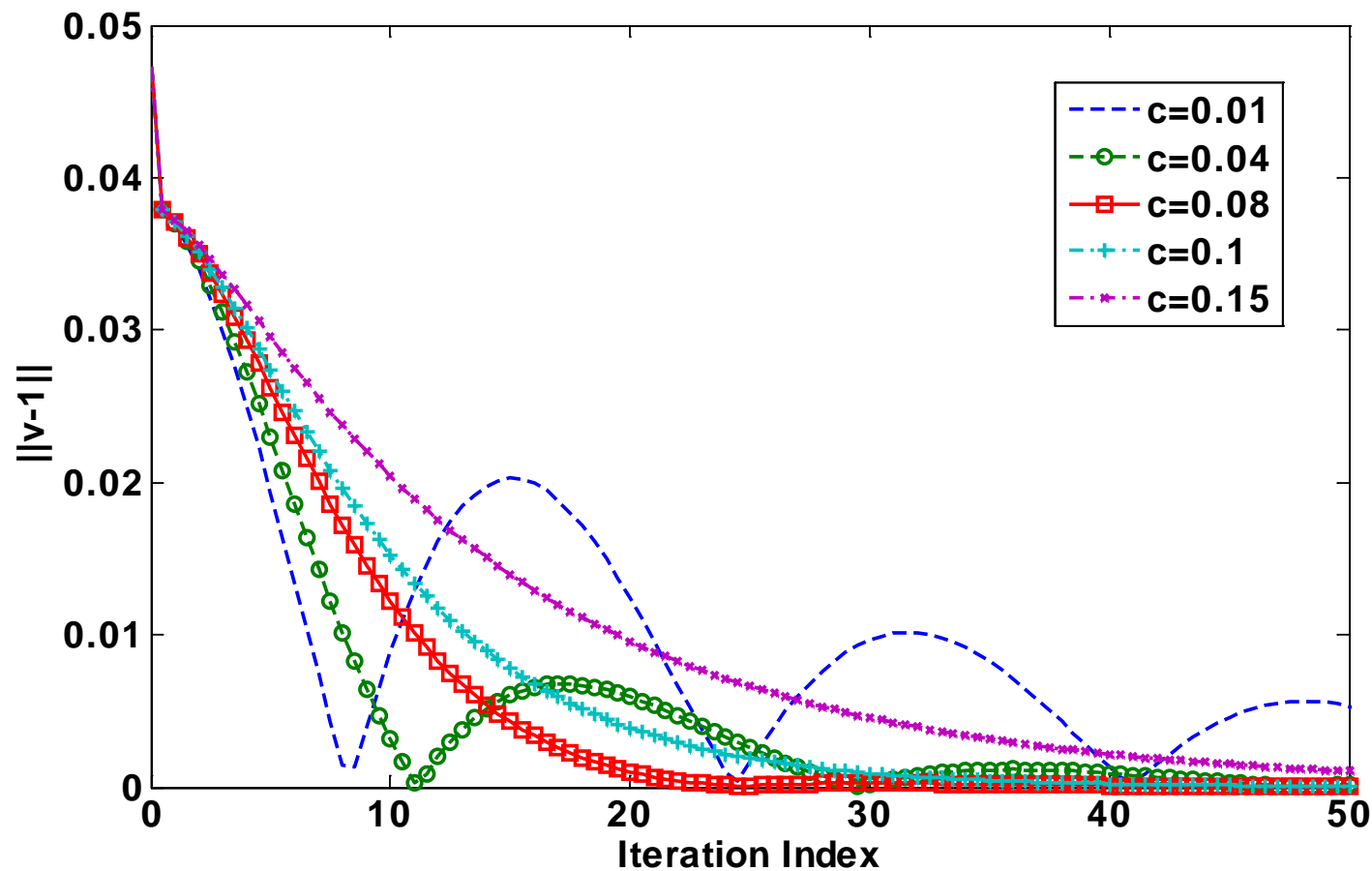
# Features of distributed control

- Simple local computation tasks: linear /QP updates
- Implemented **online** by incorporating dynamic voltage measurement
  - Neighboring buses only exchange voltage variables
  - Existing methods collect/exchange real/reactive power measurements
- Extended to unbalanced three-phase systems
- Asynchronous updates guaranteed to converge [Lutzeler et al ' 13]

$$\mathbb{B}\Delta v \approx \Delta q$$

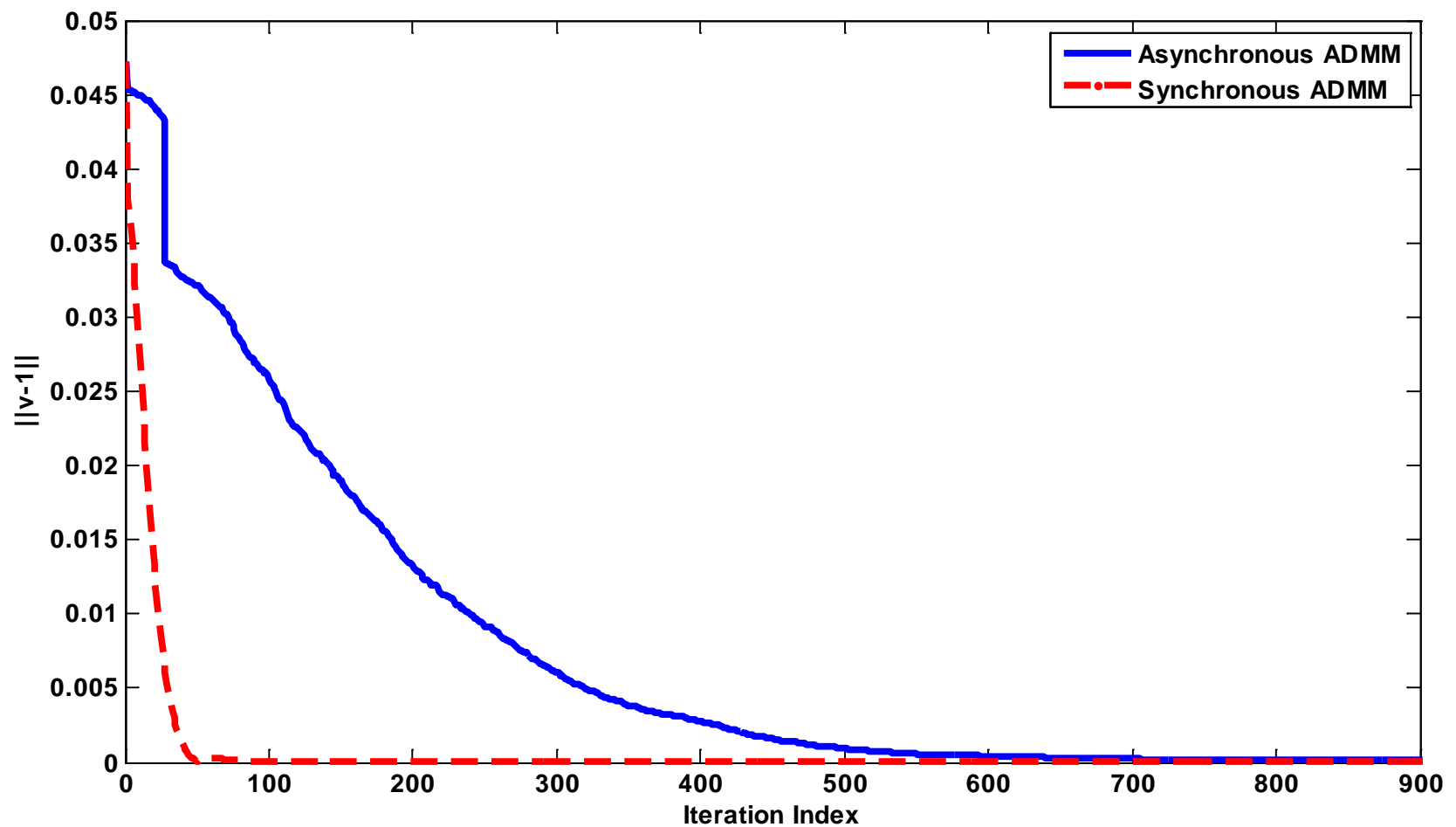
# Static system tests

- The same 16-bus single-phase case with  $r/x \approx 0.635$
- Various VAR provision cost coefficients  $c$



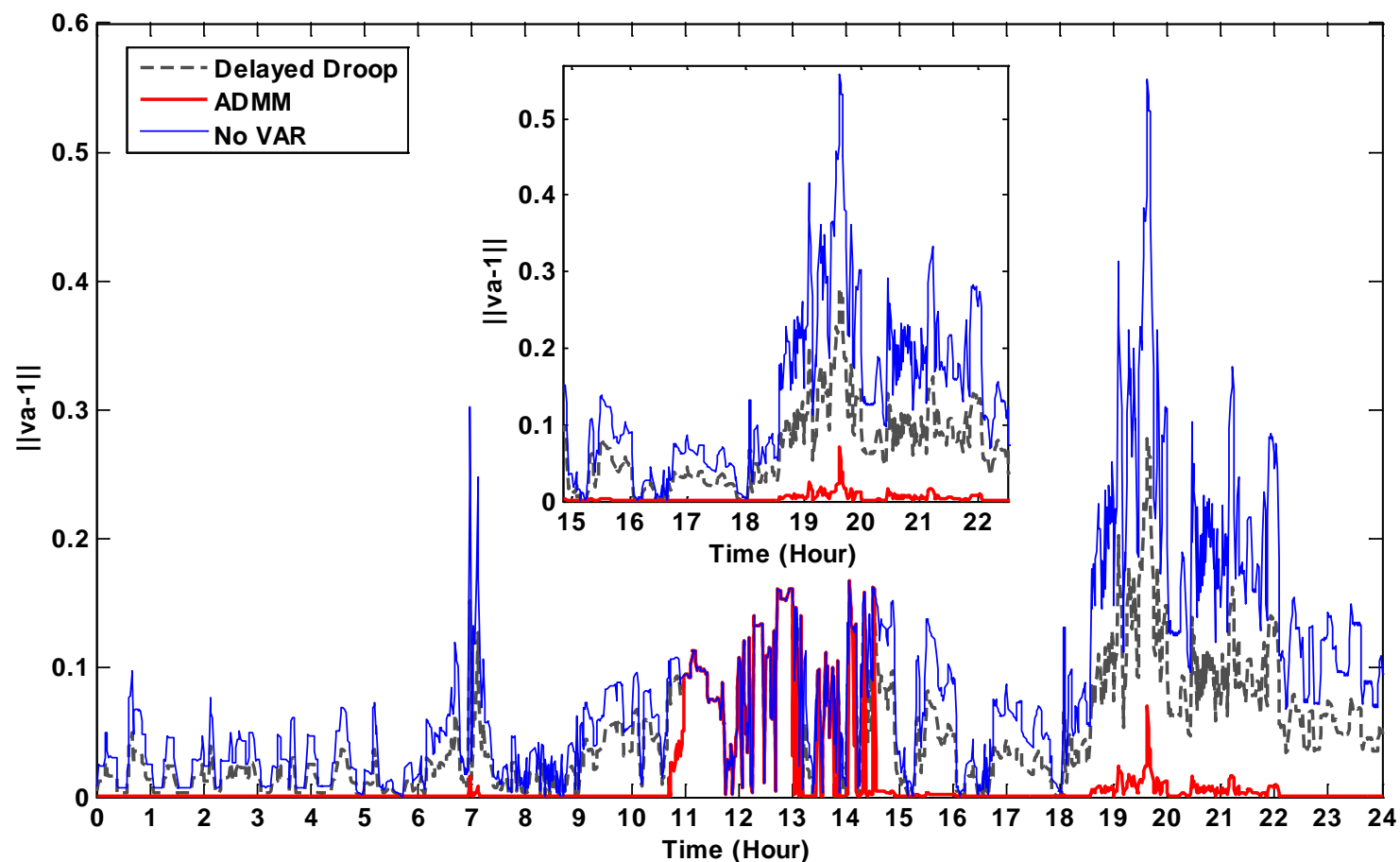
# Asynchronous updates

- Each link randomly fails with given probability  $1/|\mathcal{N}_j|$



# Dynamic tests for the 123-bus system

- Both local and distributed methods update every 3 seconds
- Distributed control more effectively reduces voltage mismatch



# Conclusions

- **Distribution system voltage control challenged by increasing load variations and intermittent DG output**
- **GP-based local control tackles the instability of droop control**
- **Distributed control seeks the globally optimal solution**
- **Both applicable to unbalanced systems and imperfect update/communication scenarios**
- **Future research: how does it interact with LTC or other devices?**

# Acknowledgements

- Collaboration work with UIUC student H.-J. (Max) Liu and colleagues Drs. Alejandro Dominguez-Garcia and B. Robbins (now at PC Krause), as well as former UMN colleagues, Drs. E. Dall'anese (now at NREL) and G. B. Giannakis; also discussions with Dr. George Moustakides (Rutgers U.)
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